

**Introduction to Cost-Benefit Analysis,**  
**(Chap.1)**  
**and**  
**Conceptual Foundations of CBA**  
**(Chap.2)**

# **Major Steps in CBA**

## **- Exact Example of Highway in Canada -**

1. Specify the set of alternative projects
2. Decide whose benefits and costs count
3. Catalogue the impacts and select measurement indicators
4. Predicts the impacts quantitatively over the life of the projects
5. Monetize all impacts
6. Discount benefits and costs to obtain present values
7. Compute the net present value of each alternative
8. Perform sensitivity analysis
9. Make a recommendation

**TABLE 1-3** Coquihalla Highway CBA (1986 \$ Million)

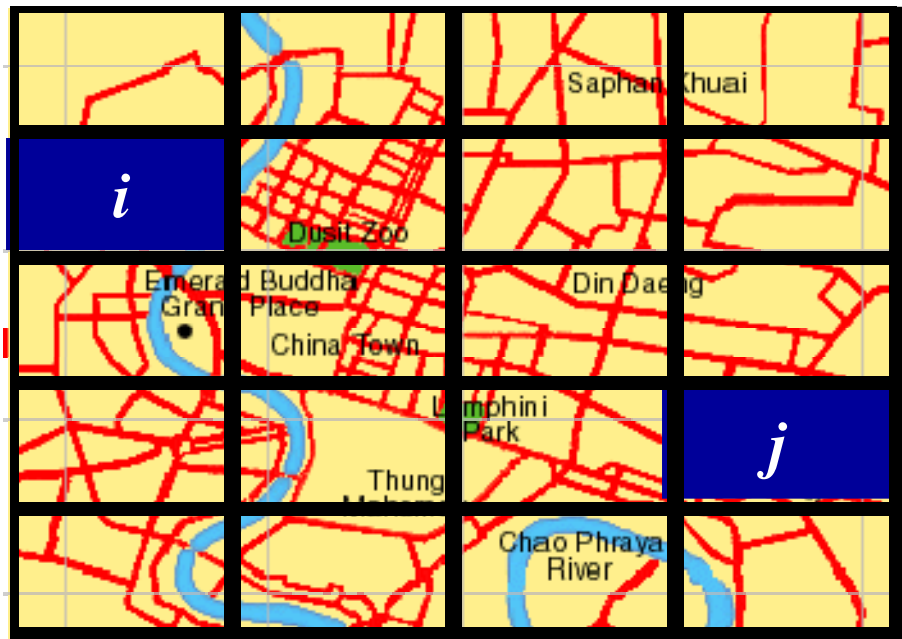
	<i>No Tolls</i>		<i>With Tolls</i>	
	<i>A Global Perspective</i>	<i>B Provincial Perspective</i>	<i>C Global Perspective</i>	<i>D Provincial Perspective</i>
Project Benefits:				
Time and Operating Cost Savings	389.8	292.3	290.4	217.8
Horizon Value of Highway	53.3	53.3	53.3	53.3
Safety Benefits (Lives)	36.0	27.0	25.2	18.9
Alternative Routes Benefits	14.6	10.9	9.4	7.1
Toll Revenues	—	—	—	37.4
New Users	0.8	0.6	0.3	0.2
Total Benefits	494.5	384.1	378.6	334.7
Project Costs:				
Construction	338.1	338.1	338.1	338.1
Maintenance	7.6	7.6	7.6	7.6
Toll Collection	—	—	8.4	8.4
Toll Booth Construction	—	—	0.3	0.3
Total Costs	345.7	345.7	354.4	354.4
Net Social Benefits	148.8	38.4	24.2	-19.7

# How to “monetize” impacts?

## Case of Transport Project

### Generalized Cost

is an amount of money representing the overall disutility (or inconvenience) of traveling between origin  $i$  and destination  $j$  by a particular mode.



**Zoning**

Origin  $i$

Destination  $j$

# Components of Generalized Cost

Public Transport

Fare, Giving up time, .....

Car

Giving up time,

Toll Charge,

VOC (Vehicle Operating Costs):

Fuel, Oil, Tire & Tube, Maintenance and Depreciation

Other components?

