

In[194]:= (*Instructor: Hiroyuki Akama

Basic Built-in Functions of Mathematica Linear Algebra– List Vector and Matrix (2)*)

```
t = {1, 2, 3, 4, 5, 6, 7, 8, 9, 10};  
t  
? Table  
Table[i, {i, 10}]  
Table[i, {i, 4}, {j, 8}]  
% // MatrixForm  
? MatrixForm
```

Out[195]= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10}

Table[*expr*, {*i*_{max}}] generates a list of *i*_{max} copies of *expr*.

Table[*expr*, {*i*, *i*_{max}}] generates a list of the values of *expr* when *i* runs from 1 to *i*_{max}.

Table[*expr*, {*i*, *i*_{min}, *i*_{max}}] starts with *i* = *i*_{min}.

Table[*expr*, {*i*, *i*_{min}, *i*_{max}, *di*}] uses steps *di*.

Table[*expr*, {*i*, {*i*₁, *i*₂, ...}}] uses the successive values *i*₁, *i*₂, ...

Table[*expr*, {*i*, {*i*_{min}, *i*_{max}}, {*j*, {*j*_{min}, *j*_{max}}, ...}] gives a nested list. The list associated with *i* is outermost. >>

Out[197]= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10}

Out[198]= {{1, 1, 1, 1, 1, 1, 1, 1}, {2, 2, 2, 2, 2, 2, 2, 2},
{3, 3, 3, 3, 3, 3, 3, 3}, {4, 4, 4, 4, 4, 4, 4, 4}}

Out[199]//MatrixForm=

$$\begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 2 & 2 & 2 & 2 & 2 & 2 & 2 & 2 \\ 3 & 3 & 3 & 3 & 3 & 3 & 3 & 3 \\ 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 \end{pmatrix}$$

MatrixForm[*list*] prints with the elements of *list* arranged in a regular array. >>

```
In[201]:= matrix1 = {{1, 0, 0, 1}, {1, 1, 0, 1}, {0, 0, 1, 1}, {0, 1, 0, 1}};
matrix1 // MatrixForm
MatrixForm[matrix1]
matrix1 - IdentityMatrix[Length[matrix1]] // MatrixForm
? IdentityMatrix
```

```
Out[202]//MatrixForm=

$$\begin{pmatrix} 1 & 0 & 0 & 1 \\ 1 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 \end{pmatrix}$$

```

```
Out[203]//MatrixForm=

$$\begin{pmatrix} 1 & 0 & 0 & 1 \\ 1 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 \end{pmatrix}$$

```

```
Out[204]//MatrixForm=

$$\begin{pmatrix} 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \end{pmatrix}$$

```

IdentityMatrix[n] gives the $n \times n$ identity matrix. >>

```
In[206]:= F0[i_, j_] := 1;
Array[F0, {4, 4}]
? Array
Table[1, {i, 4}, {j, 4}]
matrix1 /. {0 -> 1, 1 -> 0} // MatrixForm
ReplaceAll[matrix1, {0 -> 1, 1 -> 0}] // MatrixForm
? ReplaceAll
```

```
Out[207]= {{1, 1, 1, 1}, {1, 1, 1, 1}, {1, 1, 1, 1}, {1, 1, 1, 1}}
```

Array[f, n] generates a list of length n , with elements $f[i]$.

Array[f, { n_1, n_2, \dots }] generates an $n_1 \times n_2 \times \dots$ array of nested lists, with elements $f[i_1, i_2, \dots]$.

Array[f, { n_1, n_2, \dots }, { r_1, r_2, \dots }] generates a list using the index origins r_i (default 1).

