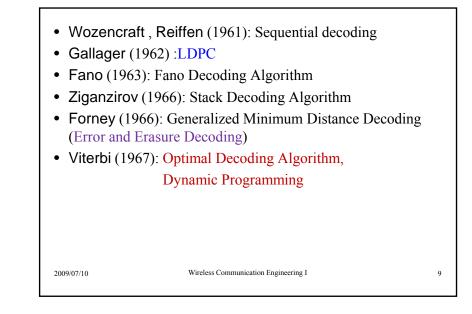


Elias (195)Reed ,Sol	54): Combinatorial Function & ECC 4): Convolutional Code omon (1960): RS Code (Maximal	
Separable		
	hem (1959) ,Bose,Chaudhuri (1960): (Multiple Error Correction)	
 Peterson 	(1960): Error Location Polynomial	
2009/07/10	Wireless Communication Engineering I	



- Berlekamp (1968): Fast Iterative BCH Decoding
- Forney (1966): Concatinated Code
- Goppa (1970): Rational Function Code
- Justeson (1972): Asymptotically Good Code
- Ungerboeck,Csajka (1976): Trellis Code Modulation,
- Goppa (1980): Algebraic-Geometry Code

Welch, Berlekamp (1983): Remainder Decoding Algorithm
Araki, Sorger and Kotter (1993): Fast GMD Decoding Algorithm
Berrou (1993): Turbo Code(Parallel concatinated convolutional code)

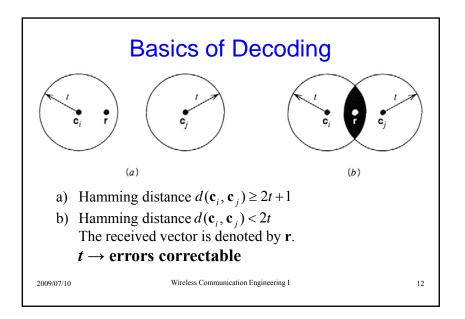
2009/07/10

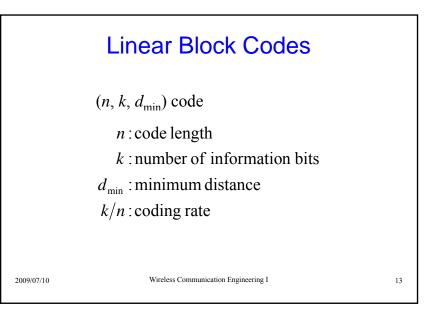
Wireless Communication Engineering

10

2009/07/10

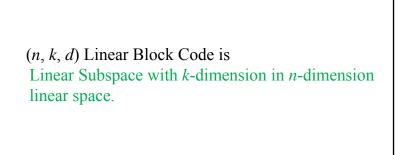
Wireless Communication Engineering I





For large *d* ,Good Error correction capability R=k/n (Low coding rate)