# Market in Transport Service

Price = Generalized Cost

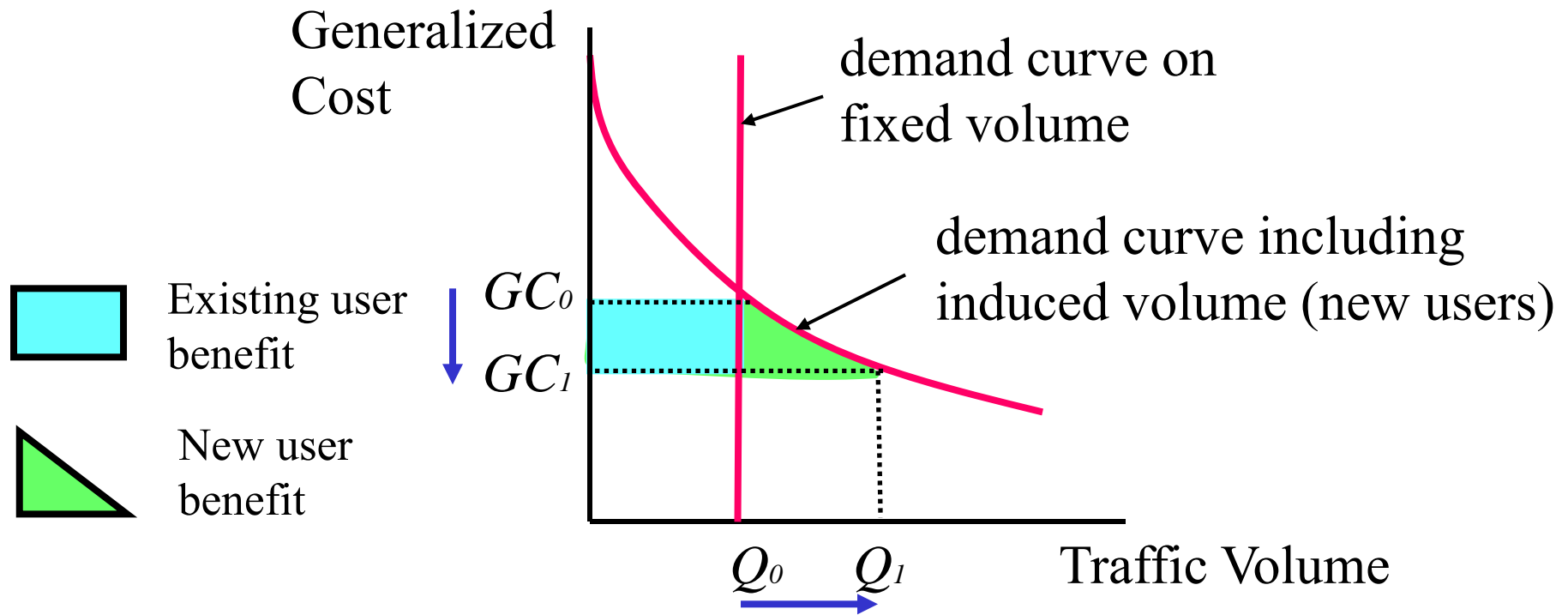
WTP is the maximum amount of money that a user would be willing to pay to make a trip. (can be interpreted as a maximum generalized cost that they are prepared to accept a trip)

**Definition of User Benefit**    Change in Consumer Surplus

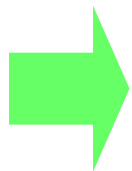
$$UB = CS_1 - CS_0$$

$CS_1$ : do-something = with-project

$CS_0$ : do-minimum = without-project



Improved transport condition by the transport project



Reduction of Generalized Cost e.g. time saving  
accidents reductions

***Rule of a Half***

$$UB = \int_{GC_1}^{GC_0} D(GC) dGC = \frac{1}{2}(GC_0 - GC_1)(Q_0 + Q_1)$$

# Generalized Cost Function

$$GC = \alpha T + \beta L$$

GC: generalized cost by day and by vehicle type [yen/ vehicle]

$\alpha$  : value of time by day and by vehicle type [yen/ vehicle\*minute]

$\beta$  : VOC by vehicle type [yen/ vehicle\*km]

T : average travel time by vehicle type [minute]

L : travel distance by vehicle type [km]