Array[f, dims, origin, h] uses head h , rather than List, for each level of the array. >>

```
Out[209]= {{1, 1, 1, 1}, {1, 1, 1, 1}, {1, 1, 1, 1}, {1, 1, 1, 1}}
```

```
Out[210]//MatrixForm=

$$\begin{pmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 \end{pmatrix}$$

```

```
Out[211]//MatrixForm=

$$\begin{pmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 \end{pmatrix}$$

```

expr /. rules applies a rule or list of rules in an attempt to transform each subpart of an expression *expr*. >>

```
In[213]:= F1[i_, j_] := If[i == j, 1, 0];
          Array[F1, {7, 7}];
          % // MatrixForm
          IdentityMatrix[7] == Array[F1, {7, 7}]
```

```
Out[215]//MatrixForm=

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

```

```
Out[216]= True
```

```
In[217]:= RandomInteger[{1, 4}]
          ? RandomInteger
          samplelist = Table[RandomInteger[{1, 4}], {i, 8}]
```

```
Out[217]= 1
```

`RandomInteger[{ i_{\min} , i_{\max} }]` gives a pseudorandom integer in the range $\{i_{\min}, \dots, i_{\max}\}$.
`RandomInteger[i_{\max}]` gives a pseudorandom integer in the range $\{0, \dots, i_{\max}\}$.
`RandomInteger[]` pseudorandomly gives 0 or 1.
`RandomInteger[range, n]` gives a list of n pseudorandom integers.
`RandomInteger[range, { n_1 , n_2 , ...}]` gives an $n_1 \times n_2 \times \dots$ array of pseudorandom integers.
`RandomInteger[dist, ...]` samples from the symbolic discrete distribution *dist*. >>

```
Out[219]= {1, 3, 2, 4, 1, 4, 4, 2}
```

```
In[220]:= ? Part
          samplelist[[2]]
          Part[samplelist, 2]
          samplelist[[2]] == Part[samplelist, 2]
```

`expr[[i]]` or `Part[expr, i]` gives the i^{th} part of *expr*.
`expr[[- i]]` counts from the end.
`expr[[i , j , ...]]` or `Part[expr, i , j , ...]` is equivalent to `expr[[i]][[j]]`
`expr[{{ i_1 , i_2 , ...}}]` gives a list of the parts i_1 , i_2 , ... of *expr*.
`expr[[m ;; n]]` gives parts m through n .
`expr[[m ;; n ;; s]]` gives parts m through n in steps of s . >>

```
Out[221]= 3
```

```
Out[222]= 3
```

```
Out[223]= True
```

```
In[224]:= MyRandomFunction1[m_, n_] := Table[RandomInteger[{1, m}], {i, n}];
MyRandomFunction1[6, 8]
Table[MyRandomFunction1[6, 8], {10}]
? Table
```

```
Out[225]= {1, 1, 2, 1, 3, 3, 3, 1}
```

```
Out[226]= {{3, 5, 3, 1, 5, 2, 2, 3}, {4, 5, 5, 5, 3, 5, 5, 6},
{6, 2, 5, 1, 2, 5, 4, 6}, {6, 5, 5, 1, 6, 6, 6, 5},
{5, 2, 2, 2, 3, 5, 2, 6}, {5, 6, 6, 6, 6, 6, 1, 6}, {3, 4, 5, 2, 6, 4, 5, 2},
{4, 5, 4, 2, 3, 2, 1, 2}, {2, 3, 1, 5, 6, 4, 6, 6}, {1, 1, 5, 6, 2, 3, 6, 4}}
```

`Table[expr, {imax}]` generates a list of *i_{max}* copies of *expr*.

`Table[expr, {i, imax}]` generates a list of the values of *expr* when *i* runs from 1 to *i_{max}*.

`Table[expr, {i, imin, imax}]` starts with *i* = *i_{min}*.

`Table[expr, {i, imin, imax, di}]` uses steps *di*.

`Table[expr, {i, {i1, i2, ...}}]` uses the successive values *i₁*, *i₂*,

`Table[expr, {i, imin, imax}, {j, jmin, jmax}, ...]` gives a nested list. The list associated with *i* is outermost. >>

```
In[228]:= MyRandomFunction2[m_, n_, t_] := Table[Table[RandomInteger[{1, m}], {i, n}], {t}];
samplematrix = MyRandomFunction2[4, 8, 12]
MyRandomFunction2a[m_, n_, t_] := Table[RandomInteger[{1, m}], {i, n}, {j, t}];
samplematrix2a = MyRandomFunction2a[4, 12, 8]
```

```
Out[228]= {{3, 4, 1, 2, 1, 3, 4, 4}, {3, 2, 1, 4, 4, 2, 1, 2}, {3, 2, 3, 4, 3, 2, 3, 2},
{4, 4, 1, 1, 2, 4, 2, 2}, {2, 2, 1, 4, 3, 1, 3, 1}, {4, 2, 2, 2, 4, 4, 3, 2},
{1, 3, 2, 4, 2, 4, 3, 3}, {3, 3, 4, 4, 4, 4, 1, 3}, {2, 1, 1, 1, 1, 4, 2, 2},
{2, 1, 1, 1, 3, 1, 1, 2}, {1, 3, 4, 4, 2, 3, 1, 1}, {1, 3, 2, 2, 2, 3, 3, 1}}
```

