

2011 1st semester
MIMO Communication Systems

#11: Distributed MIMO Networks

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Schedule (2nd half)

	Date	Text	Contents
#7	May 31	A-5	MIMO receiver
#8	June 7	A-3, 4	MIMO transmitter
#9	June 14	B-9	Adaptive commun. system
#10	June 21	A-6, B-14	Multi-user MIMO
#11	June 28	B-15, 16	Distributed MIMO networks
#12	July 5		Standardization of MIMO
	July 12		Final Examination

Agenda

■ Aim of today

Derive throughput performances
of wireless networks with MIMO technology

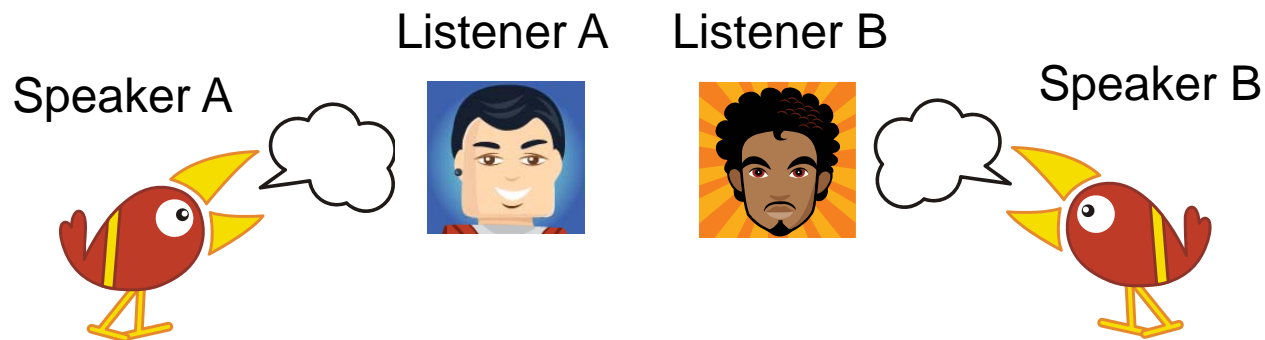
■ Contents

- Classification of wireless networks
- Wide zone
- Cellular networks
 - Base station cooperation MIMO
- Multi-hop networks
 - Two-way MIMO multi-hop relay

Warming Up

■ Question

Consider a scenario where speakers A&B are speaking to listeners A&B. Classify the scenario into four cases & give features of each case.



Case A

Speakers A&B speak independent contents at the same time.

?

Case B

Speakers A&B speak independent contents alternately.

?

Case C

Listeners A&B have special ears to perform MIMO-MA.

?

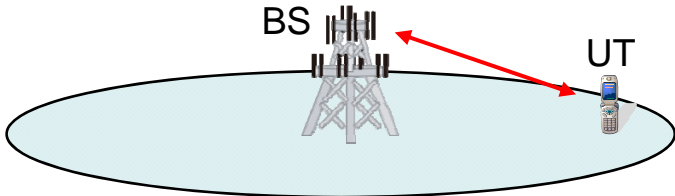
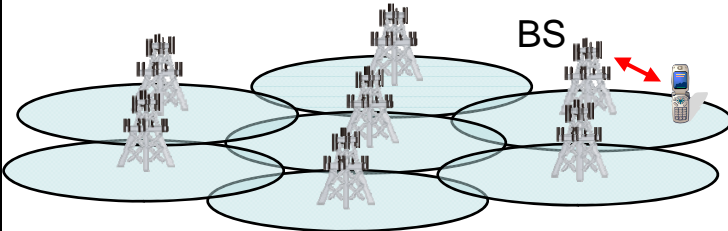
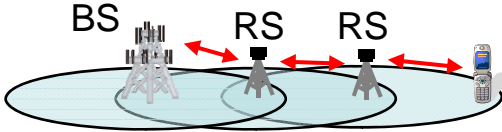
Case D

Speakers A&B cooperatively speak to perform MIMO-BC.

?