Trade-off between error correction and coding rate



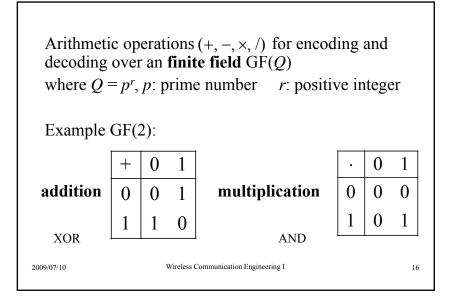
2009/07/10

Wireless Communication Engineering I

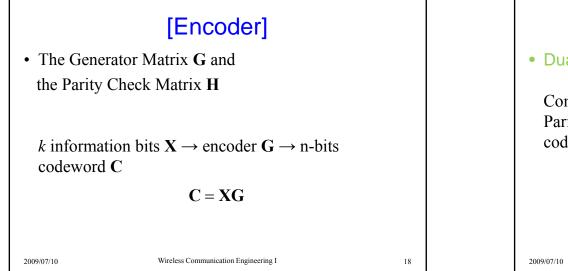
14

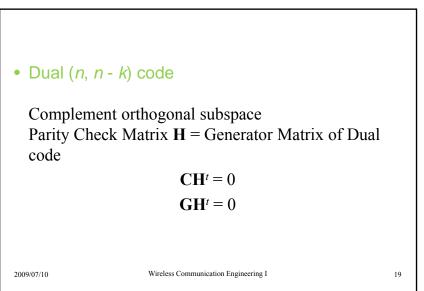
2009/07/10

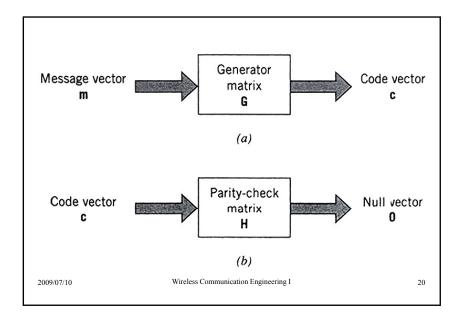
Wireless Communication Engineering I

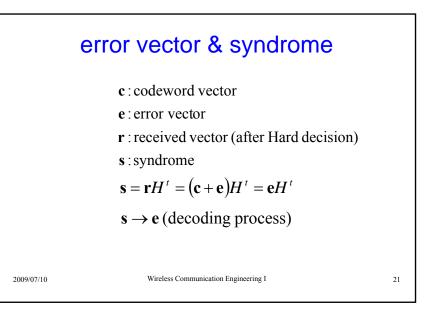


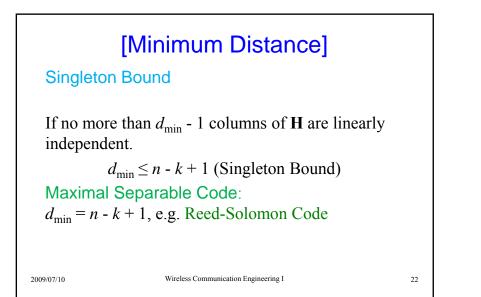
Analog and Digital Arithmetic Operation Analog: Real Number Field [R], Complex Number Field [C] Digital: Finite Field [GF(Q)]