General::spell1 :

New symbol name "MyRandomFunction2a" is similar to existing symbol "MyRandomFunction2" and may be misspelled. >>

```
Out[230]= {{4, 4, 2, 1, 2, 4, 4, 1}, {1, 3, 3, 3, 2, 3, 2, 2}, {4, 2, 4, 3, 1, 1, 4, 1},
{3, 3, 2, 2, 3, 3, 2, 2}, {2, 3, 4, 2, 4, 3, 4, 2}, {3, 2, 2, 1, 2, 2, 2, 3},
{3, 2, 3, 1, 3, 3, 4, 1}, {1, 3, 3, 2, 3, 2, 4, 2}, {4, 4, 1, 3, 2, 1, 3, 3},
{4, 3, 3, 2, 4, 4, 4, 2}, {4, 4, 4, 4, 4, 2, 1, 1}, {2, 4, 1, 4, 3, 1, 3, 1}}
```

```
In[231]:= samplematrix[[3]]
```

```
Out[231]= {3, 2, 3, 4, 3, 2, 3, 2}
```

```
In[232]:= samplematrix[[3, 8]]
samplematrix[[3]][[8]]
samplematrix[[3, 8]] == samplematrix[[3]][[8]]
Part[samplematrix, 3]
Part[samplematrix, 3, 8]
```

```
Out[232]= 2
```

```
Out[233]= 2
```

```
Out[234]= True
```

```
Out[235]= {3, 2, 3, 4, 3, 2, 3, 2}
```

```
Out[236]= 2
```

```
In[237]:= samplematrix1 = MyRandomFunction2[6, 8, 8]
```

```
Out[237]= {{3, 2, 6, 6, 5, 1, 1, 1}, {1, 3, 1, 5, 2, 6, 4, 2},
           {4, 4, 2, 5, 6, 1, 6, 3}, {2, 4, 4, 1, 4, 4, 5, 3}, {1, 3, 6, 4, 1, 1, 3, 1},
           {2, 5, 1, 6, 2, 1, 6, 6}, {4, 2, 6, 3, 6, 2, 2, 2}, {5, 3, 3, 4, 3, 1, 5, 1}}
```

```
In[239]:= MatrixPower[samplematrix1, 4] // MatrixForm
? MatrixPower
```

```
Out[239]//MatrixForm=
```

```
( 45 656 54 521 64 186 68 318 63 595 37 830 66 882 39 148
 44 484 53 024 62 566 66 587 61 957 36 810 64 970 38 120
 54 932 65 350 77 438 81 821 76 419 45 773 80 174 46 730
 49 205 58 774 69 068 73 833 68 524 40 622 72 102 42 242
 38 021 45 398 53 106 56 731 53 051 31 475 55 807 32 608
 52 315 62 303 73 517 77 774 72 818 43 557 76 536 44 519
 48 773 58 337 68 618 73 268 67 956 40 302 71 536 41 923
 45 441 54 049 63 846 67 638 63 315 37 863 66 366 38 699 )
```

MatrixPower $[m, n]$ gives the n^{th} matrix power of the matrix m .

