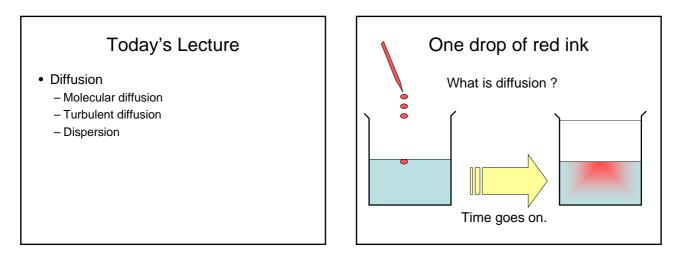
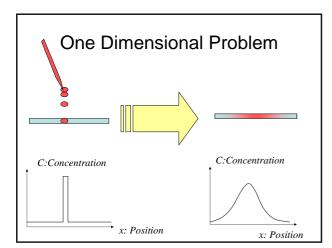
Urban Environmental Engineering 3

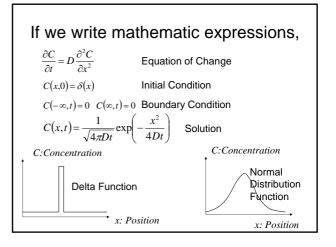
Taro Urase Tokyo Institute of Technology

Lecture in the Last time

- Phenomena taking place in water environment
- Water quality parameters for Organic pollution
 - BOD, COD, TOC
- Streeter Phelps's equation for Change in BOD and DO. > We will discuss this issue in the lecture on reaction kinetics later.



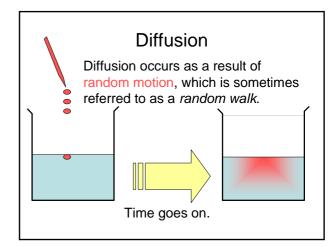




Exercises

$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial x^2}$	Equation of Change (1)
$C(x,0) = \delta(x)$	Initial Condition (2)
$C(-\infty,t)=0$ $C(\infty,t)=0$	Boundary Condition (3)
$C(x,t) = \frac{1}{\sqrt{4\pi Dt}} \exp\left(\frac{1}{\sqrt{4\pi Dt}}\right)$	$-\frac{x^2}{4Dt}$ Solution (4)

Q1: Show that equation (4) is really a solution of equation (1) under the initial condition (2) and the boundary condition (3). Draw the solution graphically with different time elapsed.

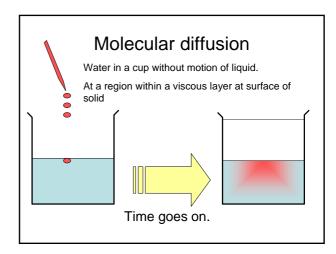


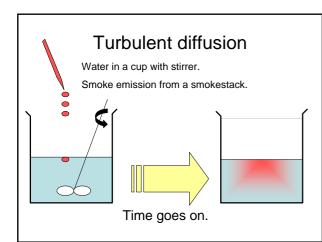
Diffusion

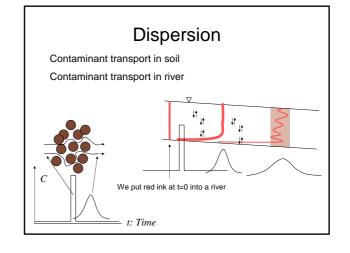
If the random motion is caused by thermodynamic position exchange of molecules, the process is called molecular diffusion.

If the random motion is caused by turbulence, the process is called eddy diffusion or turbulent diffusion.

If the random motion is caused by different flow paths or different velocities in the field, the process is called dispersion.



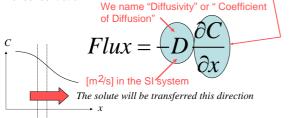


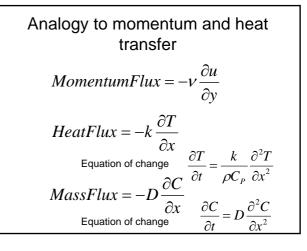


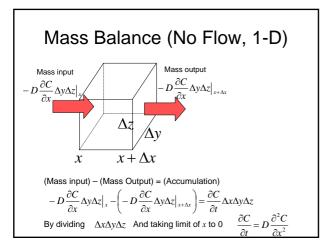
Mass Balance (No Flow, 1-D)

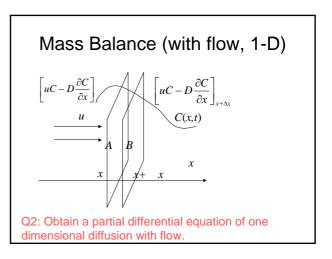
Heat is transferred from a high temperature side to a low temperature side. In the same way, mass is transferred from a high concentration side to a low concentration side.

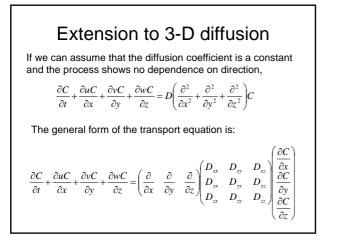
The quantity of the transfer is in proportional to the <u>gradient</u> of concentration.

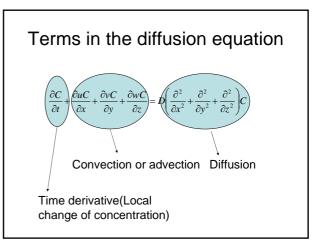


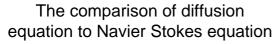




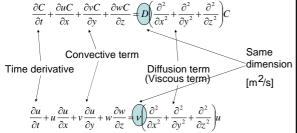








The diffusion equation obtained in the last slide has a similar terms in the Navier Stokes equation $\frac{\partial C}{\partial t} = \frac{\partial t}{\partial t} C + \frac{\partial t}{\partial t$



Diffusion equation for non compressive flow $\frac{\partial C}{\partial t} + \frac{\partial uC}{\partial x} + \frac{\partial vC}{\partial y} + \frac{\partial wC}{\partial z} = D\left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2}\right)C$ Q3: Show that the above equation can be reduced to the following equation in the case of non compressive flow. $\frac{\partial C}{\partial t} + u\frac{\partial C}{\partial x} + v\frac{\partial C}{\partial y} + w\frac{\partial C}{\partial z} = D\left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2}\right)C$

