# **RF Devices and RF Circuit Design** for Digital Communication

### • Fundamentals of RF Circuits

- Lumped-element circuits:  $\lambda \gg L$ , L is a typical length of device.

e.g. 
$$\lambda = 30$$
 cm for  $f = 1$ GHz

- Distributed-element circuits:  $\lambda \sim L$ Lead Line becomes a coil and/or capacitance.

Historically **Rayleigh** analyzed an undersea cable based on distributed circuit concept.

→Image Impedance and Propagation Constant

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### Agenda

- Fundamentals of RF Circuits
- Transmission Line
- Reflection Coefficient & Smith Chart
- Impedance Matching
- S-matrix Representation
- Amplifiers & Unilateral Gain
- RF Devices
- Digital RF

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- Basic distributed element: **Transmission Line** 

F-matrix of Transmission Line

$$F = \begin{bmatrix} \cos\theta & jZ_0 \sin\theta \\ j\sin\theta/Z_0 & \cos\theta \end{bmatrix}$$

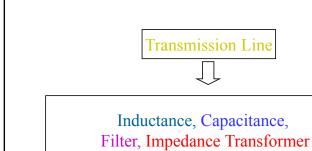
 $Z_0$ : Characteristic impedance of Transmission Line

$$\theta$$
: Phase delay  $\left(=\beta\ell=\omega\sqrt{\varepsilon\mu}\ell=\omega\ell/\nu\right)$ 

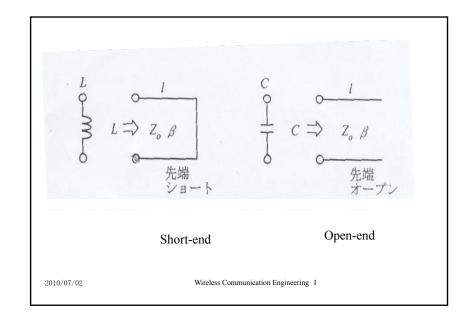
 $\ell$ : length

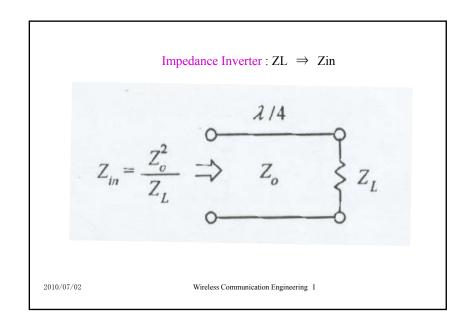
v: velocity

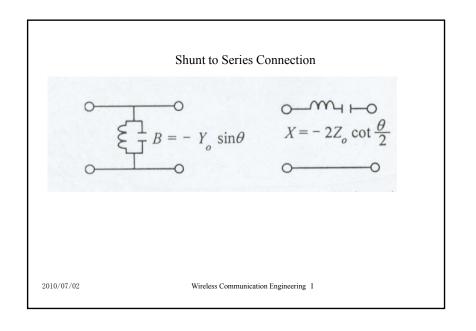
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## Impedance Matrix of Transmission Line

$$Z = \frac{Z_o}{j\sin\theta} \begin{bmatrix} \cos\theta & 1\\ 1 & \cos\theta \end{bmatrix}$$
$$= \frac{Z_o}{j} \left\{ \frac{1}{\theta} \begin{bmatrix} 1 & 1\\ 1 & 1 \end{bmatrix} + \sum_{n=1}^{\infty} \frac{2\theta}{\theta^2 - (n\pi)^2} \begin{bmatrix} 1 & (-1)^n\\ (-1)^n & 1 \end{bmatrix} \right\}$$

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-Short (Open) - circuited load:  $\rightarrow$  Reactance element  $X_{in} = Z_0 \tan \theta$ : short-circuited load

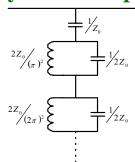
 $0 < \theta < \pi/2$ : Inductance  $\theta \approx \pi/2$ : Parallel resonance circuit  $\pi/2 < \theta < \pi$ : Capacitance

- -Stub
- -Quater-wavelength Transformer
- → Matching coating lense

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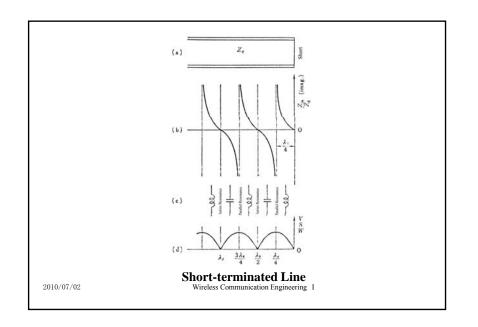
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# **Equivalent Circuit of Transmission Line by Foster Expansion**



