## Collaborative Exercise 1

June 28, 2018

## Problem A:

Write answer to the following questions about design of wireless communication systems.

- 1. Calculate channel capacity  $C_0$  bps when bandwidth B=10 MHz and SNR (SNR at coverage edge)  $\gamma_0=10$  dB.
- 2. Calculate coverage  $d_0$  m (distance between basestation and coverage edge) to realize  $\gamma_0 = 10$  dB when transmit power  $P_t = 10$  mW, transmit antenna gain  $G_t = 0$  dB, receive antenna gain  $G_r = 0$  dB, carrier frequency  $f_0 = 1$  GHz, temperature T = 270 K, and propagation channel is modeled as a free space.
- 3. Calculate user rate at coverage edge  $C_{UE}$  bps/UE when UE density (density of user equipment)  $\eta = 1000 \text{ UE/km}^2$ .
- 4. Change carrier frequency from  $f_0$  to  $\widetilde{f}_0$  to achieve 100 times more user rate than  $C_{UE}$  calculated in Problem 3 under conditions of  $\widetilde{B}=B\frac{\widetilde{f}_0}{f_0}, \widetilde{G}_t=G_t\left(\frac{\widetilde{f}_0}{f_0}\right)^2$ , and  $\widetilde{G}_r=G_r$ .
- 5. How many more basestations are needed to achieve 100 times more user rate in Problem 4?

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## Problem B:

Write answer to the following questions about up/down converters.

1. Calculate and draw power spectrum of baseband (BB) transmit signal  $S_B^s(f)$  W/Hz when BB transmit signal  $s_B(t)$  is given as

$$s_B(t) = \sum_n a_n g(t - nT_s)$$
 $a_n = \begin{cases} +1, & \text{if } m_n = 0 \\ -1, & \text{if } m_n = 1 \end{cases}$ 

$$g(t) = \begin{cases} A, if |t| \le \frac{T_s}{2} \\ 0, if |t| > \frac{T_s}{2} \end{cases}$$

where  $m_n$  is a random binary message at time index n and g(t) is a rectangular pulse with pulse length (symbol period)  $T_s = 100 \ ns$ .

- 2. Calculate and draw power spectrum of analytical transmit signal  $s_A(t) = s_B(t)e^{j2\pi f_0 t}$  when carrier frequency  $f_0 = 1$  GHz.
- 3. Calculate and draw power spectrum of RF transmit signal  $s(t) = \text{Re}[s_A(t)]$ .
- 4. Calculate BB equivalent channel response  $H_B(f)$  and draw  $|H_B(f)|^2$  when channel impulse response  $h(\tau) = \delta(\tau) + \delta(\tau \tau_0)$  and  $\tau_0 = 100$  ns.
- 5. Calculate and draw power spectrum of BB receive signal  $S_B^{\gamma}(f)$  by using equivalent BB system model.