



# Fundamentals of Dynamics (11)

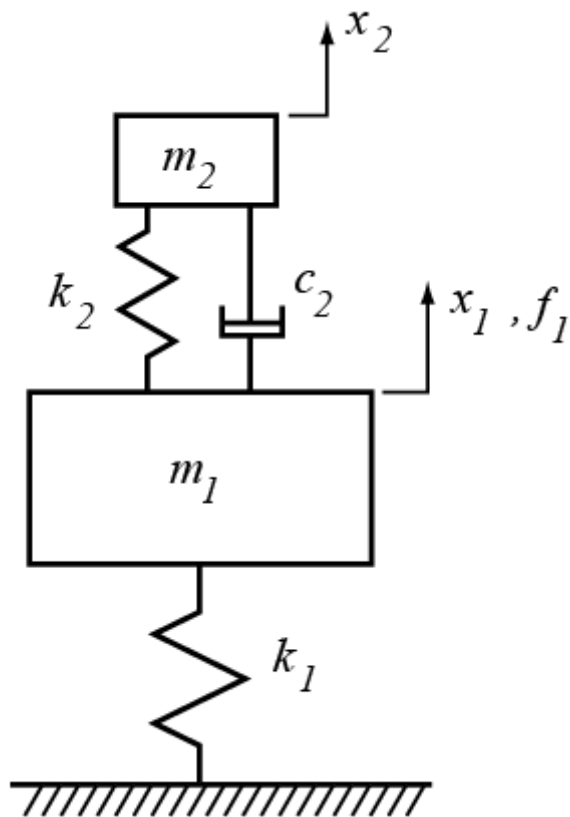
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# Dynamic Absorber

# [ Analytical Model ]



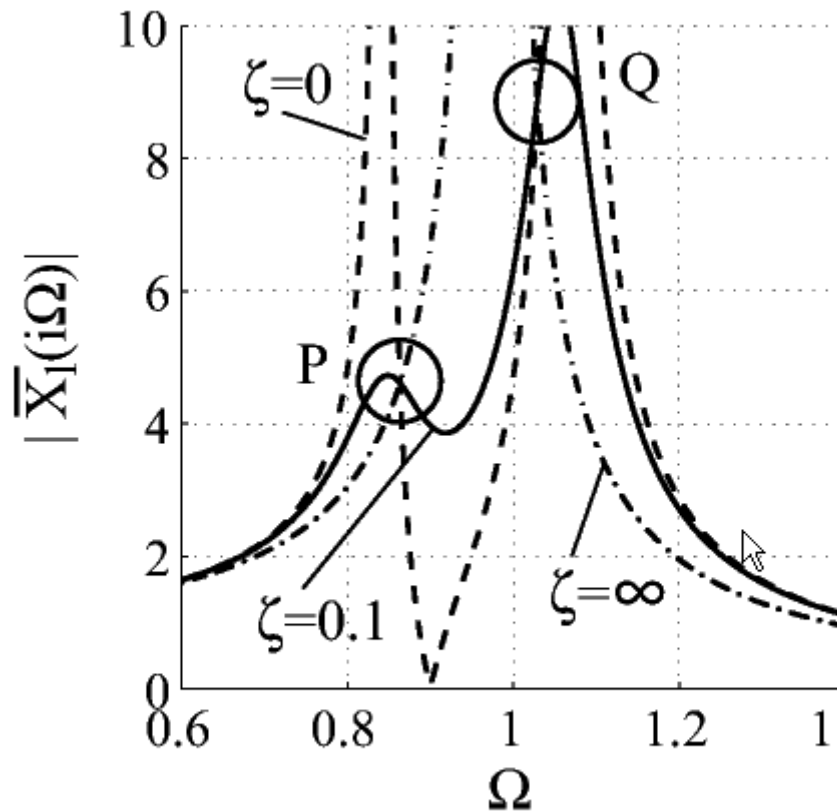
$$m_1 \ddot{x}_1 + c_2(\dot{x}_1 - \dot{x}_2)$$

$$+ k_1 x_1 + k_2(x_1 - x_2) = f_1$$

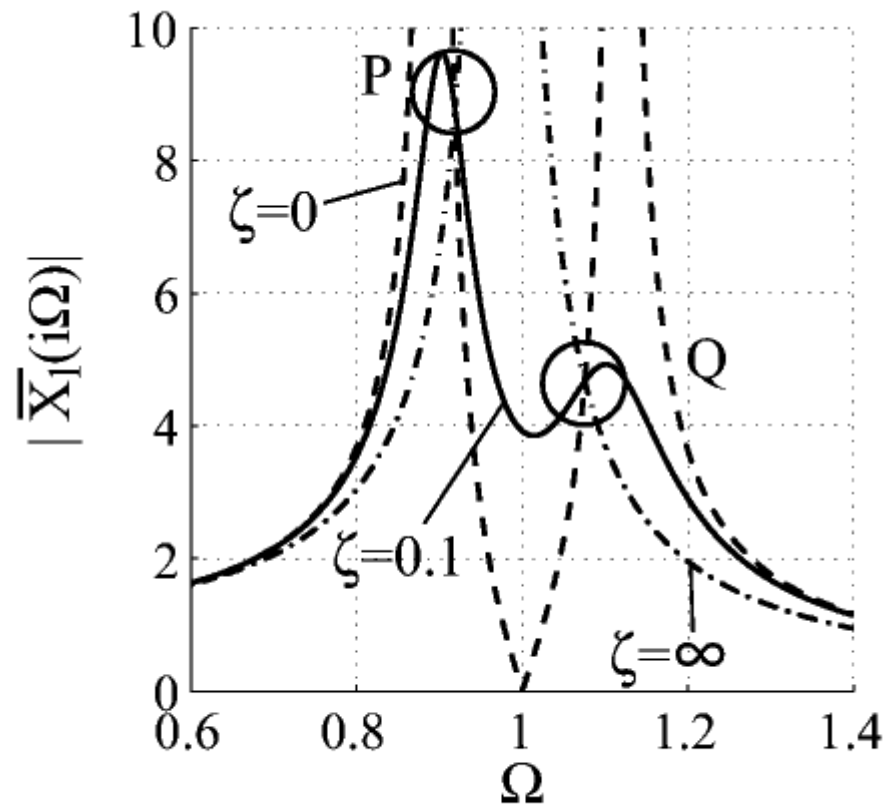
$$m_2 \ddot{x}_2 + c_2(\dot{x}_2 - \dot{x}_1) + k_2(x_2 - x_1) = 0$$

$$\nu \equiv \frac{\omega_2}{\omega_1} = \sqrt{\frac{m_1 k_2}{m_2 k_1}}$$

# Dynamic Amplitude Ratio and Fixed Points



(a)  $\nu = 0.9$



(b)  $\nu = 1.0$

# [Optimal Design]

## Fixed Points Theory

Optimal Tuning for  $k_2$

$$\nu = \frac{1}{1 + \mu} \quad \text{where} \quad \mu \equiv \frac{m_2}{m_1}$$

Best Adjustment for  $c_2$

$$\zeta = \sqrt{\frac{3\mu}{8(1 + \mu)^3}} \quad \text{where} \quad \zeta \equiv \frac{c_2}{2\sqrt{m_2 k_2}}$$