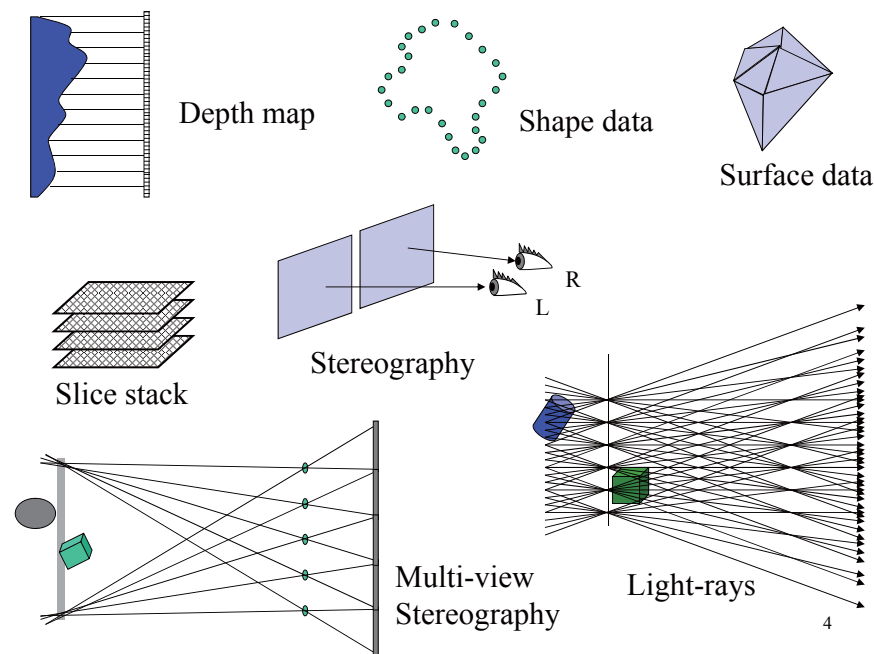


Optical imaging and image processing (XI)

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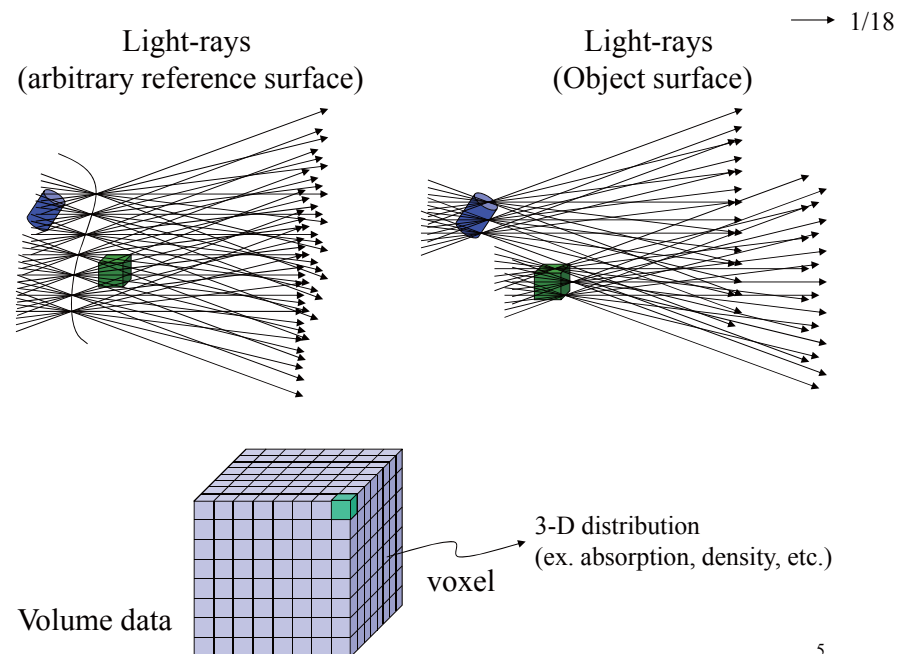
7. 三次元画像とホログラフィー