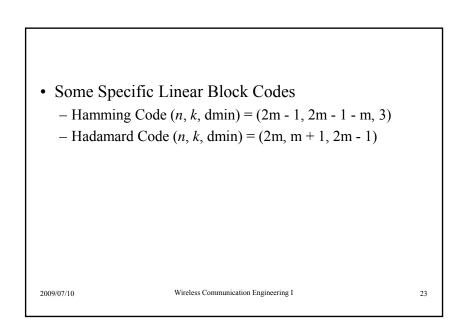


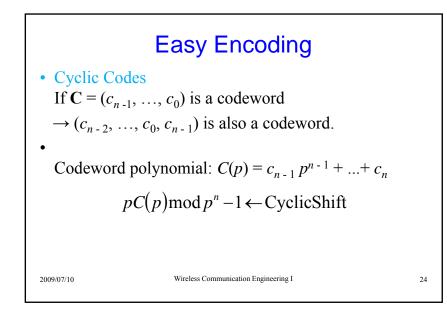


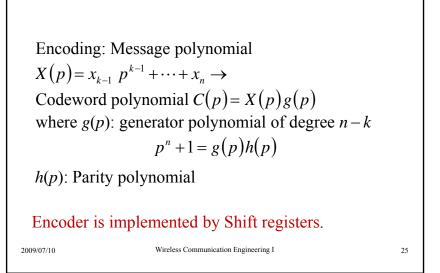


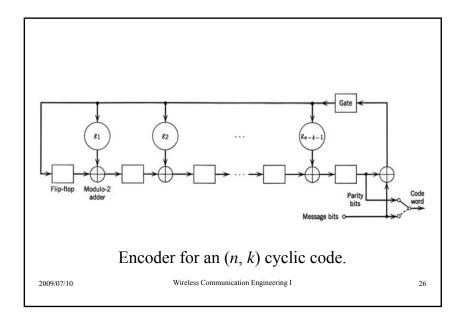


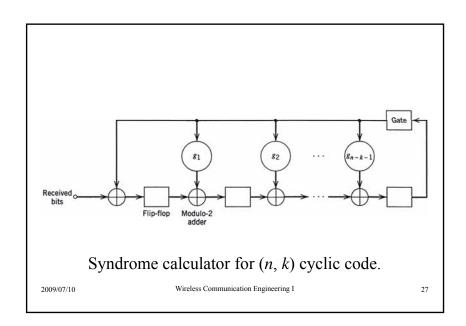


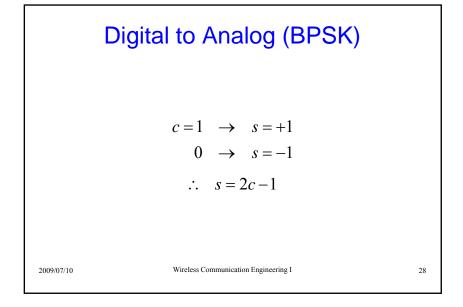












Soft-Decoding & Maximum Likelihood $\begin{aligned} \mathbf{r} &= \mathbf{s}^{(k)} + \mathbf{n} \\ &= (r_1, \dots, r_n) \\ &= (s_1, \dots, s_n) + (n_1, \dots, n_n) \end{aligned}$ $\operatorname{Prob} \left[\mathbf{r} | \mathbf{s}^{(k)} \right] : \operatorname{Likelihood} \end{aligned}$ $\operatorname{Max} \operatorname{Prob} \left[\mathbf{r} | \mathbf{s}^{(k)} \right] \rightarrow \operatorname{Min}_k (\mathbf{r} - \mathbf{s}^{(k)})^2$ $\rightarrow \operatorname{Max} : \operatorname{Correlation} \left[\mathbf{r}, \mathbf{c}^{(k)} \right] \end{aligned}$ 2090710 Wirdes Communication Engineering 1 200000

• Optimum Soft-Decision Decoding of Linear Block Codes Optimum receiver has $M = 2^k$ Matched Filter \rightarrow

Optimum receiver has $M = 2^k$ Matched Filter \rightarrow M correlation metrics

$$C(\mathbf{r},\mathbf{C}_i) = \sum_{j=1}^n (2c_{ij}-1)r_j$$

where C_i : *i* - th codeword

 c_{ii} : *j* - th position bit of the *i* - th codeword

 r_i : *j* - th received signal

 \rightarrow Largest matched filter output is selected.

2009/07/10

Wireless Communication Engineering I

30

Error probability for soft-decision decoding (Coherent PSK)

$$P_M < \exp\left(-\gamma_b R_c d_{\min} + k \ln 2\right)$$

where γ_b : SNR per bit

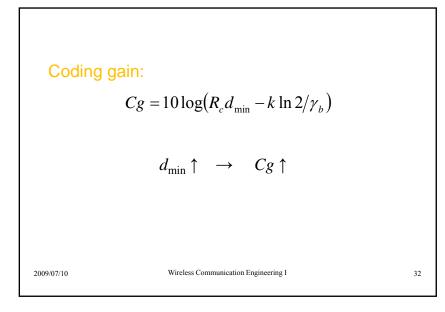
 R_c : Coding rate (= k/n)