**User benefit (per day)** m: vehicle type. i,j: origin and destination.

$$\text{weekday } BU_n = \sum_{m,i,j} \frac{1}{2} (GC_0 - GC_1)(Q_0 + Q_1)$$

$$\text{holiday } BU_s = (h \text{ factor}) \cdot \sum_{m,i,j} \frac{1}{2} (GC_0 - GC_1)(Q_0 + Q_1)$$

$$\text{annual user benefit } BU_n \times 243 + BU_s \times 122$$



# Measurement of Value of Time

## 1) **Resource value**, based on Opportunity Cost

a) Average (expected) gross wage rate (per hour)

b) National annual income data (instead of gross wage rate)

ex.  $VOT = GDP / \text{number of employment} / \text{working time}$

## 2) **Behavioral value**, based on Generalized Cost Function

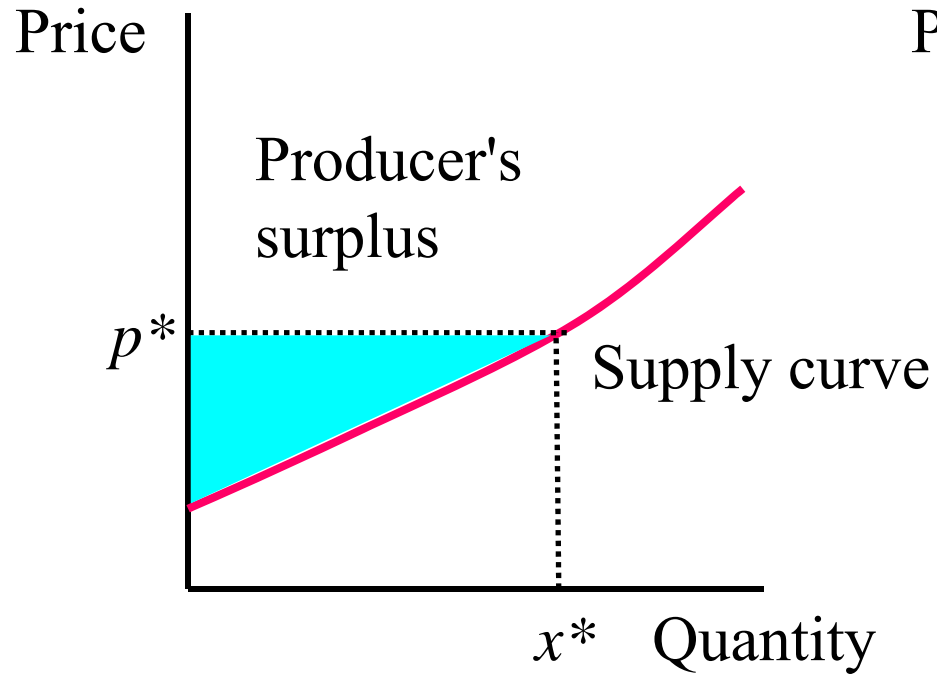
$$Utility = GC = -0.147TW - 0.0411TT - 2.24C$$

(estimated by mode choice model)

