## Structural Analysis II 構造力学第二 (3)

# Kazuhiko Kawashima Department of Civil Engineering Tokyo institute of Technology 東京工業大学大学院理工学研究科土木工学専攻 川島一彦

### 9.6 STATIC VERSUS KINEMATIC INDETERMINACY

1) Which is better between static and kinematic determinacy?

•The above example problem had only one static redundancy,  $R_{by}$ , and only one kinematic redundancy,  $\theta_b$ . So whether the static indeterminacy or kinematic determinacy is better does not matter.

 However, as the structure becomes more complex, static vs. kinematic indeterminacy becomes important









3) Important observation for static versus kinematic indeterminacy

 In establishing the statically determinate primary structure, there are a number of alternative selection patters for redundant force quantities.

 However, in developing the kinematically determinate primary structure, no selection process is necessary. Instead, all of the displacement quantities that are necessary to describe the structure's response automatically become redundant quantities.

# 9.7 COMPATIBILITY METHOD OF ANALYSIS (**変位適合解析法**)

1) What is the compatibility method?

•The compatibility method is based on the solution of a set of equations that express compatibility relationship throughout the structure.

•The compatibility method is also referred as the force method (荷重法) or the flexibility method (フレキシビリティー法), since the unknowns in the governing equations are forces and the coefficients of those unknowns are flexibility (displacement quantities)(たわみ性、 フレキシビリティー).

# 2) Flexibility and Stiffness(フレキシビリティーと 剛性)

F=ku

where,

where,

F: force (力) u: displacement (変位) K: stiffness (剛性)

u=fF

(A2)

(A1)

Compatibility method, or Force method, or Flexibility method

Equilibrium

method, or

method, or

stiffness

method

displacement

F: force (力)methou: displacement (変位)f: flexibility (たわみ性、フレキシビリティー)

#### 3) Example of the compatibility method



 As we studied in 9.3, we have the compatibility condition for a statically determinate structure as

$$\Delta_b = \Delta_{b1} + \Delta_{b2}$$



Fig. 9.4 Primary structure of Fig. 9.3



4) Are requirements of equilibrium approved in the compatibility method?

•The final solution must satisfy both the conditions of compatibility and the requirements of equilibrium.

•When the method is properly formulated, the compatibility equations represent a superposition of a set of partial solutions, each of which satisfies the requirements of equilibrium.

## 9.8 EQUILIBRIUM METHOD OF ANALYSIS (荷重つり合い法)

## 1) What is the equilibrium method?

•The equilibrium method is based on the solution of a set of equations that express the equilibrium requirements for the structure.

●The equilibrium method is also called the displacement method (変位法) or the stiffness method (剛性法).



## 3) Advantage of equilibrium method

•For larger structures, there are many redundant displacement quantities. There is one redundant displacement quantity corresponding to each kinematic degree of freedom.

 Therefore, a number of equilibrium equations must be solved simultaneously for the displacement quantities.

•However unlike the compatibility method, there is no selectivity in choosing the redundants. All the kinematic degree of freedom are taken as redundant displacements.

•This is a major advantage for the automation that is needed in computer programming.

9.9 BEHAVIORAL CHARACTERISTICS OF STATICALLY INDETERMINATE STRUCTURES

1) Why are statically indeterminate structures used?

(1) A statically indeterminate structure displays greater stiffness in resisting load than does a comparable statically determinate structure.



(2) A statically indeterminate structure has lower stress intensities than would a comparative statically determinate structure.



(3) A statically indeterminate structure is safer than would a comparative statically determinate structure.

•There are either internal force or external reactions that are not needed for stability in a statically indeterminate structure.

 No matter how these force components are removed, the structure will not become unstable.



# 3) What is disadvantage of a statically indeterminate structure?

 Continuity which is the advantage of a statically indeterminate structure can be the primary disadvantage.

• If point b of a three-span continuous beam settled as shown in Fig. 9.12 (b), bending moment as shown in Fig. 9.12 (c) would be developed. Thus, without any loading on the structure, sizable moments would be introduced at the interior support points.



Fig. 9.12

 In situations where such settlements can occur, a statically determinate structure should be employed as shown in Fig. 9.13.