7. Three-dimensional imaging and holography

7.1 Variations of 3-D information

Type	Parameters	Amount of data
2D image	x, y, value	$N^2 \times L_b$
Depth map	x, y, depth	$N^2 \times L_d$
Shape data	x, y, z	$3P \times X$
Surface data	$x, y, z, \text{reflectivity}$ x, y, z, color	$3P \times L_b \times X$
Slice stack	$x, y, \text{value}, \text{number}$	$N^2 \times L_b \times D$
Stereography	$x, y, \text{value}, \text{angle}$	$N^2 \times L_b \times M$
Volume data	x, y, z, value	$N^3 \times L_b$
Light-field	$x, y, \text{value}, \text{angle}_x, \text{angle}_y$	$N^2 \times L_b \times M^2$
Time-sequence	x, y, value, t	$N^2 \times T$

三次元画像工学、大越孝敬、朝倉書店 (1997)



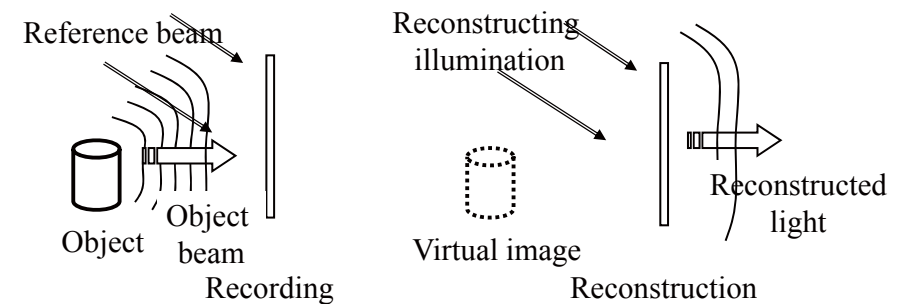
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7.2 3D display techniques

	Principle	Method	Depth-cues (Only important cues shown)
No parallax Single 2D image	Monocular depth-cue	Pictorial techniques	Overlapping, Linear Perspective Texture Gradient, Shades and Shadows, Aerial Perspective
		Large field of view Floating real-image	Display surface becomes unstable
No parallax Multiple 2D images		Motion picture Observer Tracking	Motion Parallax
Binocular stereogram Two 2-D images	Binocular parallax	Polarizing glasses, Anaglyph, Time-sequential, Goggle, Lenticular stereogram (binocular)	Binocular Parallax
Autostereoscopic 3D display (3D images)	Multi-view	Parallax panoramagram Lenticular sheet IP, Integral imaging	Binocular Parallax, Motion Parallax
	Depth sampling	Varifocal mirror LCD Stack	Binocular Parallax, Motion Parallax Accommodation, Convergence Difficult to reproduce overlapping effect
	light-ray or wavefront reconstruction	IP, Parallax barrier, High-density light-ray reproduction Holography	Binocular Parallax, Motion Parallax Accommodation, Convergence

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Hologram



- Reconstructing wavefront of light wave

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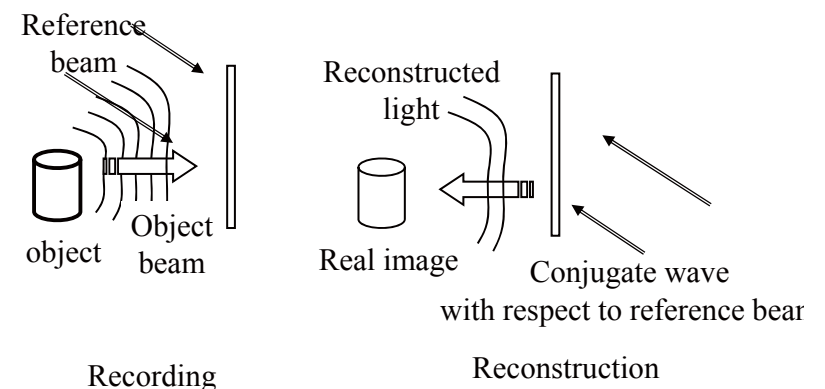
7.3 Holography

