

# Chapter 18 Cost-Effectiveness Analysis (CEA)

Cost-Effective Analysis (CEA) is a widely used alternative to CBA, especially health and defense policy. CEA compares (mutually exclusive) alternatives in terms of the ratio of their costs and a single quantified, but not monetized, effectiveness measure.

Three common constraints to doing CBA

- > If CBA is not possible, CEA may give useful information concerning the relative efficiency of alternatives.
- 1. Unwilling or unable to monetize the most important policy impact.
- 2. A particular effectiveness measure does not capture all of the social benefits of each alternative, and some of these other social benefits are difficult to monetize.
- 3. Dealing with intermediate goods whose linkage to preferences is not clear.

# Cost-Effectiveness Ratios

**Costs (C)** are measured in monetary terms.

**Effectiveness (E)** may be measured in units such as lives saved, tons of carbon dioxide reduction, children vaccinated.

Two ways: *Cost-Effectiveness ratio* (CE ratio) more commonly used.

*Effectiveness-Cost ratio* (EC ratio)

Incremental CE ratio: Alternatives policy  $i$  and policy  $j$

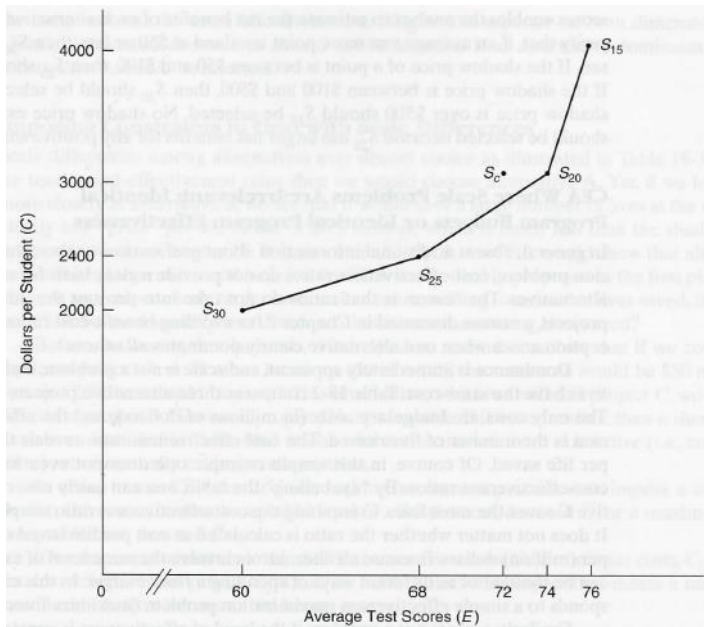
$i$ : policy implementation(with),  $j$ : status quo(without)

$$CE_{ij} = \frac{C}{E} = \frac{C_i - C_j}{E_i - E_j}$$

# Application of Cost-Effectiveness Ratio

## Student achievement Scores

	C (dollars per student)	E (average test score)	C/E (relative to no schooling)	$S_j$ (basis for comparison)	$\Delta C$ (relative to $S_j$ )	$\Delta E$ (relative to $S_j$ )	$\Delta C/\Delta E$ (incremental cost-effectiveness ratio)
$S_{30}$	2000	60	33.3	—	—	—	—
$S_{25}$	2400	68	35.3	$S_{30}$	400	8	50
$S_{20}$	3000	74	40.5	$S_{25}$	600	6	100
$S_{15}$	4000	76	52.6	$S_{20}$	1000	2	500
$S_c$	3000	72	41.7	$S_{30}$	1000	12	83.3



Frontier: best possible outcome  
southeast as possible  
 $S_c$ : Extended (weak) dominance  
...to eliminate from considered alternatives.  
located at northwest of the frontier

If assigning a shadow price to  
average test score, how about NPV?