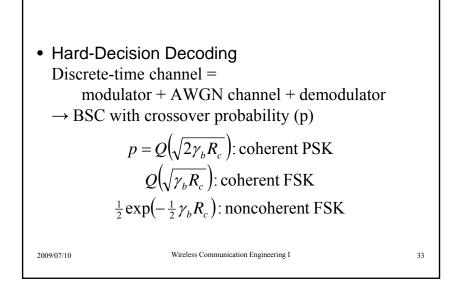
Uncoded binary PSK

$$P_e < \frac{1}{2} \exp(-\gamma_b)$$

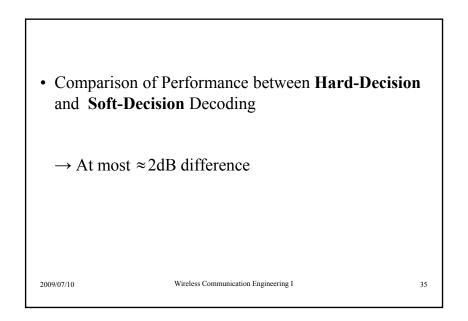
Wireless Communication Engineering I

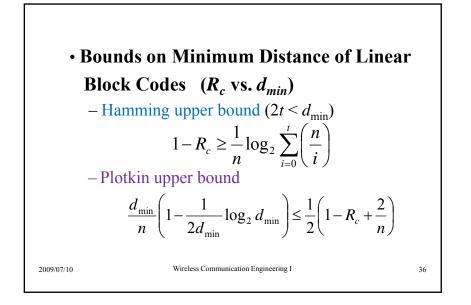
2009/07/10

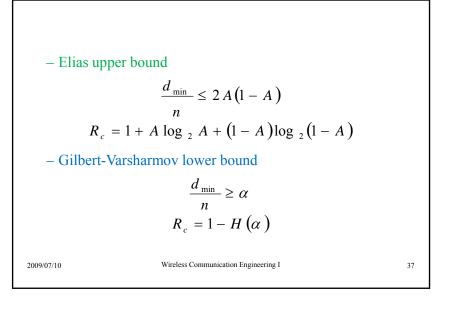


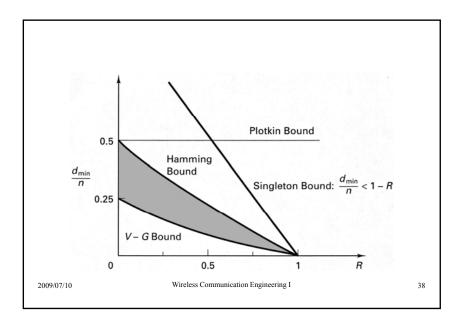


Maximum-Likelihood Decoding \rightarrow Minimum Distance Decoding Syndrome Calculation by Parity check matrix **H** $\mathbf{S} = \mathbf{Y}\mathbf{H}^{t}$ $= (\mathbf{C}_{m} + \mathbf{e}) \mathbf{H}^{t}$ $= \mathbf{e}\mathbf{H}^{t}$ where \mathbf{C}_{m} : transmitted codeword Y: received codeword at the demodulator \mathbf{e} : binary error vector









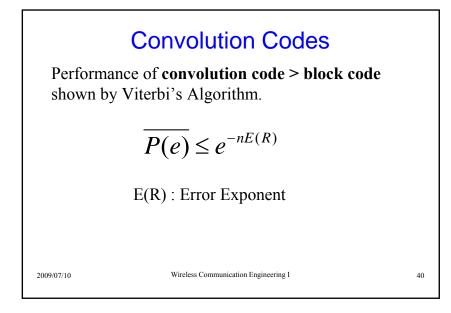
 Interleaving of Coded Data for Channels with Burst Errors
 Multipath and fading channel → burst error
 Burst error correction code: Fire code
 Correctable burst length b

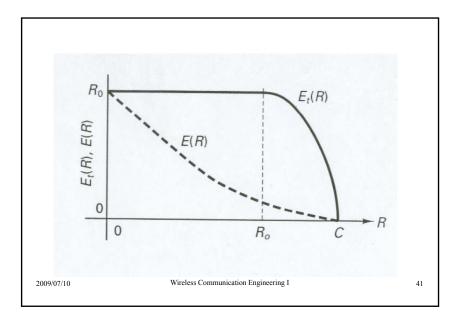
$$b \le \left\lfloor \frac{1}{2} \left(n - k \right) \right\rfloor$$

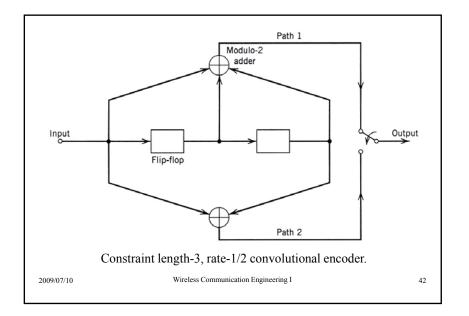
Block and Convolution interleave is effective for burst error.