**A Series Connection of Parallel Resonance Circuits** 

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• Reflection coefficient ( $\Gamma$ ) and Load Impedance ( $Z_L$ )

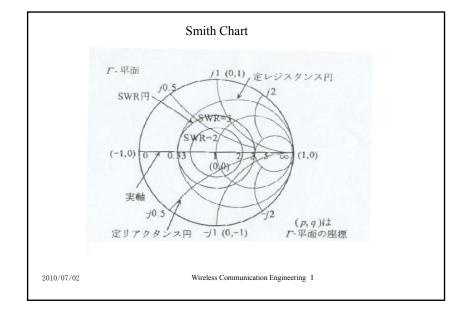
$$\Gamma = \frac{Z_L - Z_0}{Z_L + Z_0}$$
: Bilinear mapping

 $Z_0$ : reference characteristic impedance

Circle to Circle Mapping (Moebius Transform)

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$$|\operatorname{Re}(Z_L)>0:|\Gamma|<1 \text{ (Passive)}|$$

$$|\operatorname{Re}(Z_L) = 0: |\Gamma| = 1 \text{ (Lossless)}$$

Reflection type phase modulator

$$|\operatorname{Re}(Z_L) < 0: |\Gamma| > 1 \text{ (Active)}|$$

Reflectiontypeamplifier

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• Voltage Standing Wave Ratio (VSWR)≥1

$$VSWR = \frac{V_{max}}{V_{min}} = \frac{V_i + V_r}{V_i - V_r}$$

$$\left|\Gamma\right| = \frac{V_r}{V_i} = \frac{VSWR - 1}{VSWR + 1}$$

 $V_i$ : incident wave

 $V_r$ : reflected wave

• Special Terminations / Circuits

-Matched load: 
$$(Z_L = Z_0) \rightarrow \Gamma = 0$$
, No reflection

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### - Smith-chart and its usage

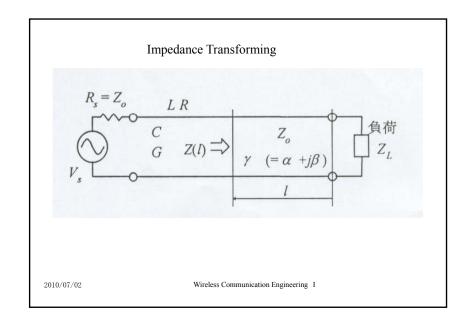
• Smith-chart (Bell Lab. 1950's)

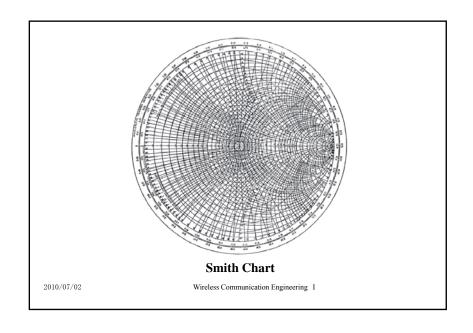
$$Z_{\rm in} = Z_0 \frac{Z_L + jZ_0 \tan \theta}{Z_0 + jZ_L \tan \theta}$$

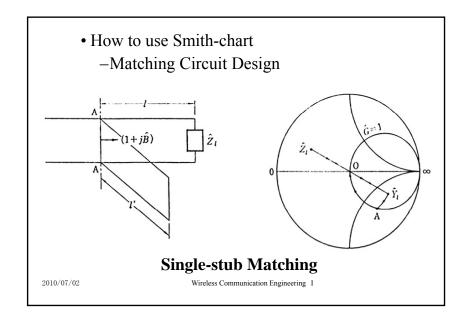
$$Z_{L} \to \widetilde{Z}_{L} = \frac{Z_{L}}{Z_{0}} \to \Gamma_{L} = \frac{\widetilde{Z}_{L} - 1}{\widetilde{Z}_{L} + 1} \to$$

$$\Gamma_{\text{in}} = \Gamma_{L} \exp^{-j2\theta} \to \widetilde{Z}_{\text{in}} = \frac{1 + \Gamma_{\text{in}}}{1 - \Gamma_{\text{in}}} \to Z_{\text{in}}$$