MatrixPower $[m, n, v]$ gives the n^{th} matrix power of the matrix m applied to the vector v . >>

```
In[241]:= MyMatrixFunction[i_] := MatrixPower[samplematrix1, i];
MyMatrixFunction[3]
MyMatrixFunction[3][[4]]
MyMatrixFunction[3][[4]][[5]]
```

```
Out[242]= {{1760, 2089, 2468, 2627, 2453, 1473, 2568, 1498},
           {1749, 2031, 2370, 2551, 2364, 1449, 2513, 1462},
           {2098, 2545, 2900, 3183, 2954, 1704, 3135, 1845},
           {1901, 2251, 2690, 2786, 2652, 1606, 2760, 1603},
           {1456, 1734, 2117, 2210, 2002, 1209, 2104, 1239},
           {1998, 2405, 2809, 3076, 2790, 1608, 2928, 1762},
           {1881, 2231, 2667, 2764, 2655, 1595, 2742, 1578},
           {1725, 2110, 2441, 2631, 2417, 1405, 2592, 1507}}
```

```
Out[243]= {1901, 2251, 2690, 2786, 2652, 1606, 2760, 1603}
```

```
Out[244]= 2652
```

```
In[256]:= samplelist
? Select
Select[samplelist, EvenQ]
Select[samplelist, OddQ]
Union[%]
```

```
Out[256]= {1, 3, 2, 4, 1, 4, 4, 2}
```

Select[list, crit] picks out all elements e_i of list for which crit[e_i] is True.
 Select[list, crit, n] picks out the first n elements for which crit[e_i] is True. >>

```
Out[258]= {2, 4, 4, 4, 2}
```

```
Out[259]= {1, 3, 1}
```

```
Out[260]= {1, 3}
```

Select[list, crit] crit[e_i]がTrueとなる list のすべての要素 e_i を取り出す .
 Select[list, crit, n] crit[e_i]がTrueとなる最初から n 個の要素を取り出す . >>

```
{4, 4, 4, 4, 2}
```

```
{1, 3, 3}
```

```
{1, 3}
```

```
In[250]:= Cases[samplelist, x_? (Mod[#, 2] == 0 &)]
Cases[samplelist, x_? (Mod[#, 2] != 0 &)]
? Cases
? Mod
Select[samplelist, EvenQ] == Cases[samplelist, x_? (Mod[#, 2] == 0 &)]
Select[samplelist, OddQ] == Cases[samplelist, x_? (Mod[#, 2] != 0 &)]
```

```
Out[250]= {2, 4, 4, 4, 2}
```

```
Out[251]= {1, 3, 1}
```

Cases[{ e_1, e_2, \dots }, pattern] gives a list of the e_i that match the pattern.
 Cases[{ e_1, \dots }, pattern \rightarrow rhs] gives a list of the values of rhs corresponding to the e_i that match the pattern.
 Cases[expr, pattern, levelspec] gives a list of all parts of expr on levels specified by levelspec that match the pattern.
 Cases[expr, pattern \rightarrow rhs, levelspec] gives the values of rhs that match the pattern.
 Cases[expr, pattern, levelspec, n] gives the first n parts in expr that match the pattern. >>