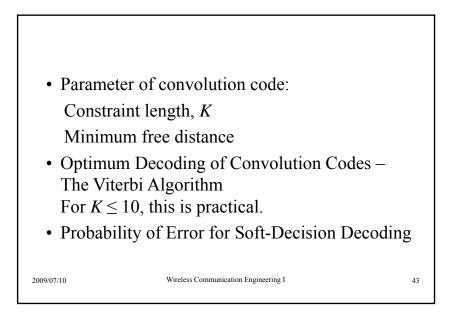
Wireless Communication Engineering I

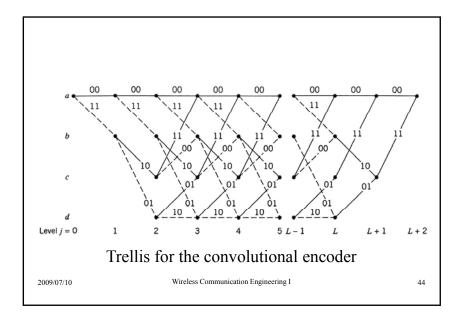
2009/07/10





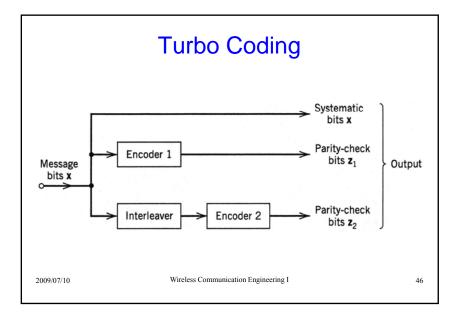


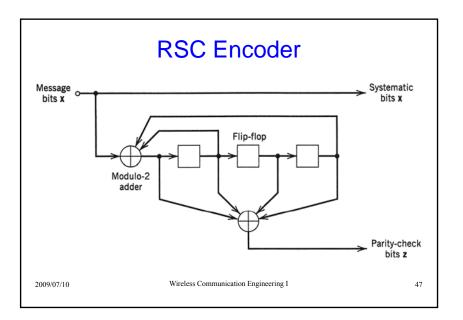


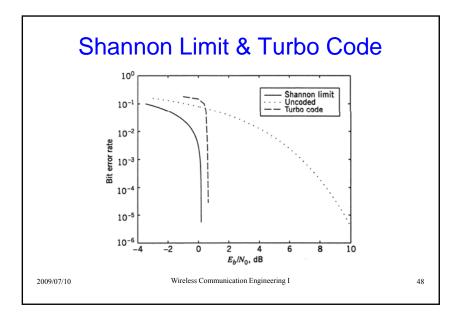


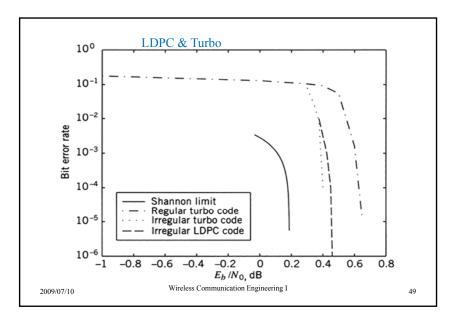
$$P_{e} \leq \sum_{d=d_{\text{free}}}^{\infty} a_{d} Q\left(\sqrt{2\gamma_{b}R_{c}d}\right)$$

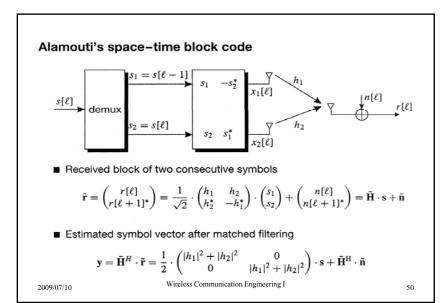
where a_{d} : the number of paths of distance d
• Probability of Error for Hard-Decision Decoding
Hamming distance is a metric for hard-decision

