## Mathematical Modeling of Individual Choice Behavior (選択行動の数理モデル) [CVE.D401]

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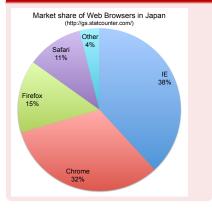
Department of Civil and Environmental Engineering School of Environment and Society Tokyo Institute of Technology

#### **Motivation of this Course**

# Individuals Choices (Decision-making)



#### Aggregate Output (Market Demand/Share)



#### **Motivation of this Course**

#### Human dimension in

- Engineering
- Planning
- Marketing
- Business
- Policy-making

#### Need for

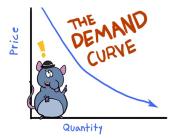
- Behavioral theories
- Quantitative methods
- Mathematical models
- Computing with programming languages or softwares

## **Aggregate Demand**



Source: marcusgohmarcusgoh.com

Homogenous population



Source: economnomnomics.com

Identical behavior

### **Disaggregate Demand**



- Heterogeneous population
- 十人一色 (ten people, one color) → 一人一色 (one people, one color) → 一人 +色 (one people, ten colors) …

- Different behaviors
- Many variables:
  - Attributes: price, travel time, reliability, frequency, etc.
  - Characteristics: age, income, education, etc.
- Complex demand/inverse demand functions.

#### Aims and Scopes

- To study the theory of "Discrete Choice Model (DCM, 離散選択モデル)", which is one of the most popular method of market demand analysis.
  - Theoretical Basis: Microeconomics, Applied Statistics, Optimization Theory, Simulation
  - Applications: Predicting future demand in transportation or other markets, Economic evaluation of transport infrastructures
- To learn knowledge on practical applications of DCM through some exercises and assignments (model estimations with some dataset).
  - "BIOGEME": Free software for estimation and simulation
  - Computer laboratories with the dataset from various research field such as "transportation", "telecommunication", "energy" and "marketing".

### Applications of DCM

- Most of early studies deal with individual mode choice.
  - McFadden (1974): Seminal paper
  - Domencich and McFadden (1975): Forecasting the passenger demand for Bay Area Rapid Transit (BART) in San Francisco.
- Other applications include:
  - Trip destination choice (Yai 1985)
  - Recreation demand (Fukuda & Morichi 1999)
  - Telephone-service choice (Train et al. 1987)
  - Occupation (job) choice (Schmidt & Strauss 1975)
  - Rail route choice in Tokyo (Yai et al. 1997)
  - Choice of a daily activity pattern (Fujii 1997)
  - Car-parking choice (Muromachi 1993)
  - Analysis of illegal-bicycle-parking (Fukuda 2004)
  - Pedestrian behavior (Fukuda et al. 2013)
  - Facial expressions (Robin et al. 2011)
  - Political party to support (Carey et al. 1995)

### BART (Bay Area Rapid Transit) and DCM





Professor D. McFadden (2001 Novel Prize in Economics Winner)

McFadden, D. "Conditional logit analysis of qualitative choice behavior," in P. Zarembka (ed.), *Frontiers in Econometrics*, pp. 105–142, Academic Press: New York, 1974.

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#### Transportation: One of the most advanced DCM applications

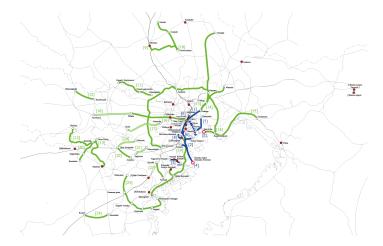
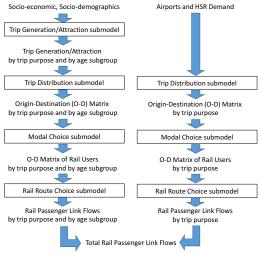


Figure: Planned rail routes in 2016 by 2030 with DCM-based demand forecasting (Kato, Fukuda, Yamashita, Iwakura and Yai, 2017)

#### Transportation: One of the most advanced DCM applications

#### Structure of Urban Rail Demand Forecast Model System in Tokyo



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#### Transportation: One of the most advanced DCM applications

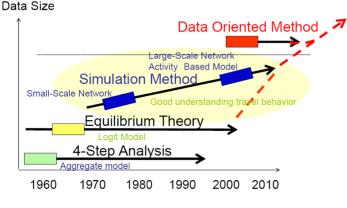
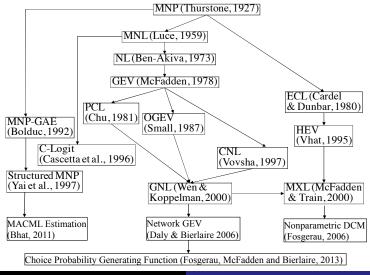


Figure: History of Travel Survey Methods (Hato, 2013)

#### **History of Discrete Choice Models**



#### **Textbooks**

- BL Ben-Akiva, M. & Lerman, S. (1985) Discrete Choice Analysis: Theory and Applications to Travel Demand, MIT Press. ["BBBW" Fully upgraded by Ben-Akiva and his colleagues. Downloadable at OCW-i]
  - Tr Train, K. (2003) Discrete Choice Methods with Simulation, Cambridge University Press. Downloadable at http://eml.berkeley.edu/books/choice2.html [Also, the Japanese version (translated by Fukuda) will be downloadable at OCW-i.]
- KM 北村隆一・森川高行 [編] (2002) 交通行動の分析とモデリン グ, 技報堂出版.
- JSCE 土木学会 [編] (1996) 非集計行動モデルの理論と応用, 土木 学会.
  - Supplemental materials will be provided at OCW-i.

#### **Class Schedule**

- (April 5) Choice Behavior and Binary Choice Models (BCM)
- (April 9) Estimation of BCM
  - (April 12) Computer Lab. (1): Estimation of BCM
- (April 16) Multinomial Choice Models: Logit and Probit
- (April 19) Specification and Estimation of Multinomial Logit Models (MNL)
- (April 23) Computer Lab. (2): Estimation of MNL
- (April 26) Statistical Tests of Discrete Choice Models
- (May 7) Independent from Irrelevant Alternatives, Forecasting and Microsimulation
- (May 10) Computer Lab. (3): Statistical Testing & Forecasting
- (May 14) Nested Logit Model (NL)
- (May 17) Issues on Sampling
- (May 21) Computer Lab. (4): NL & Sampling Issues
- (May 24) Mixed Logit Model (MXL) & Simulation-based Estimation
- (May 28) Computer Lab. (5): Estimation of MXL
- (May 31) Recent Developments of DCM in Transportation

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### **Course Evaluation and Advance Preparation**

- Class participation
- Five assignments
  - Estimation of DCM, programming and forecasting
  - The "BIOGEME" will be used in all exercises and assignments. The website of BIOGEME: http://biogeme.epfl.ch
  - Interpretation, discussion & new suggestions with your estimation results
- You may write assignments either in English or in Japanese.
- Students are required to bring a laptop PC for those five exercises.
- All lecture materials have already been uploaded on TITECH OCW-i (https://secure.ocw.titech.ac.jp/ocwi/). Students are required to print them out and bring them to each class.
- Exercise materials have also been uploaded. Students are required to download and save them into your PC in advance.

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