Wavefront recording and reconstruction using the light interference and diffraction

- Recording and reconstruction of wavefront
 - Recording and display of 3D image
 - Optical measurement
- Modification of the light propagation or the beam shape
 - Diffractive optical element, Holographic optical element
 - Optical information processing
- Light dispersion, wavelength selectivity
 - Optical element, diffraction grating, filter
 - 3D display with white light reconstruction
- High-density information recording, redundancy
 - Optical memory
- Combination of above features
 - Security printing (anti-counterfeit printing)

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Reconstruction of real image



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Recording of hologram

- Interference of two wavefronts

$$I(\mathbf{r}) = \langle |U_{Sc}(\mathbf{r}, t) + U_{Rc}(\mathbf{r}, t)|^2 \rangle$$

- Complex amplitude

- Object wave $U_S(\mathbf{r}) = A(\mathbf{r}) \exp \{j \phi(\mathbf{r})\}$
- Reference wave $U_R(\mathbf{r}) = B \exp \{j k x \sin \theta\}$

- For coherent light

$$\begin{aligned} I(\mathbf{r}) &= |U_S(\mathbf{r}) + U_R(\mathbf{r})|^2 \\ &= |U_S(\mathbf{r})|^2 + |U_R(\mathbf{r})|^2 + U_S(\mathbf{r}) U_R(\mathbf{r})^* + U_S(\mathbf{r})^* U_R(\mathbf{r}) \\ &= A(\mathbf{r})^2 + B^2 + A(\mathbf{r}) B \exp \{j(\phi(\mathbf{r}) - kx \sin \theta)\} \\ &\quad + A(\mathbf{r}) B \exp \{-j(\phi(\mathbf{r}) - kx \sin \theta)\} \end{aligned}$$

- Amplitude transmittance of recording medium

- When it is linear to exposed light energy

$$T_A = T_0 + t_1 I(\mathbf{r})$$

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Applications of holography

- 3D display
 - Publishing, Security, Package, Interior, Advertisement, Education
 - Printing of 3D image data, Medical 3D displays
- Security Printing
 - Banknote (10k, 5k bills), Credit card, Package of digital media
- Optical measurement
 - Holographic interferometer
 - Shape, Motion, Vibration, Refractive index, birefringence
 - Digital holography (using CCD cameras instead of photographic recording media)
- Optical information processing, Optical memory
 - Holographic matched filter, Holographic memory
- Holographic Optical Element (HOE)
 - Lens, Mirror, Diffuser, HUD, Projector, LCD
 - Screen, Dispersion element, Optical interconnection
 - Optical pickup, Scanner, Bar-code reader, Laser-beam printer, Beam shaping
- Imaging (Microscopy)
 - Electron holography, X-ray holography

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Reconstruction of hologram

$$\begin{aligned} \text{Reconstructing wave } U(\mathbf{r}) &= U_R(\mathbf{r}) T_A \\ &= t_1 U_R(\mathbf{r}) T_0 + t_1 U_R(\mathbf{r}) \{|U_S(\mathbf{r})|^2 + |U_R(\mathbf{r})|^2\} \\ &\quad + t_1 U_S(\mathbf{r}) |U_R(\mathbf{r})|^2 + t_1 U_S(\mathbf{r})^* U_R(\mathbf{r})^2 \\ &= U_0'(\mathbf{r}) + U_D'(\mathbf{r}) + U_C'(\mathbf{r}) \end{aligned}$$

$$U_D'(\mathbf{r}) = t_1 U_S(\mathbf{r}) |U_R(\mathbf{r})|^2 = t_1 B^2 U_S(\mathbf{r})$$

→ Object wave is reconstructed (Virtual image)

- Conjugate image reconstruction

$$\begin{aligned} U(\mathbf{r}) &= U_R(\mathbf{r})^* T_A \\ &= U_0''(\mathbf{r}) + U_C''(\mathbf{r}) + U_D''(\mathbf{r}) \end{aligned}$$

$$\begin{aligned} U_D''(\mathbf{r}) &= t_1 U_S(\mathbf{r})^* |U_R(\mathbf{r})|^2 \\ &= t_1 B^2 U_S(\mathbf{r})^* = t_1 B^2 A(\mathbf{r}) \exp \{-j \phi(\mathbf{r})\} \quad (188) \end{aligned}$$