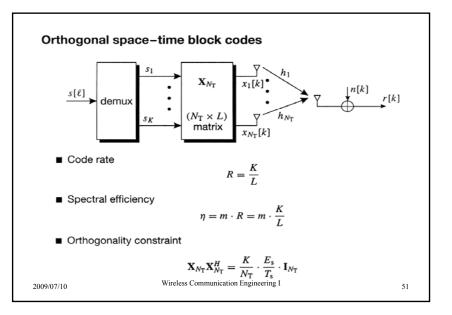


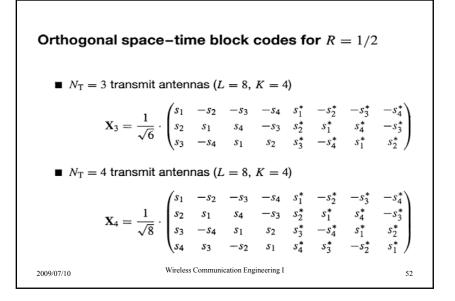


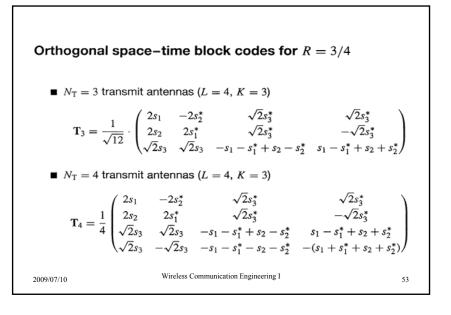


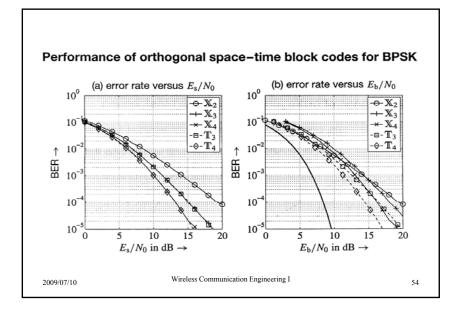


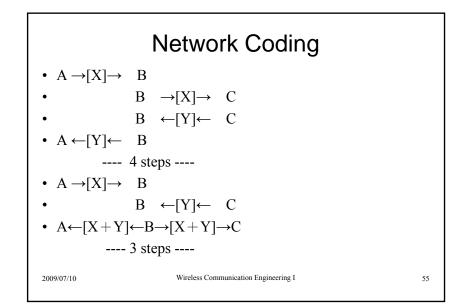


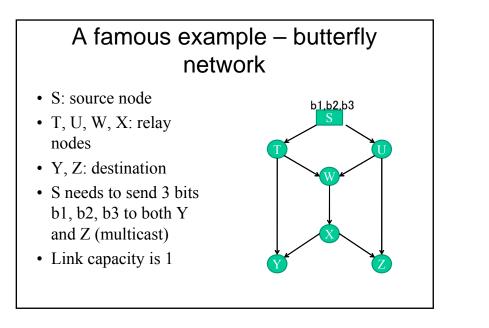






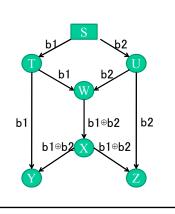


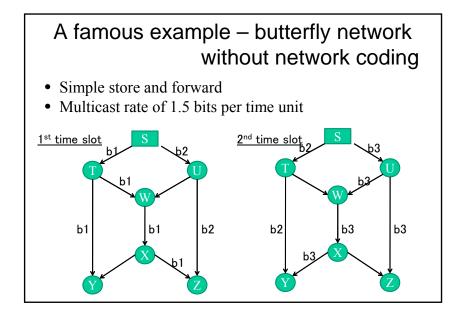


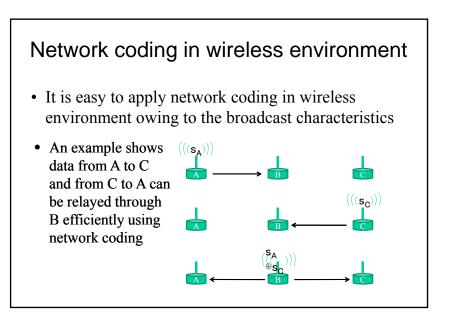


A famous example – butterfly network with network coding

- W receives b1 and b2, then performs exclusive OR (XOR) on received bits and forward to X
- Y receives b1 and b1⊕b2, then extracts b2 as b2 = b1⊕(b1⊕b2)
- Z receives b2 and b1⊕b2 then extracts b1 as b1 = b2⊕(b1⊕b2)
- Achieve multicast rate of 2 bits per time unit

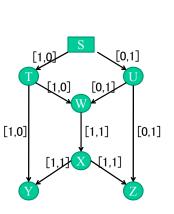






Network coding header

- In network coding, since information is processed inside the network, network coding header is required for network decoding at the destination
- Network coding header describes how a packet is processed
- The right figure shows network coding header of the butterfly network example
- If packet length is long enough, we can neglect the inefficiency of header





Multiple Access Techniques

1. A common communication channel is shared by many users.

up-link in a satellite communication, a set of terminals \rightarrow

a central computer, a mobile cellular system

- 2. A broadcast network down-links in a satellite system, radio and TV broadcast systems
- 3. Store-and-forward networks
- 4. Two-way communication systems