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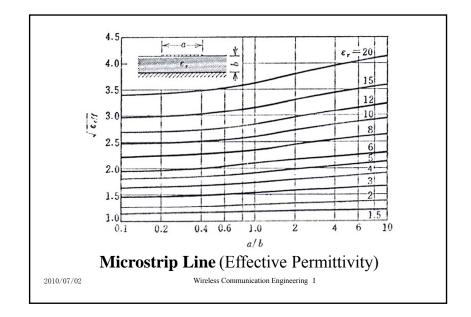


### - Microstrip Line

- Effective permittivity and guided wavelength
- Characteristic Impedance
- Several notes : Finite conductor thickness

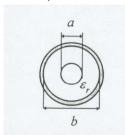
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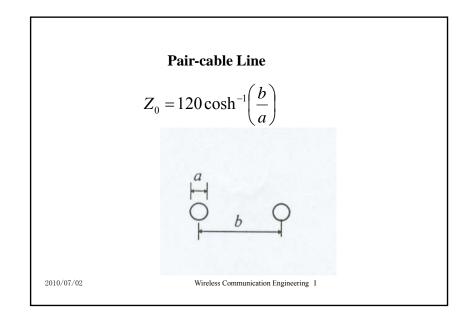


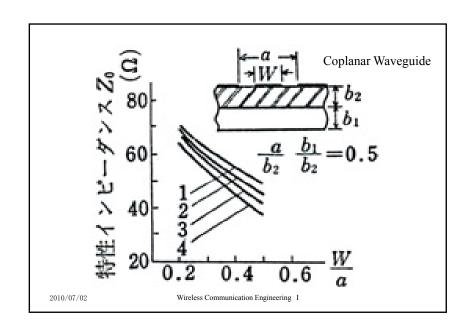
### **Coaxial Line**

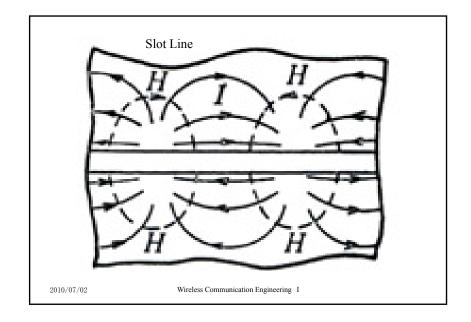
$$Z_0 = \frac{138}{\sqrt{\varepsilon_r}} \log \frac{b}{a}$$



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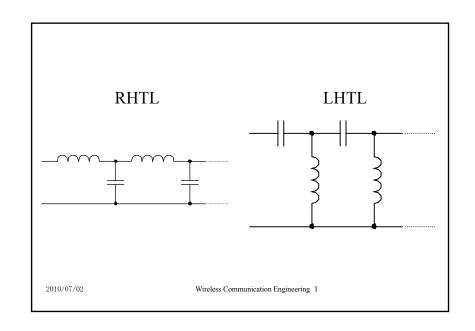


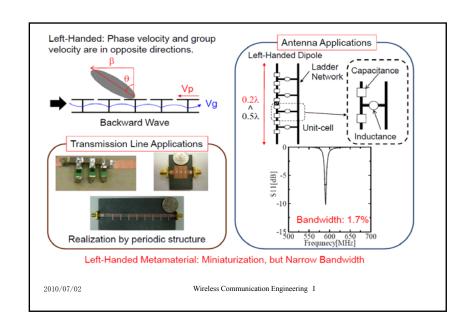


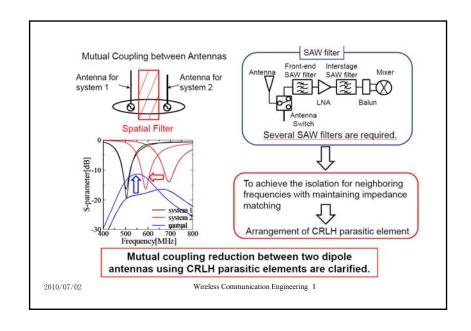
### Meta Material

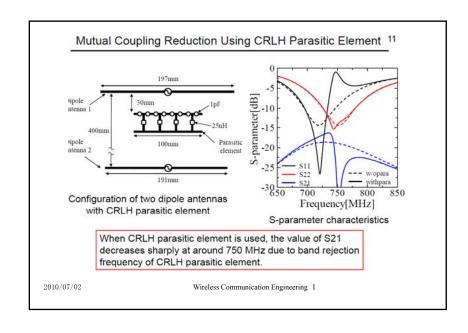
- Right-Hand Transmission Line
- Left-Hand Transmission Line
- Composite RH/LH Transmission Line
- Compact Directional Coupler
- Super-Lense