→ Conjugate wave is reconstructed (Real image)

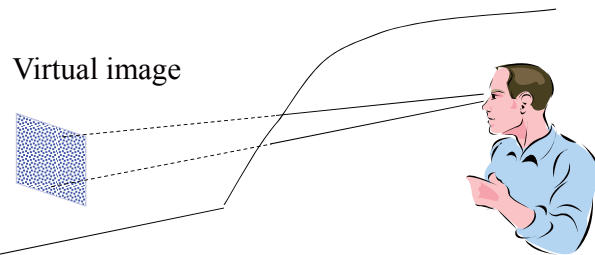
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Display holograms

- Laser reconstruction
 - Fresnel hologram
- White-light reconstruction
 - Image-type,
 - Rainbow hologram (1-step, 2-step),
 - Volume reflection hologram (Denisyuk hologram, Lippmann hologram)
- Holographic stereogram
- Computer generated hologram
- Color holograms
 - Laser light reconstruction (RGB lasers)
 - White-light reconstruction
 - Rainbow-type, Volume-reflection type
 - Color holographic stereogram
 - Rainbow-type, Volume-reflection type

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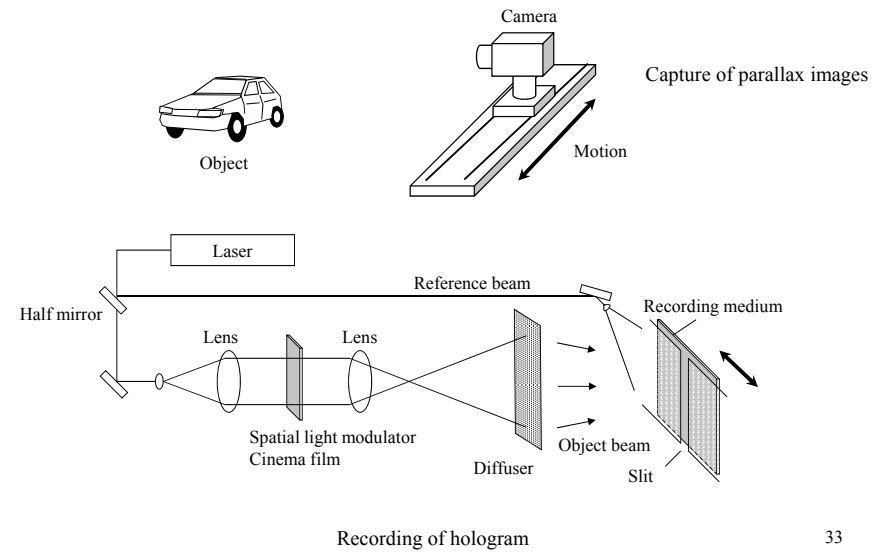
HUD(Head-up display)



- Features
 - Virtual image formation
 - Only the light of specific wavelength is reflected, others are transmitted. (High-transmittance)
 - Thin device (Sandwich between glasses)
- Substitution of concave half-mirror, Fresnel lens, and Dichroic mirror

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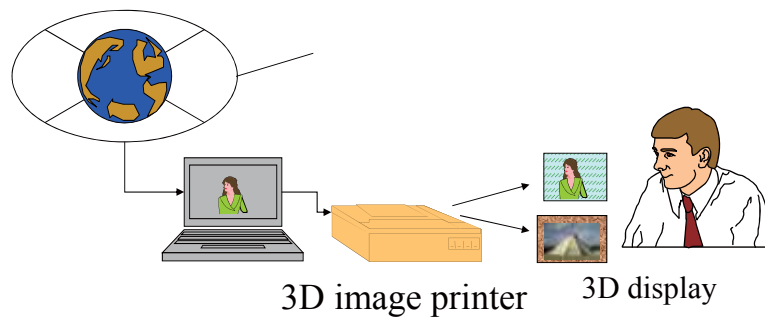
Recording of holographic stereogram Horizontal parallax only (HPO)