2009/07/10

Wireless Communication Engineering

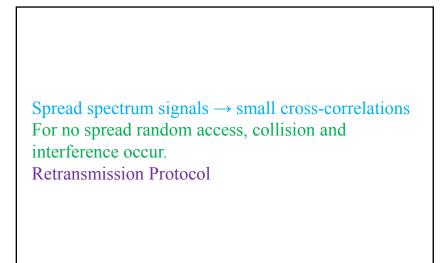
62

-FDMA (Frequency-division Multiple Access)
-TDMA (Time-division Multiple Access)
-CDMA (Code-division Multiple Access): for burst and low-duty-cycle information

transmission

2009/07/10

Wireless Communication Engineering I



2009/07/10

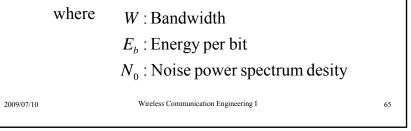
Wireless Communication Engineering

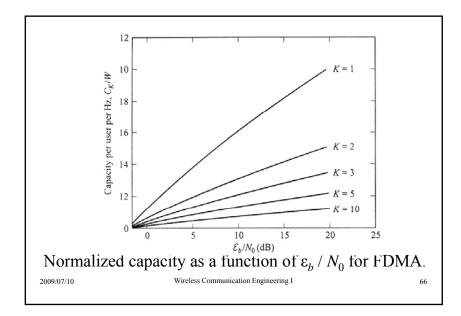
64

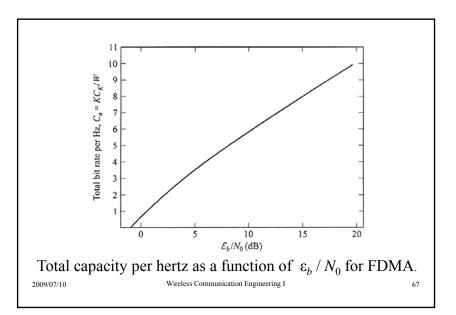
Capacity of Multiple Access Methods

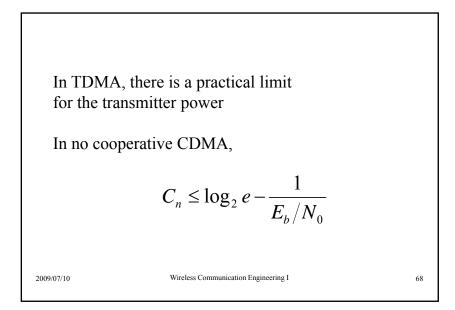
In FDMA, normalized total capacity $C_n = KC_K / W$ (total bit rate for all *K* users per unit of bandwidth)

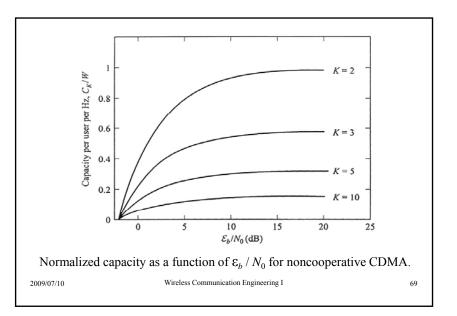
$$C_n = \log_2 \left(1 + C_n \frac{E_b}{N_0} \right)$$