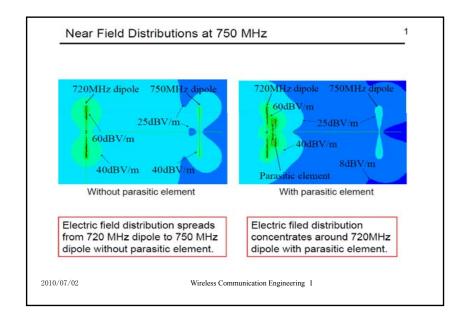
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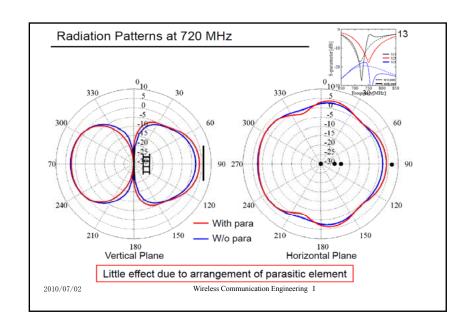


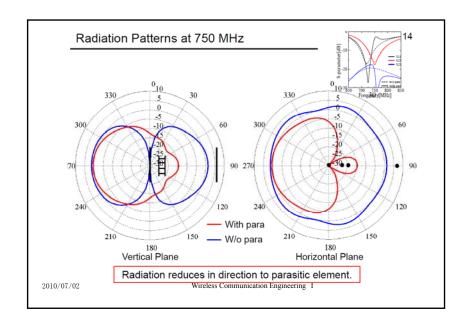












### • S-parameter and RF Circuit Design

-S-parameter (1950's ← Nuclear Physics)

voltage, current  $\rightarrow$  incident wave, reflected wave impedance  $\rightarrow$  reflection coefficient impedance matrix  $\rightarrow$  scattering matrix, [S]

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For lossless circuit, **S-matrix** = **Unitary Matrix** 

For lossy circuit,  $S^{\dagger}S \leq I$  Para-unitary

For Reciprocal circuit, S-matrix = Symmetric matrix

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SVD (Singular Value Decomposition)

$$S=U^{\dagger}DV$$
 (Youla)

U,V: Unitary matrix (Lossless Circuit)

D: Diagonal Matrix ( $\rightarrow$  Isolated n-port circuit)

$$D = Diag[\lambda_1, ..., \lambda_n]$$

$$\lambda_i < 1$$
  $\rightarrow$  resistance

$$\lambda_i > 1$$
  $\rightarrow$  negative resistance

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### -Basics of RF Circuit Design

• Impedance Matching Circuits

$$Z_g = Z_L^*$$

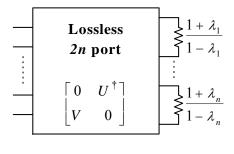
 $Z_g$ : Generator Impedance

 $Z_L$ : Load Impedance

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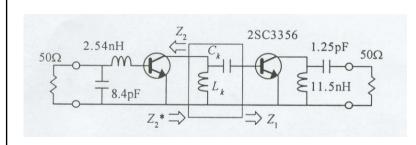
## Generalization of Darlington realization



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### Conjugate Matching



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### Unilateral Transducer Gain $G_{TU}$

(For the case,  $S_{12} = 0$  Reverse transfer coefficient from output to input)

FET 
$$S$$
 - parameter  $\begin{vmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{vmatrix}$ 

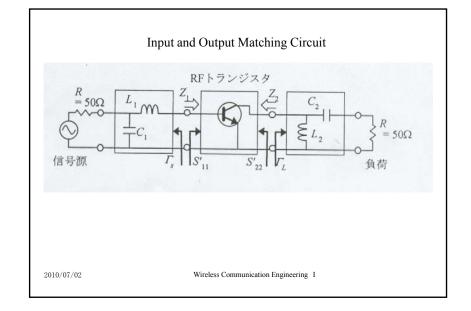
$$G_{TU} = \frac{\left(1 - \left|\Gamma_{s}\right|^{2}\right)}{\left|1 - S_{11}\Gamma_{s}\right|^{2}} \cdot \left|S_{21}\right|^{2} \cdot \frac{\left(1 - \left|\Gamma_{L}\right|^{2}\right)}{\left|1 - S_{22}\Gamma_{L}\right|^{2}}$$