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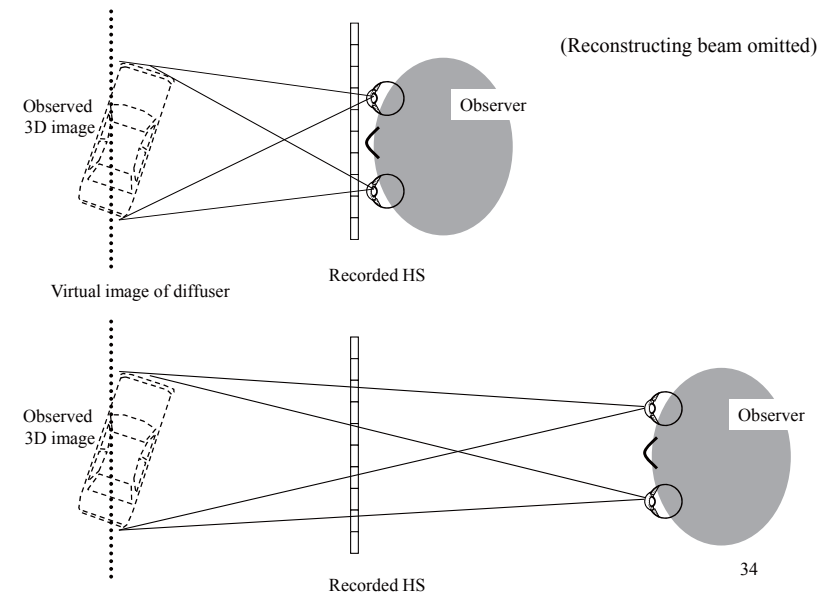
Holographic printer

- Holographic stereogram
- Computer Generated Hologram (HOE)



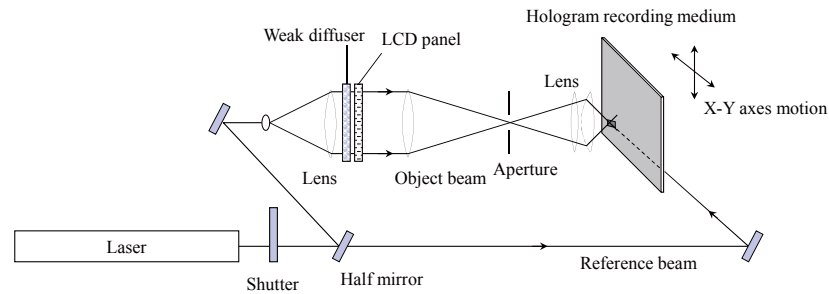
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Observation of holographic stereogram



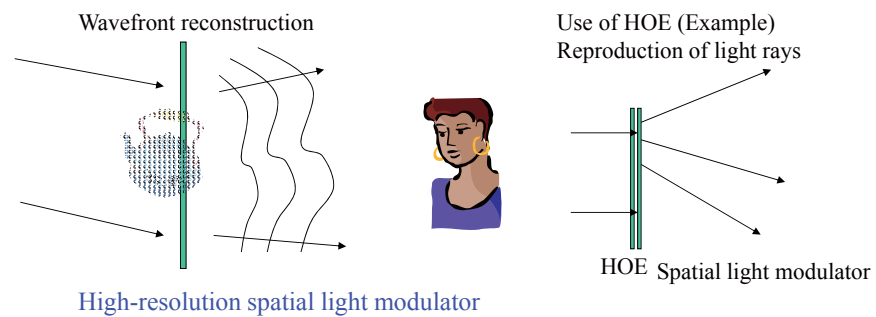
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Recording of full-parallax holographic stereogram



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Electro-holography, Holographic TV



- 3D electronic display using holography
- Wavefront reconstruction (CGH)
- Use of holographic stereogram technique
- Use of holographic optical element
- High-resolution image with the large range of depth

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