

# Mathematical Modeling of Individual Choice Behavior (選択行動の数理モデル) [CVE.D401]

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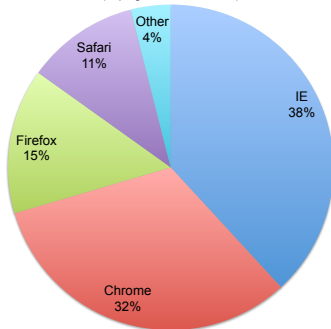
# Motivation of this Course

## Individuals Choices (Decision-making)



## Aggregate Output (Market Demand/Share)

Market share of Web Browsers in Japan  
(<http://gs.statcounter.com/>)



## Human dimension in

- Engineering
- Planning
- Marketing
- Business
- Policy-making

## Need for

- Behavioral theories
- Quantitative methods
- Mathematical models
- Computing (free) softwares

# Aims and Scopes

- To study the theory of “Discrete Choice Model (DCM, 離散選択モデル)”, which is one of the most popular method of market demand analysis.
  - **Theoretical Basis:** Microeconomics, Applied Statistics, Optimization Theory, Simulation
  - **Applications:** Predicting future demand in transportation or other markets, Economic evaluation of transport infrastructures
- To learn knowledge on practical applications of DCM through some exercises and assignments (model estimations with some dataset).
  - “BIOGEME”: Free software for estimation and simulation
  - Computer laboratories with the dataset from various research field such as “transportation”, “telecommunication”, “energy” and “marketing”.

- Most of early studies deal with individual **mode choice**.
  - McFadden (1974): Seminal paper
  - Domencich and McFadden (1975): Forecasting the passenger demand for Bay Area Rapid Transit (BART) in San Francisco.
- Other applications include:
  - **Trip destination** choice (Yai 1985)
  - **Recreation demand** (Fukuda & Morichi 1999)
  - **Telephone-service** choice (Train et al. 1987)
  - **Occupation (job)** choice (Schmidt & Strauss 1975)
  - **Rail route** choice in Tokyo (Yai et al. 1997)
  - Choice of **a daily activity pattern** (Fujii 1997)
  - **Car-parking** choice (Muromachi 1993)
  - Analysis of **illegal-bicycle-parking** (Fukuda 2004)
  - **Pedestrian behavior** (Fukuda et al. 2013)
  - **Facial expressions** (Robin et al. 2011)
  - **Political party** to support (Carey et al. 1995)

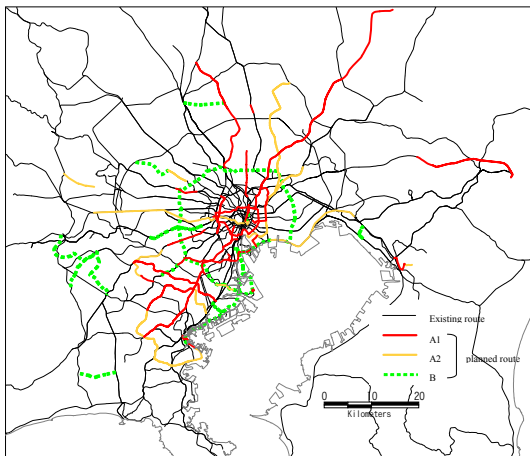
# BART and DCM



Professor D. McFadden  
(2001 Nobel Prize Winner)

"Conditional logit analysis of qualitative choice behavior," in P. Zarembka (ed.), *Frontiers in Econometrics*, pp. 105–142, Academic Press: New York, 1974.