Mod[m, n] gives the remainder on division of m by n .
 Mod[m, n, d] uses an offset d . >>

```
Out[254]= True
```

```
Out[255]= True
```

```

In[261]:= samplelist
Position[samplelist, x_? (# == 1 &)]
Position[samplelist, x_? (Mod[#, 2] != 0 &)]
Position[samplelist, x_? (# ≥ 3 &)]
Flatten[Position[samplelist, x_? (# == 3 &)]]
Part[samplelist, %]

Out[261]= {1, 3, 2, 4, 1, 4, 4, 2}

Out[262]= {{1}, {5}}

Out[263]= {{1}, {2}, {5}}

Out[264]= {{2}, {4}, {6}, {7}}

Out[265]= {2}

Out[266]= {3}

In[267]:= Position[IdentityMatrix[4], x_? (# == 1 &), 2]
Position[IdentityMatrix[4], x_? (# ≠ 1 &), 2]

Out[267]= {{1, 1}, {2, 2}, {3, 3}, {4, 4}}

Out[268]= {{1, 2}, {1, 3}, {1, 4}, {2, 1}, {2, 3}, {2, 4}, {3, 1}, {3, 2}, {3, 4}, {4, 1}, {4, 2}, {4, 3}}

In[269]:= samplematrix1
% // MatrixForm
Position[samplematrix1, x_? (# == 6 &), 2]
Position[samplematrix1, x_? (# < 3 &), 2]
? Position

Out[269]= {{3, 2, 6, 6, 5, 1, 1, 1}, {1, 3, 1, 5, 2, 6, 4, 2},
           {4, 4, 2, 5, 6, 1, 6, 3}, {2, 4, 4, 1, 4, 4, 5, 3}, {1, 3, 6, 4, 1, 1, 3, 1},
           {2, 5, 1, 6, 2, 1, 6, 6}, {4, 2, 6, 3, 6, 2, 2, 2}, {5, 3, 3, 4, 3, 1, 5, 1}}

Out[270]//MatrixForm=

$$\begin{pmatrix} 3 & 2 & 6 & 6 & 5 & 1 & 1 & 1 \\ 1 & 3 & 1 & 5 & 2 & 6 & 4 & 2 \\ 4 & 4 & 2 & 5 & 6 & 1 & 6 & 3 \\ 2 & 4 & 4 & 1 & 4 & 4 & 5 & 3 \\ 1 & 3 & 6 & 4 & 1 & 1 & 3 & 1 \\ 2 & 5 & 1 & 6 & 2 & 1 & 6 & 6 \\ 4 & 2 & 6 & 3 & 6 & 2 & 2 & 2 \\ 5 & 3 & 3 & 4 & 3 & 1 & 5 & 1 \end{pmatrix}$$


Out[271]= {{1, 3}, {1, 4}, {2, 6}, {3, 5}, {3, 7}, {5, 3}, {6, 4}, {6, 7}, {6, 8}, {7, 3}, {7, 5}}

Out[272]= {{1, 2}, {1, 6}, {1, 7}, {1, 8}, {2, 1}, {2, 3}, {2, 5}, {2, 8},
           {3, 3}, {3, 6}, {4, 1}, {4, 4}, {5, 1}, {5, 5}, {5, 6}, {5, 8}, {6, 1},
           {6, 3}, {6, 5}, {6, 6}, {7, 2}, {7, 6}, {7, 7}, {7, 8}, {8, 6}, {8, 8}}

```

`Position[expr, pattern]` gives a list of the positions at which objects matching *pattern* appear in *expr*.

`Position[expr, pattern, levelspec]` finds only objects that appear on levels specified by *levspec*.

`Position[expr, pattern, levelspec, n]` gives the positions of the first *n* objects found. >>

```

In[274]:= samplematrix1

Out[274]= {{3, 2, 6, 6, 5, 1, 1, 1}, {1, 3, 1, 5, 2, 6, 4, 2},
           {4, 4, 2, 5, 6, 1, 6, 3}, {2, 4, 4, 1, 4, 4, 5, 3}, {1, 3, 6, 4, 1, 1, 3, 1},
           {2, 5, 1, 6, 2, 1, 6, 6}, {4, 2, 6, 3, 6, 2, 2, 2}, {5, 3, 3, 4, 3, 1, 5, 1}}

```

```
In[275]:= Clear[samplematrix1]
? Clear
```

`Clear[symbol1, symbol2, ...]` clears values and definitions for the *symbol_i*.
`Clear["form1", "form2", ...]` clears values and definitions for all symbols whose names match any of the string patterns *form_i*. >>

```
In[277]:= samplematrix1
```

```
Out[277]= samplematrix1
```

```
In[278]:= samplelist
```

```
Out[278]= {1, 3, 2, 4, 1, 4, 4, 2}
```

```
In[279]:= Range[Length[samplelist]]
? Range
```

```
Out[279]= {1, 2, 3, 4, 5, 6, 7, 8}
```

`Range[imax]` generates the list {1, 2, ..., i_{max}}.
`Range[imin, imax]` generates the list {i_{min}, ..., i_{max}}.
`Range[imin, imax, di]` uses step *di*. >>

```
In[281]:= Part[samplelist, 1]
Part[samplelist, 2]
Part[samplelist, 3]
Part[samplelist, 4]
Part[samplelist, 5]
Part[samplelist, 6]
Part[samplelist, 7]
Part[samplelist, 8]
{{1, Part[samplelist, 1]}, {2, Part[samplelist, 2]},
 {3, Part[samplelist, 3]}, {4, Part[samplelist, 4]}, {5, Part[samplelist, 5]},
 {6, Part[samplelist, 6]}, {7, Part[samplelist, 7]}, {8, Part[samplelist, 8]}}
Transpose[{Range[Length[samplelist]], samplelist}]
```

```
Out[281]= 1
```

```
Out[282]= 3
```

```
Out[283]= 2
```

```
Out[284]= 4
```

```
Out[285]= 1
```

```
Out[286]= 4
```

```
Out[287]= 4
```

```
Out[288]= 2
```

```
Out[289]= {{1, 1}, {2, 3}, {3, 2}, {4, 4}, {5, 1}, {6, 4}, {7, 4}, {8, 2}}
```

```
Out[290]= {{1, 1}, {2, 3}, {3, 2}, {4, 4}, {5, 1}, {6, 4}, {7, 4}, {8, 2}}
```



```
In[291]:= Insert[{1, 2, 3, 4}, 2.5, 3]
? Insert
```

```
Out[291]= {1, 2, 2.5, 3, 4}
```