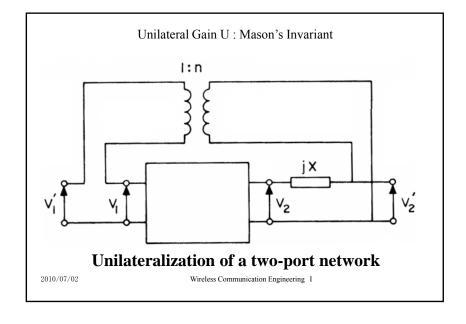
$$= G_{s} \cdot G_{0} \cdot G_{L}$$

$$G_{TU,\text{max}} = \frac{1}{1 - |S_{11}|^2} \cdot |S_{21}|^2 \cdot \frac{1}{1 - |S_{22}|^2}$$

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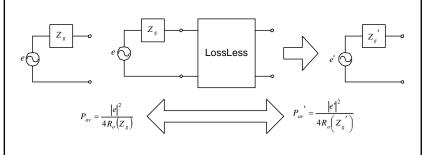


### **Circuit Invariant**

- Unilateral Gain (U)
- Maximum Available Gain (MAG)
- Noise Measure (M)
- 2-state diode (m, Q)
- Circulator Invariant (α)
- Directional Coupler Invariant (K)

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### Available Power



### 2-state device

- On-state impedance Z1, Off-state impedance Z2
- M= $|Z1-Z2|/|Z1+Z2*| \Rightarrow$  Invariant w.r.t. Lossless 2port connection
- M= $|\Gamma 1 \Gamma 2| / |1 \Gamma 1 \Gamma 2^*| \Rightarrow \text{Optimum BPSK}$ Direct Modulation Design

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### RF Devices

- Passive Components / Circuits
  - Reactance Elements
    - Distributed-element:
       Open-stub, Short-stub, Line Gap
       Wide Line, Narrow Line
    - Lumped-element:Spiral Inductor, Gap Capacitor, Thin Film Capacitor

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### Attenuators:

Thin Film Resistor

• Impedance Transformers: Quarter-wavelength Impedance Transformer

$$Z_{\rm in} = \frac{{Z_0}^2}{Z_L}$$

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### • Resonator:

- -Lumped Element Type
- -Microstrip Line Type
- -Dielectric Resonator Type (Good Ceramic)

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# (3) $Y_0$ $Y_a$ $Y_0$ (4) $Y_b$ $Y_b$ $Y_0$ (2) Branch-line Coupler 2010/07/02 Wireless Communication Engineering I

### - Distributing Components / Circuits

• Directional Coupler:

Power Monitor, Balanced Type Modulator / Amplifier / Mixer Lossless reciprocal matched two-fold symmetry 4-port

- → Perfect Directional Coupler with 90deg. Phase Difference
- Coupled Line Type
- Inter-digital Type
- Branch Line Type
- Rat-race Type

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### • Power Divider / Combiner:

Perfect Matching + Perfect Isolation → Absorbing Resistance

- Filter
  - -Low Pass Filter (LPF):
  - L, C Ladder Filter
  - Band Pass Filter (BPF):Half-wavelength transmission line resonator
  - -Band Stop Filter (BSF):

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### • Transmission Scheme and RF Circuits

Objectives: Low Power Consumption, Higher Frequency, Small Size, Low Weight

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### – Basic configuration of RF Circuits: Super-Heterodyne

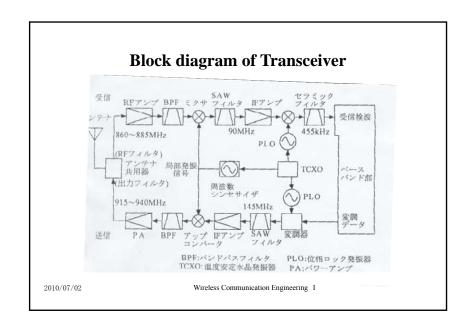
Mixer: Up-conversion Down-conversion

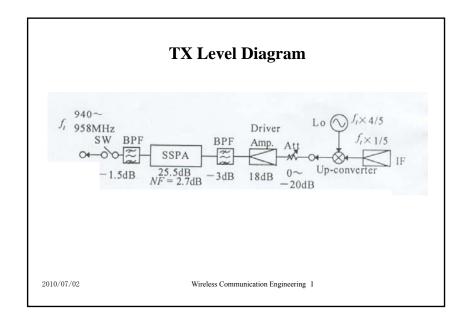
Amplifier: Power Amp. (TX) Low Noise Amp. (RX)