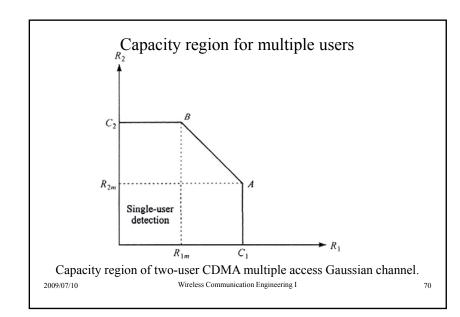


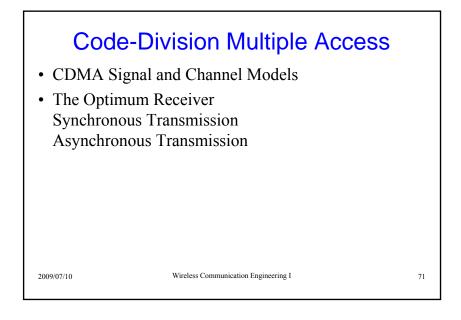


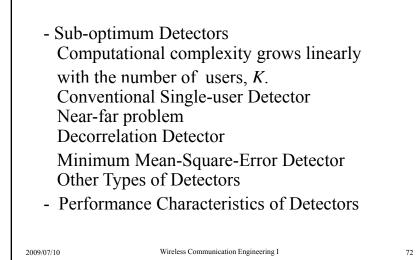


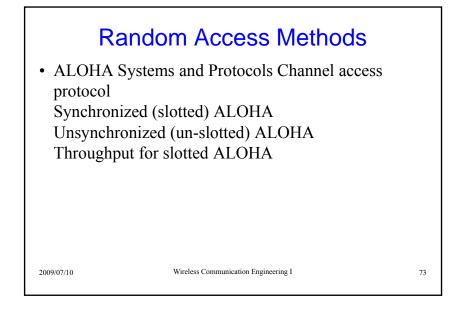


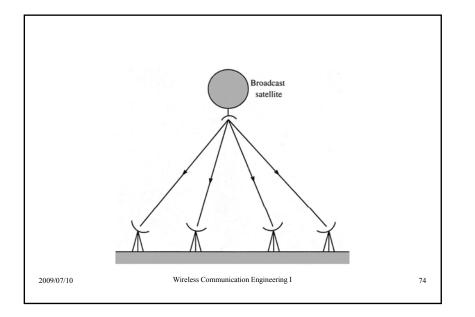


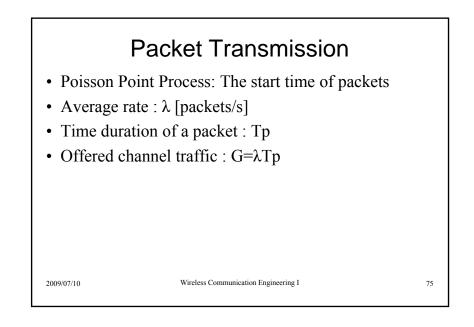


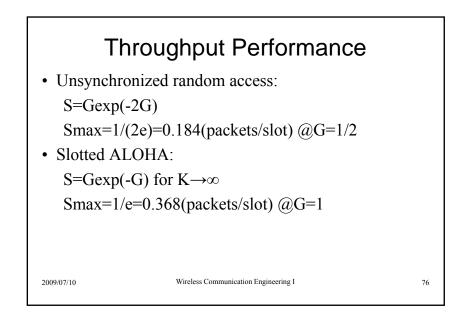


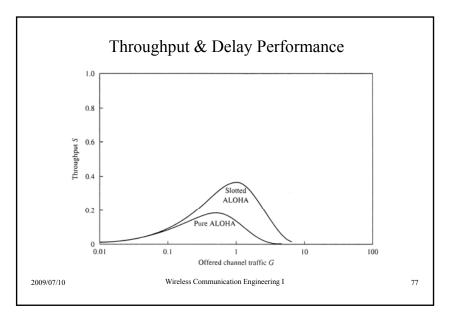


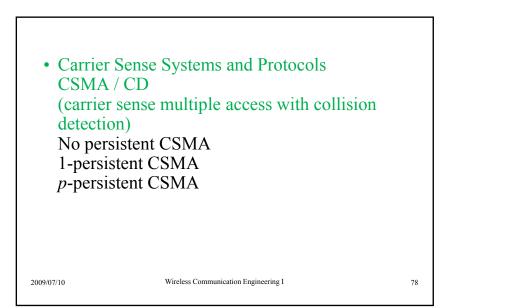


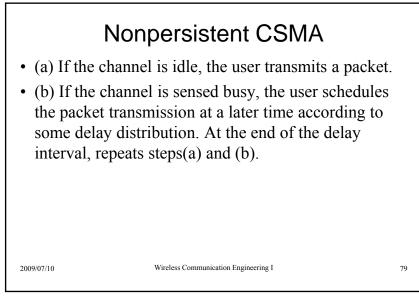












1-persistent CSMA

- (a) If the channel is sensed idle, the user transmits the packet with probability 1.
- (b) If the channel is sensed busy, the user waits until the channel becomes idle and transmits a packet with probability one. Note that in this protocol, a collision will always occur when one user has a packet to transmit.

Wireless Communication Engineering I

80

p-persistent CSMA

- (a) If the channel is idle, the packet is transmitted with probability p, and with probability 1-p the transmission is delayed by τ.
- (b) If at t=τ, the channel is still sensed to be idle, step

 (a) is repeated. If a collision occurs, the user schedules retransmission of the packets according to some preselected transmission delay distribution.
- (c) If at t=τ, the channel is sensed busy, the user waits until it becomes idle, and then operates as in (a) and (b) above.