`Insert[list, elem, n]` inserts *elem* at position *n* in *list*. If *n* is negative, the position is counted from the end.
`Insert[expr, elem, {i, j, ...}]` inserts *elem* at position {*i*, *j*, ...} in *expr*.
`Insert[expr, elem, {{i1, j1, ...}, {i2, j2, ...}, ...}]` inserts *elem* at several positions. >>

```
In[293]:= samplelist1 = {1, 3, 2, 1, 5, 6, 7, 3, 1, 9};
pos = {2, 7, 9};
samplelist1inserted = {1, {}, 3, 2, 1, 5, {}, 6, {}, 7, 3, 1, 9};
```

```
In[296]:= Part[samplelist1inserted, pos]

Insert[samplelist1, {}, pos[[1]]]
Insert[Insert[samplelist1, {}, pos[[1]]], {}, pos[[2]]]
Insert[Insert[Insert[samplelist1, {}, pos[[1]]], {}, pos[[2]]], {}, pos[[3]]]
```

```
Out[296]= {{}, {}, {}}
```

```
Out[297]= {1, {}, 3, 2, 1, 5, 6, 7, 3, 1, 9}
```

```
Out[298]= {1, {}, 3, 2, 1, 5, {}, 6, 7, 3, 1, 9}
```

```
Out[299]= {1, {}, 3, 2, 1, 5, {}, 6, {}, 7, 3, 1, 9}
```

```
In[300]:= ? While
? Drop
i = 1;
tmp[1] = samplelist1;
While[i ≤ Length[pos], tmp[i + 1] = Insert[tmp[i], {}, pos[[i]]]; i++]
tmp[i]
j = 1;
poslist = {2, 4, 6, 8, 10, 12, 14, 16, 18};
mylist[1] = {1, 2, 3, 4, 5, 6, 7, 8, 9, 10};
While[j ≤ Length[poslist], mylist[j + 1] = Insert[mylist[j], NUL, poslist[[j]]]; j++]
mylist[j]
Drop[Flatten[{#, NUL} & /@ {1, 2, 3, 4, 5, 6, 7, 8, 9, 10}], -1]
```

`While[test, body]` evaluates *test*, then *body*, repetitively, until *test* first fails to give True. >>

`Drop[list, n]` gives *list* with its first *n* elements dropped.
`Drop[list, -n]` gives *list* with its last *n* elements dropped.
`Drop[list, {n}]` gives *list* with its *n*th element dropped.
`Drop[list, {m, n}]` gives *list* with elements *m* through *n* dropped.
`Drop[list, {m, n, s}]` gives *list* with elements *m* through *n* in steps of *s* dropped.
`Drop[list, seq1, seq2, ...]` gives a nested list
in which elements specified by *seq_i* have been dropped at level *i* in *list*. >>

```
Out[305]= {1, {}, 3, 2, 1, 5, {}, 6, {}, 7, 3, 1, 9}
```

```
Out[310]= {1, NUL, 2, NUL, 3, NUL, 4, NUL, 5, NUL, 6, NUL, 7, NUL, 8, NUL, 9, NUL, 10}
```

```
Out[311]= {1, NUL, 2, NUL, 3, NUL, 4, NUL, 5, NUL, 6, NUL, 7, NUL, 8, NUL, 9, NUL, 10}
```

```
In[312]:= samplelist1 = {1, 3, 2, 1, 5, 6, 7, 3, 1, 9};
samplelist2 = samplelist1^2
Clear[samplelist1]
samplelist1 = samplelist2;
samplelist1
```

```
Out[313]= {1, 9, 4, 1, 25, 36, 49, 9, 1, 81}
```

```
Out[316]= {1, 9, 4, 1, 25, 36, 49, 9, 1, 81}
```

```
In[317]:= ? Prepend
? Join
Insert[samplelist1, 0, 1]
Prepend[samplelist1, 0]
Join[{0}, samplelist1]
Prepend[samplelist1, 0] == Insert[samplelist1, 0, 1]
Insert[samplelist1, 0, 1] == Join[{0}, samplelist1]
```