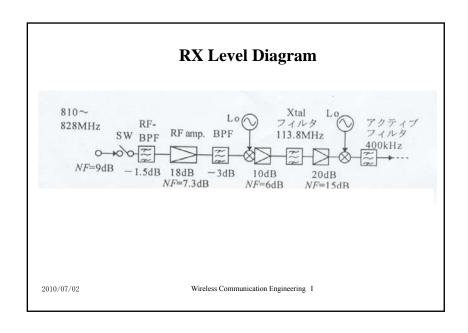
Oscillator: Local Oscillator

Filter: LPF, BPF

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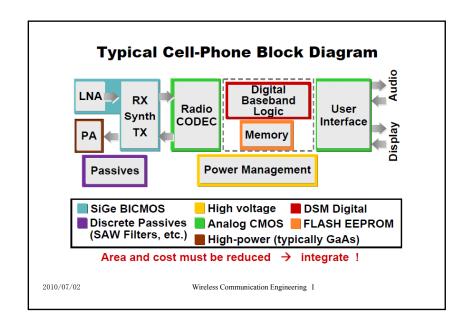


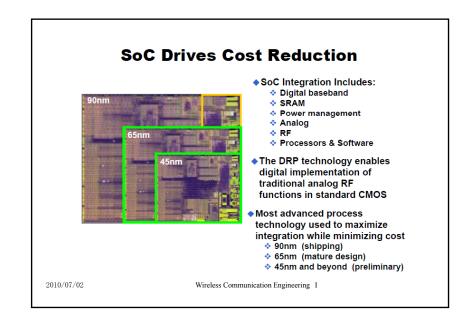


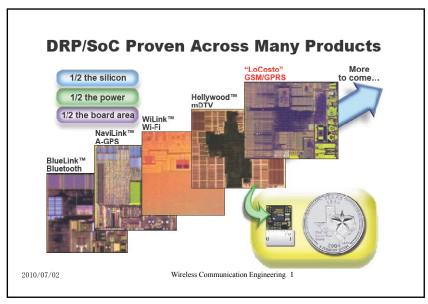
## Digital RF Circuits

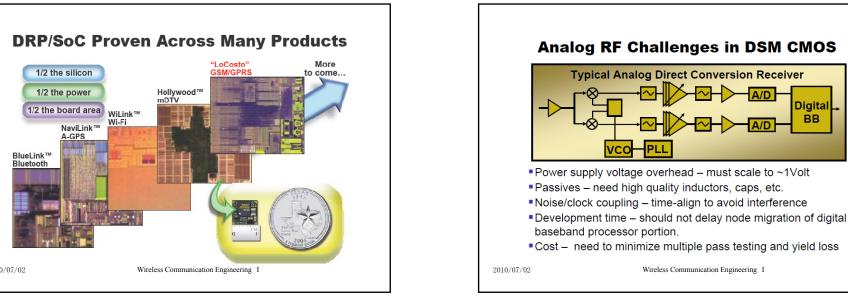
- RF-CMOS Technology
- Analog Signal Processing & Digital Signal Processing
- Continuous Time & Discrete Time
- Direct Conversion & Sampling
- Built-in RF Self Test & Calibration

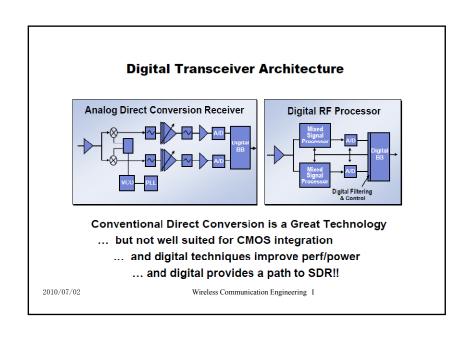
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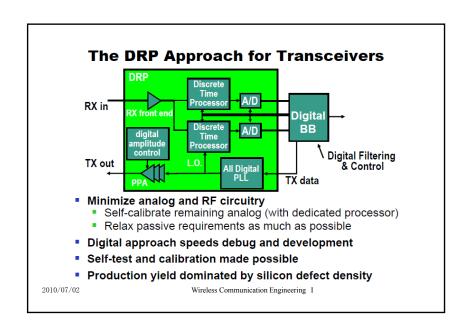












Digital

BB

