

2020 Basic Nuclear Engineering 1 Lecture note (1)

- Nuclear Energy –

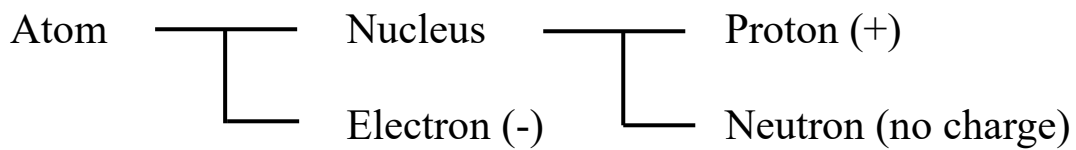
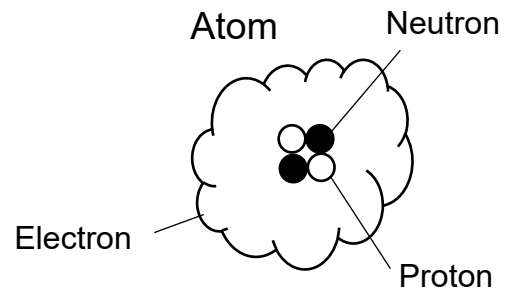
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1. Nuclear Energy

1.1 Origin of nuclear energy

• Structure of atom



• Relation between energy and mass

$$E = m c^2$$

E : energy

m : mass

c : the speed of light ($=3 \times 10^8$ m/s)

• Chemical energy and nuclear energy

Chemical energy (Combustion of coal, oil, etc.)

Change of chemical binding

→ small reduction of mass

→ energy release

Nuclear energy (Nuclear reactor, Sun)

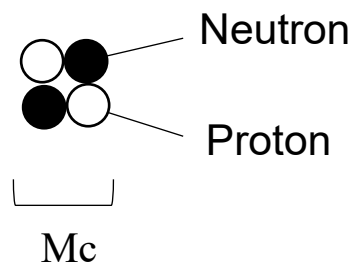
Change of nuclear binding

→ change of mass

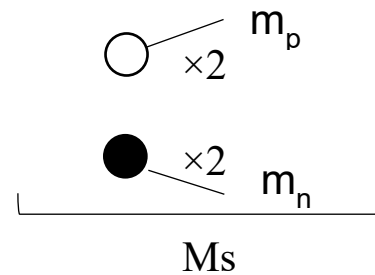
→ energy release

• Mass defect and binding energy

Nucleus



Protons and neutrons



$M_c < \text{Total mass of protons and neutrons (} M_s \text{)}$

$$\Delta M = M_s - M_c$$

Mass defect

$$\Delta E = \Delta M c^2$$

Binding energy

• Binding energy per nuclear

(Figure) Fig of Binding energy

Composition (or fusion) of light nuclei

→ Energy release (Fusion reactor, Sun)

Splitting (or fission) of heavy nuclei

→ Energy release (Nuclear reactor)

1.2 Radioactivity

The process that nucleus changes the number of protons and neutrons spontaneously

- α -decay: An alpha-particle (two protons + two neutrons) is emitted

Atomic number -2, Mass number -4

- β -decay: A neutron in the nucleus is transformed into a proton.

An electron is emitted. (β -ray)

Atomic number +1, Mass number unchanged

The decay process → Mass defect

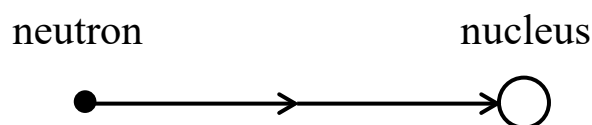
→ Energy release

Kinetic energy of the α - particle or the electron

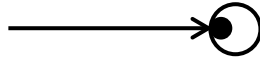
Energy of photon (γ -ray)

1.3 Nuclear reaction with neutrons

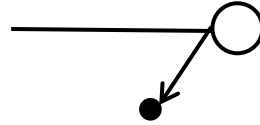
- Nuclear reactions



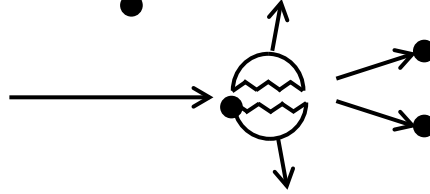
- Capture



- Scattering



- Fission



- Nuclear cross section

Index of probability of nuclear reaction

$$\text{unit } \text{b (barn)} = 10^{-24} \text{ cm}^2$$

- Capture cross section σ_c

- Scattering cross section σ_s

- Fission cross section σ_f

(unit of energy $1\text{eV} = 1.602 \times 10^{-19} \text{ J}$)

- Nuclear cross sections of ^{235}U and ^{238}U (Fig of cross sections)

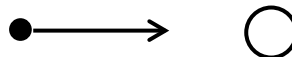
^{235}U 0.7% in natural uranium

^{238}U 99.3% in natural uranium

- Fission cross section σ_f

^{235}U large in low neutron energy ($<1\text{eV}$)

slow speed



about 1b if $E > 1\text{MeV}$
(high energy = high neutron speed)

$^{238}\text{U} \dots$ almost 0 in low energy

about 1b if $E > 1\text{MeV}$

• Capture cross section σ_c

$^{238}\text{U} \dots$ many large peaks between $5\text{eV} \sim 500\text{eV}$ (Resonance peaks)