`Prepend[expr, elem]` gives *expr* with *elem* prepended. >>

`Join[list1, list2, ...]` concatenates lists or other expressions that share the same head.

`Join[list1, list2, ..., n]` joins the objects at level *n* in each of the *list_i*. >>

```
Out[319]= {0, 1, 9, 4, 1, 25, 36, 49, 9, 1, 81}
```

```
Out[320]= {0, 1, 9, 4, 1, 25, 36, 49, 9, 1, 81}
```

```
Out[321]= {0, 1, 9, 4, 1, 25, 36, 49, 9, 1, 81}
```

```
Out[322]= True
```

```
Out[323]= True
```

```
In[324]:= Insert[samplelist1, 0, -1]
Append[samplelist1, 0]
Join[samplelist1, {0}]
Append[samplelist1, 0] == Insert[samplelist1, 0, -1] == Join[samplelist1, {0}]
```

```
Out[324]= {1, 9, 4, 1, 25, 36, 49, 9, 1, 81, 0}
```

```
Out[325]= {1, 9, 4, 1, 25, 36, 49, 9, 1, 81, 0}
```

```
Out[326]= {1, 9, 4, 1, 25, 36, 49, 9, 1, 81, 0}
```

```
Out[327]= True
```

```
In[328]:= Union[{1, 2, 3}, {3, 4, 5}]
Intersection[{1, 2, 3}, {3, 4, 5}]
Complement[{1, 2, 3}, {3, 4, 5}]
Complement[{3, 4, 5}, {1, 2, 3}]
MyComplement[list1_, list2_] := {Complement[list1, list2], Complement[list2, list1]};
MyComplement[{1, 2, 3}, {3, 4, 5}]
```

```
Out[328]= {1, 2, 3, 4, 5}
```

```
Out[329]= {3}
```

```
Out[330]= {1, 2}
```

```
Out[331]= {4, 5}
```

```
Out[333]= {{1, 2}, {4, 5}}
```

```
In[334]:= Table[RandomInteger[4], {i, 30}]
```

```
ex = Table[RandomInteger[4], {i, 30}] /. {0 → a, 1 → b, 2 → c, 3 → d, 4 → e}
ReplaceAll[Table[RandomInteger[4], {i, 30}], {0 → a, 1 → b, 2 → c, 3 → d, 4 → e}]
? ReplaceAll
sortandsplitex = Split[Sort[ex]]
Split[Sort[ex]]
frequencyvalue = Length /@ sortandsplitex
Length[#] & /@ sortandsplitex
(Length[#1] &) /@ sortandsplitex
frequencylist = MapThread[{#1, #2} &, {{a, b, c, d, e}, frequencyvalue}]
? MapThread
Transpose[{{a, b, c, d, e}, frequencyvalue}]
```

```
Out[334]= {3, 2, 0, 1, 1, 1, 2, 2, 0, 4, 0, 3, 1, 3, 2, 1, 1, 4, 4, 2, 0, 0, 4, 4, 2, 0, 4, 0, 2, 1}
```

```
Out[335]= {d, d, e, b, c, c, b, b, c, c, e, e, e, c, e, d, c, e, b, d, d, e, c, d, a, b, a, e, b, c}
```

```
Out[336]= {e, a, b, e, a, d, c, d, b, c, e, c, b, b, b, e, c, e, c, d, d, e, e, e, c, d, a, e, a, c}
```

expr /. rules applies a rule or list of rules in an attempt to transform each subpart of an expression *expr*. >>

```
Out[338]= {{a, a}, {b, b, b, b, b, b}, {c, c, c, c, c, c, c, c}, {d, d, d, d, d, d}, {e, e, e, e, e, e, e, e}}
```

```
Out[339]= {{a, a}, {b, b, b, b, b, b}, {c, c, c, c, c, c, c, c}, {d, d, d, d, d, d}, {e, e, e, e, e, e, e, e}}
```

```
Out[340]= {2, 6, 8, 6, 8}
```

```
Out[341]= {2, 6, 8, 6, 8}
```

```
Out[342]= {2, 6, 8, 6, 8}
```

```
Out[343]= {{a, 2}, {b, 6}, {c, 8}, {d, 6}, {e, 8}}
```