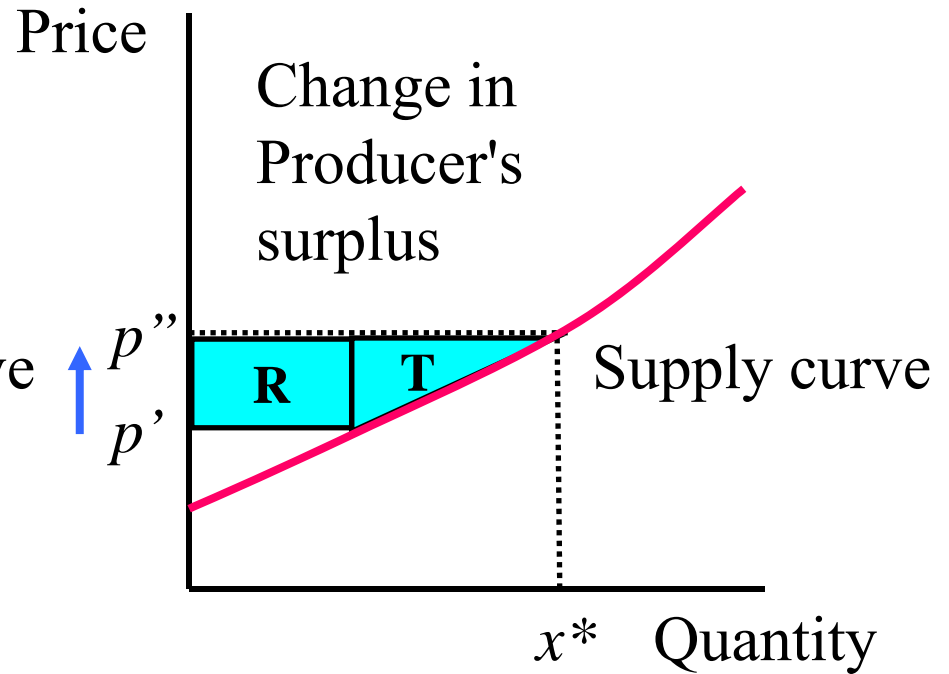
$$VOT = 0.0411 / 2.24$$

$$= 1.10 \text{ US\$ / hr / person}$$

# Producer's Surplus



Net producer's surplus



R: Gain (revenue) to sell the higher price