# Cost-Effectiveness Analysis in Same Scale

<i>Cost and Effectiveness</i>	<i>Alternatives</i>		
	<i>A</i>	<i>B</i>	<i>C</i>
Cost measure (budget cost)	\$10M	\$10M	\$10M
Effectiveness measure (number of lives saved)	5	10	15
CE ratio (cost per life saved)	\$2.0M	\$1.0M	\$0.67M <sup>a</sup>
EC ratio (lives saved per million dollars)	0.5 life	1.0 life	1.5 lives <sup>a</sup>

<sup>a</sup> *CE ratio or EC ratio of the most cost-effective alternative.*

Fixed cost: Maximize effectiveness (lives saved)

Fixed effectiveness: Minimize cost (dollars)

# Imposing Constraints to deal with Scale Differences

<i>Cost and Effectiveness</i>	<i>Alternatives</i>	
	<i>A</i>	<i>B</i>
Cost measure (budget cost)	\$1M	\$100M
Effectiveness measure (number of lives saved)	4	200
CE ratio (cost per life saved)	\$250,000 <sup>a</sup>	\$500,000
EC ratio (lives saved per million dollars)	4.0 lives <sup>a</sup>	2.0 lives

<sup>a</sup> *CE ratio or EC ratio of the most cost-effective alternative.*

$$\text{Min } C_i$$

$$\text{s.t. } E_i \geq \bar{E}$$

$$\text{Min } CE_i$$

$$\text{s.t. } E_i \geq \bar{E}$$

$$\text{Max } E_i$$

$$\text{s.t. } C_i \leq \bar{C}$$

$$\text{Min } CE_i$$

$$\text{s.t. } C_i \leq \bar{C}$$

$\bar{E}$  : Minimum acceptable level of effectiveness

$\bar{C}$  : Maximum acceptable level of cost

# Illustration of the Different CE Rules

<i>Projects</i> (1)	<i>Lives Saved</i> (2)	<i>Budget Cost (\$M)</i> (3)	<i>CE Ratio (cost per life saved) (\$M/life saved)</i> (4)	<i>E ≥ 50</i>		<i>C ≤ 250</i>	
				<i>Budget Cost of Projects That Save at Least 50 Lives</i> (5)	<i>CE Ratio of Projects That Save at Least 50 Lives</i> (6)	<i>Lives Saved of Projects That Cost No More than \$250M</i> (7)	<i>CE Ratio of Projects That Cost No More than \$250M</i> (8)
A	100	250	2.5	250	2.5 <sup>a</sup>	100 <sup>a</sup>	2.5
B	20	44	2.2	—	—	20	2.2
C	100	300	3.0	300	3.0	—	—
D	50	300	6.0	300	6.0	—	—
E	10	20	2.0 <sup>a</sup>	—	—	10	2.0 <sup>a</sup>
F	100	900	9.0	900	9.0	—	—
G	60	210	3.5	210	3.5	60	3.5
H	50	200	4.0	200 <sup>a</sup>	4.0	50	4.0
I	40	100	2.5	—	—	40	2.5
J	45	110	2.4	—	—	45	2.4

<sup>a</sup> CE ratio, budget cost, or effectiveness of the most preferred alternative

# Chapter 20 How Accurate is CBA?

## Sources of Error in CBA Studies

1. Omission Errors: to exclude some impact category completely.  
by “uncertainty of the fundamental scientific relationship”
2. Forecasting Errors: to arise due to the difficulty of predicting technological change, cognitive biases, changing project specifications, etc.  
by “uncertainty” and “Over optimism: underweight low-probability *bad* events and overweight low-probability *good* events”.
3. Valuation Errors: Difficulty of accurate monetary estimates of the social value.
4. Estimation/ Measurement Errors: Impact are often observed, recorded or interpreted inaccurately.



# Choosing among Projects (in Chapter 2)

Net Present Value  $NPV = \sum_{t=0}^{t=n} \frac{B_t - C_t}{(1+i)^t} = \sum_{t=0}^{t=n} \frac{B_t}{(1+i)^t} - \sum_{t=0}^{t=n} \frac{C_t}{(1+i)^t} = PVB - PVC$

Cost Benefit Ratio  $CBR = \sum_{t=0}^{t=n} \frac{B_t}{(1+i)^t} / \sum_{t=0}^{t=n} \frac{C_t}{(1+i)^t} = PVB / PVC$

	<i>Costs (millions of dollars)</i>	<i>Benefits (millions of dollars)</i>	<i>Net Benefits (millions of dollars)</i>	<i>Benefits/Costs</i>
No project	0	0	0	–
Project A	1	10	9	10
Project B	10	30	20	3
Project C	4	8	4	2
Project D	3	5	2	1.7
Projects C and D	7	21	14	3
Project E	10	8	–2	0.8

(1) No constraints: Choose A, B, and combination C and D (net benefits equal \$43 million).

(2) All projects mutually exclusive: Choose B (net benefits equal \$20 million).

(3) Total costs cannot exceed \$10 million: Choose A and combination C and D (net benefits equal \$23 million).