MapThread[f, {{a₁, a₂, ...}, {b₁, b₂, ...}, ...}] gives *{f[a₁, b₁, ...], f[a₂, b₂, ...], ...}*.
MapThread[f, {expr₁, expr₂, ...}, n] applies *f* to the parts of the *expr_i* at level *n*. >>

```
Out[345]= {{a, 2}, {b, 6}, {c, 8}, {d, 6}, {e, 8}}
```

```
In[346]:= Transpose[{Range[Length[samplelist1]], samplelist1}]
```

```
Out[346]= {{1, 1}, {2, 9}, {3, 4}, {4, 1}, {5, 25}, {6, 36}, {7, 49}, {8, 9}, {9, 1}, {10, 81}}
```

```

In[347]:= MakeADummyCoefficientMatrix[size_] :=
Module[{tmp1 = {}, tmp2 = {}, tmp3 = {}, tmp4 = {}, tmp5 = {}, i = 1, j = 1},
While[i ≤ size, tmp2 = RandomReal[{-1., 1.}], i]; tmp1 = Append[tmp1, tmp2]; i++;
While[j ≤ size, tmp4 = Drop[tmp1, j - 1][[All, j]]; tmp3 = Append[tmp3, Rest[tmp4]]; j++;
tmp5 = MapThread[Join[#1, #2] &, {tmp1, tmp3}];
soukan = ReplacePart[tmp5, 1, Transpose[{Range[size], Range[size]}]]];
MakeADummyCoefficientMatrix[5]
SymmetricalQ[matrix_] := If[Transpose[matrix] == matrix, True, False];
SymmetricalQ[soukan]
SymmetricalQ1[matrix_] := If[MatrixQ[matrix],
If[Transpose[matrix] == matrix, True, False], Print["It is not a matrix."]];
SymmetricalQ1[soukan]
SymmetricalQ1[{1, 2, 3}]

Out[348]= {{1, -0.626117, 0.690885, 0.553006, 0.976262},
{-0.626117, 1, 0.577994, 0.483225, 0.801742}, {0.690885, 0.577994, 1, -0.644286, -0.0500596},
{0.553006, 0.483225, -0.644286, 1, -0.80577}, {0.976262, 0.801742, -0.0500596, -0.80577, 1}}

Out[350]= True

Out[352]= True

It is not a matrix.

In[354]:= ?FoldList
FoldList[Plus, 0, {a, b, c, d, e, f}]

```

FoldList[f, x, {a, b, ...}] gives {x, f[x, a], f[f[x, a], b], ...}. >>

```
Out[355]= {0, a, a + b, a + b + c, a + b + c + d, a + b + c + d + e, a + b + c + d + e + f}
```

```
In[356]:= FoldList[Times, 1, {a, b, c, d, e, f}]
```

```
Out[356]= {1, a, ab, abc, abcd, abcde, abcdef}
```

```

In[357]:= lengths = RandomInteger[{1, 10}, 10]
flist0 = Drop[FoldList[Plus, 0, lengths], 1]
flist1 = Drop[FoldList[Plus, 1, lengths], -1]
possegment = Transpose[{flist1, flist0}]

```

```
Out[357]= {2, 7, 3, 7, 4, 10, 9, 9, 6, 3}
```

```
Out[358]= {2, 9, 12, 19, 23, 33, 42, 51, 57, 60}
```

General::spell1 : New symbol name "flist1" is similar to existing symbol "list1" and may be misspelled. >>

```
Out[359]= {1, 3, 10, 13, 20, 24, 34, 43, 52, 58}
```

```
Out[360]= {{1, 2}, {3, 9}, {10, 12}, {13, 19}, {20, 23}, {24, 33}, {34, 42}, {43, 51}, {52, 57}, {58, 60}}
```