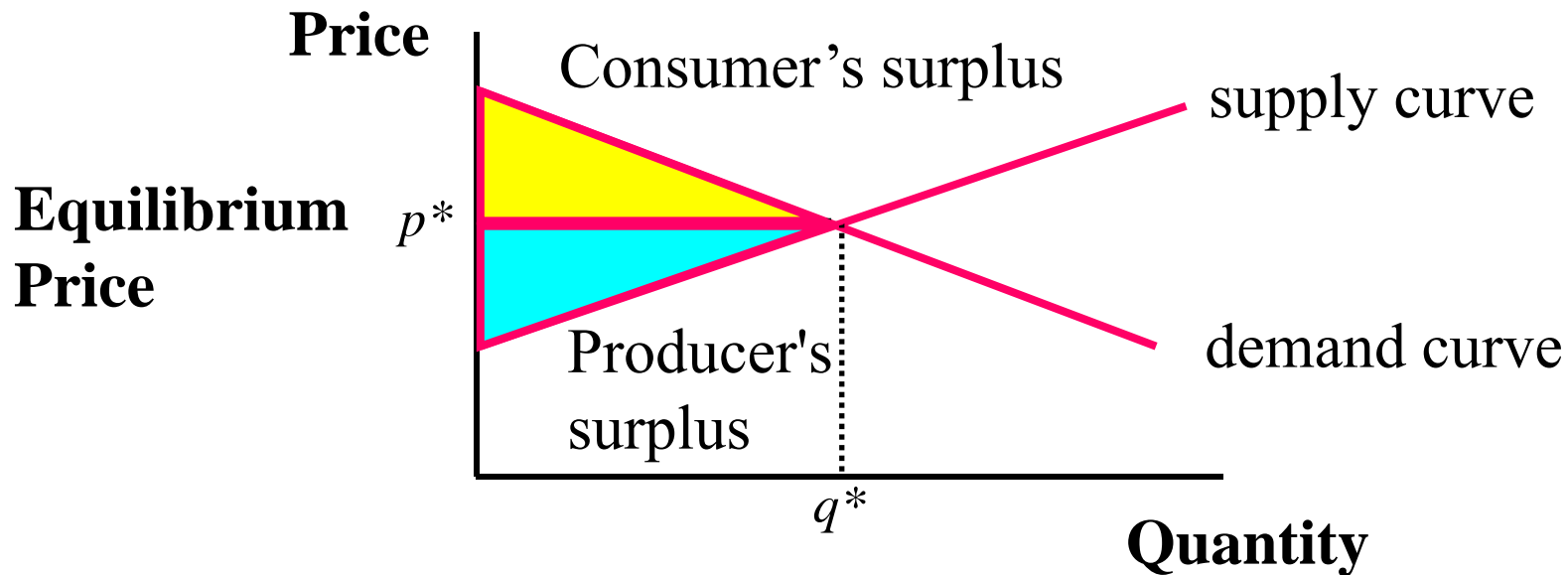
T: Gain (revenue) to sell more units

# Equilibrium and Social Surplus

## Competitive Market

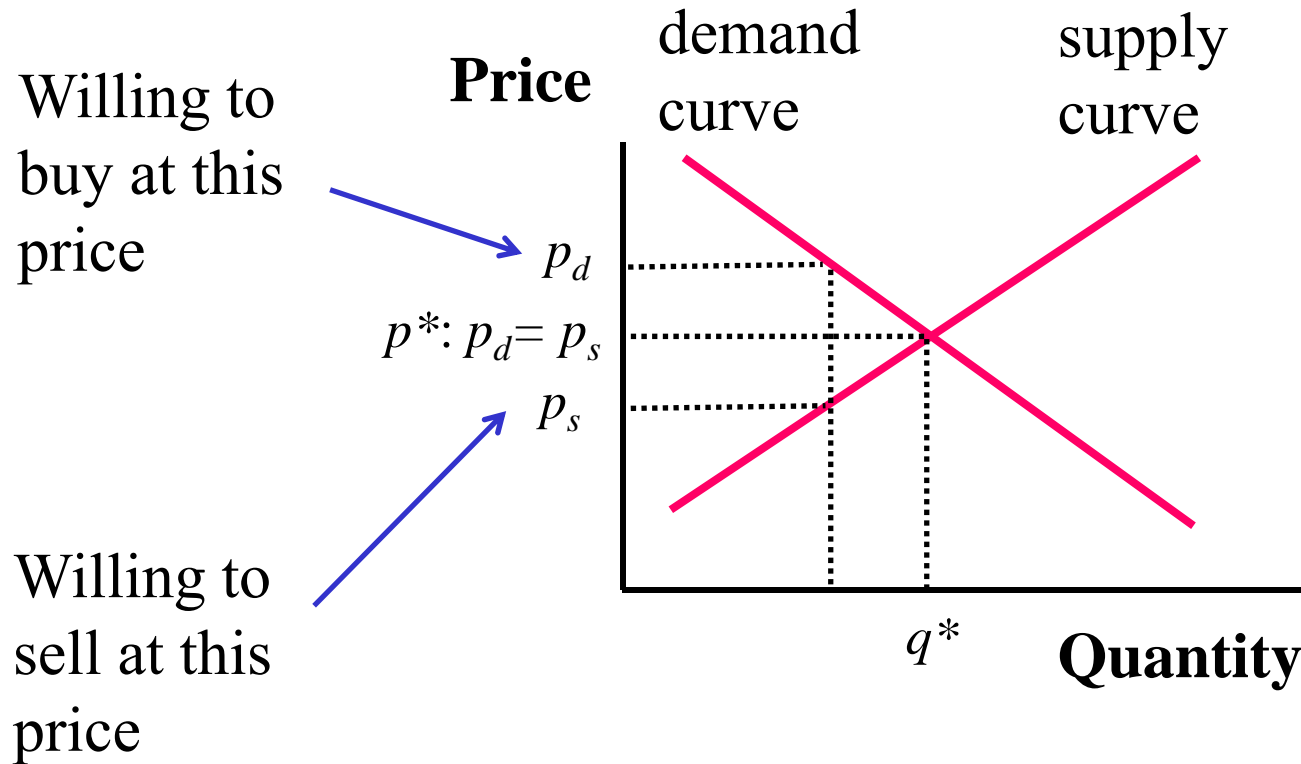
Consumers and Suppliers are *Price Takers*