## Transportation: One of the most advanced DCM applications



**Figure:** Planned rail routes in 2000 by 2015 with DCM-based demand forecasting (Morichi et al., 2001)

# Transportation: One of the most advanced DCM applications

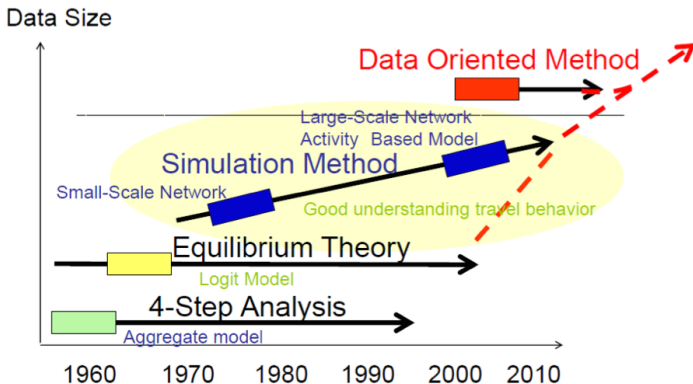
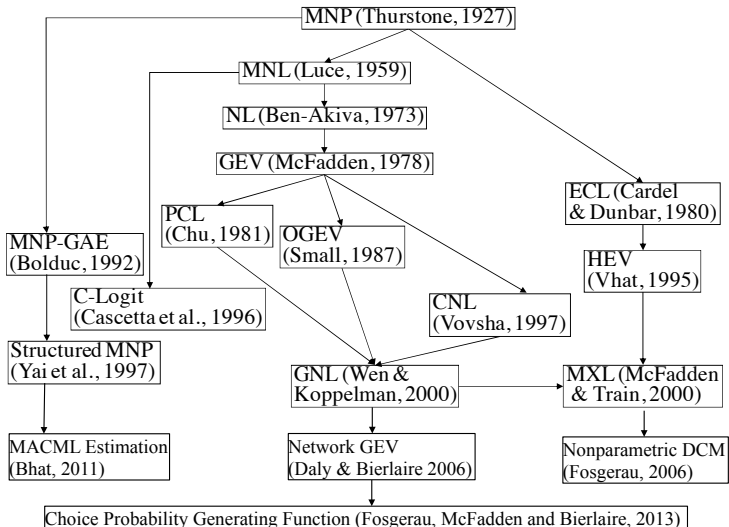


Figure: History of Travel Survey Methods (Hato, 2013)



# History of Discrete Choice Models



Original Source by Hato (2001) and updated by Fukuda

**BL** Ben-Akiva, M. & Lerman, S. (1985) Discrete Choice Analysis: Theory and Applications to Travel Demand, MIT Press.

[[BBBW] Now upgraded by Ben-Akiva and his colleagues. Downloadable at OCW-i]

**Tr** Train, K. (2003) Discrete Choice Methods with Simulation, Cambridge University Press. Downloadable at <http://eml.berkeley.edu/books/choice2.html>

[Also, the Japanese version (translated by Fukuda) will be downloadable at OCW-i.]

**KM** 北村隆一・森川高行 [編] (2002) 交通行動の分析とモデリング, 技報堂出版.

**JSCE** 土木学会 [編] (1996) 非集計行動モデルの理論と応用, 土木学会.

- Supplemental materials will be provided at [OCW-i](#).

# Class Schedule

- ① (April 7) Choice Behavior and Binary Choice Models (BCM)
- ② (April 11) Estimation of BCM
- ③ (April 14) *Computer Lab. (1)*: Estimation of BCM
- ④ (April 18) Multinomial Choice Models: Logit and Probit
- ⑤ (April 21) Specification and Estimation of Multinomial Logit Models (MNL)
- ⑥ (April 25) *Computer Lab. (2)*: Estimation of MNL
- ⑦ (April 28) Statistical Tests of Discrete Choice Models
- ⑧ (May 2) Independent from Irrelevant Alternatives, Forecasting and Microsimulation
- ⑨ (May 9) *Computer Lab. (3)*: Statistical Testing & Forecasting
- ⑩ (May 12) Nested Logit Model (NL)
- ⑪ (May 16) Issues on Sampling
- ⑫ (May 19) *Computer Lab. (4)*: NL & Sampling Issues
- ⑬ (May 23) Mixed Logit Model (MXL) & Simulation-based Estimation
- ⑭ (May 26) *Computer Lab. (5)*: Estimation of MXL
- ⑮ (June 6) Recent Developments of DCM in Transportation

# Course Evaluation and Advance Preparation

- Class participation
  - Five assignments (corresponding five exercises)
    - Estimation of DCM, programming and forecasting market shares
    - The “BIOGEME” will be used in all exercises and assignments. The website of BIOGEME: <http://biogeme.epfl.ch>
    - Interpretation, discussion & new suggestions with your estimation results
  - You may write assignments either in English or in Japanese.
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- Students are required to bring a laptop PC for those five exercises.
  - All lecture materials have already been uploaded on TITECH OCW-i (<https://secure.ocw.titech.ac.jp/ocwi/>). Students are required to print them out and bring them to each class.
  - Exercise materials have also been uploaded. Students are required to download and save them into your PC in advance.