Market price is independent of any agent's behavior



**Social surplus** = Consumer's surplus + Producer's surplus

# Pareto Efficiency (1)

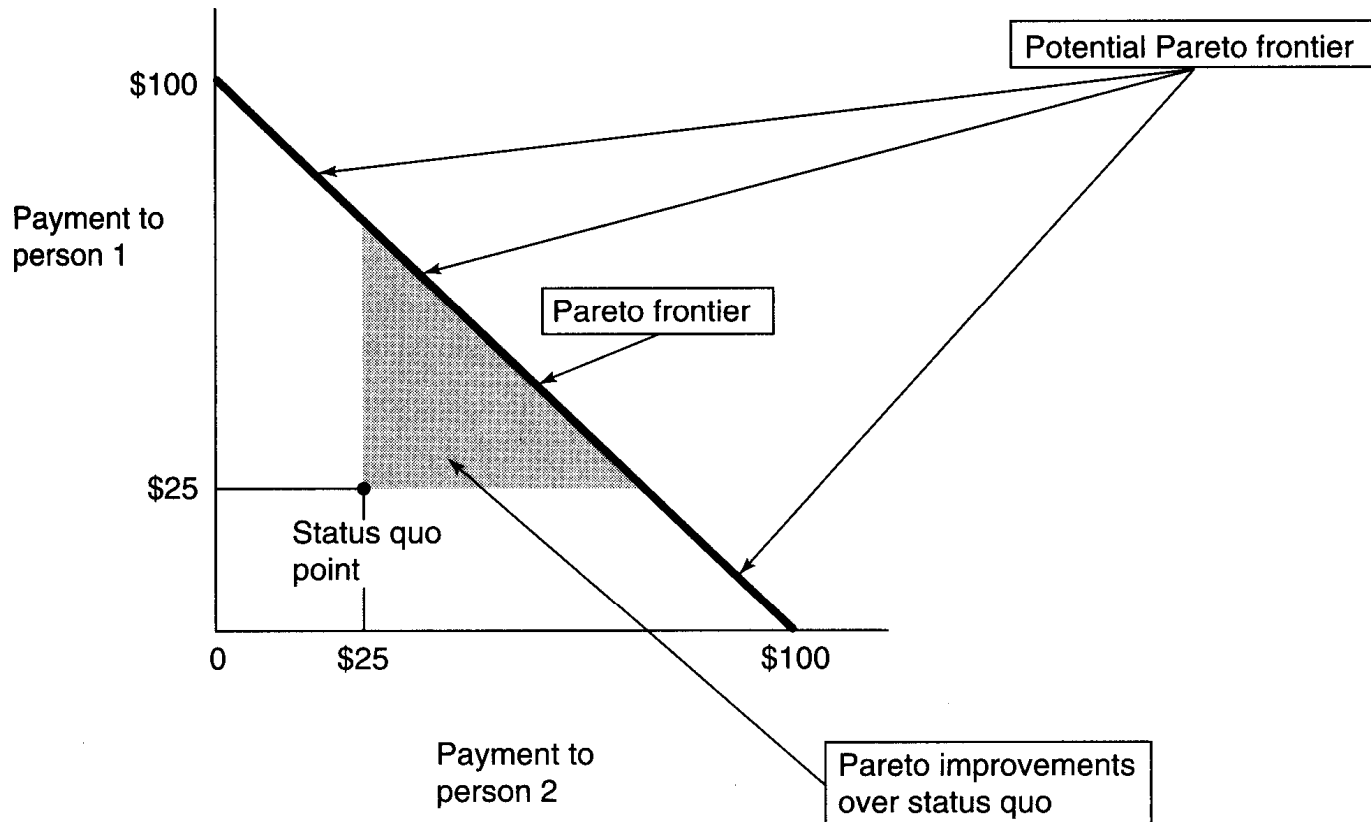


Competitive market produce **Pareto efficient**  
amount of output

# Pareto Efficiency (2)

## Pareto Efficiency

We cannot find a way to make some people better off without making anybody else worse off



# Net (Social) Benefits and Pareto Efficiency

If a policy (or project, measure) has positive net social benefits (= present social benefit – present social cost ), then it is possible to find a set of transfer that makes at least one person better off without making anyone else worse off.

## Willingness-to-Pay (WTP)

Person 1: \$100

Person 2: \$200

Person 3: - \$250 (Willingness-to-Accept, WTA)

Net Benefit +\$50

(Not Pareto Efficiency)



## Compensation

1 to 3: \$75

2 to 3: \$175

1: \$25 (=100-75)

2: \$25 (=200-175)

3: \$ 0 (=75+175-250)

# Potential Pareto Efficiency

## Kaldor-Hicks Criterion

Basis for the Potential Pareto Efficiency rule = Net Benefit Criterion  
Positive Net Benefit

A policy should be adopted if and only if those who will gain could fully compensate those who will lose and still be better off.

## Justification of Potential Pareto Efficiency

- Society maximizes aggregate wealth
- Different policies will have different sets of winners and losers
- Contrast to the incentives in representative political systems
- Equity of wealth or income will be addressed after adopting efficient policies

# Pareto Efficiency and Equity

Criterion for comparing the outcomes of different situation

## Definition

If there is no way to make any person better off without hurting anybody else.

Social net benefit express efficiency, but do not consider equity.