Classification of Wireless Networks

Wireless networks to achieve wide area coverage

	Architecture	System throughput	Drawbacks
Wide zone		Low	High power
Cellular network		High	Cost of base stations & backbone networks
Multi-hop network		Medium	Cost of relay stations

Wide Zone

SISO capacity

$$C = \log_2(1 + \gamma) \quad \gamma = \frac{|h|^2 P_{\text{SZ}}}{\sigma^2}$$

Path loss model

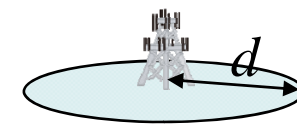
$$L_{\text{SZ}}^{\text{db}} = 10 \log_{10} \left(E[|h|^2] \right) = -34.5 - 35 \log_{10} d$$

$$L_{\text{WZ}}^{\text{db}} = -34.5 - 35 \log_{10} d - 35 \log_{10} \alpha$$

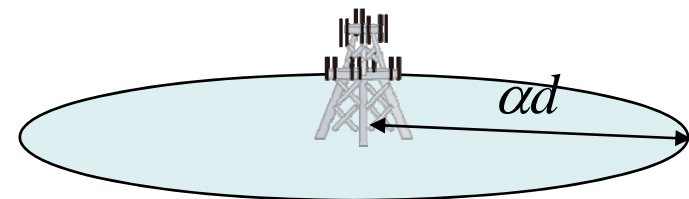
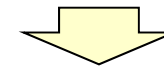
Required power

$$P_{\text{WZ}}^{\text{db}} = P_{\text{SZ}}^{\text{db}} + 35 \log_{10} \alpha$$

Ex. $\alpha = 10$ $P_{\text{SZ}} = 1 [\text{W}] \rightarrow P_{\text{WZ}} = 3 [\text{kW}]$



Small zone



Wide zone

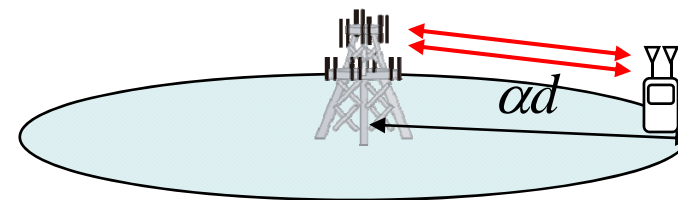
Wide Zone with MIMO

MIMO capacity

$$C_{\text{MIMO}} \cong MC_{\text{SISO}} \quad \text{if } \gamma \gg 1$$

Rank of MIMO channel

$$= \log_2(1 + \gamma)^M \cong \log_2(\gamma^M)$$



Wide zone with MIMO

Required power

$$\gamma_{\text{SZ}}^{\text{dB}} = P_{\text{SZ}}^{\text{dB}} - 34.5 - 35 \log_{10} d - 10 \log_{10} \sigma^2$$

$$\gamma_{\text{wzMIMO}}^{\text{db}} = M \left(P_{\text{wz}}^{\text{dB}} - 34.5 - 35 \log_{10} d - 35 \log_{10} \alpha - 10 \log_{10} \sigma^2 \right)$$

$$= M \left(\gamma_{\text{SZ}}^{\text{dB}} \right) - 35M \log_{10} \alpha + MP_+^{\text{dB}} \quad \longleftarrow \quad P_{\text{wz}}^{\text{db}} = P_{\text{SZ}}^{\text{db}} + P_+^{\text{db}}$$

$$P_+^{\text{dB}} = 35 \log_{10} \alpha - \gamma_{\text{SZ}}^{\text{dB}} \left(1 - \frac{1}{M} \right)$$

Ex. $\alpha = 10 \quad M = 2$
 $P_{\text{SZ}} = 1 [\text{W}] \rightarrow P_{\text{wz}} = 317 [\text{W}]$

Cellular Network

System capacity

$$C_{\text{sys}} \cong N_{\text{BS}} C$$

Number of BSs

Single cell capacity

Required cost

$$Y_{\text{cell}} \cong N_{\text{BS}} Y_{\text{sz}} + Y_{\text{bb}}$$

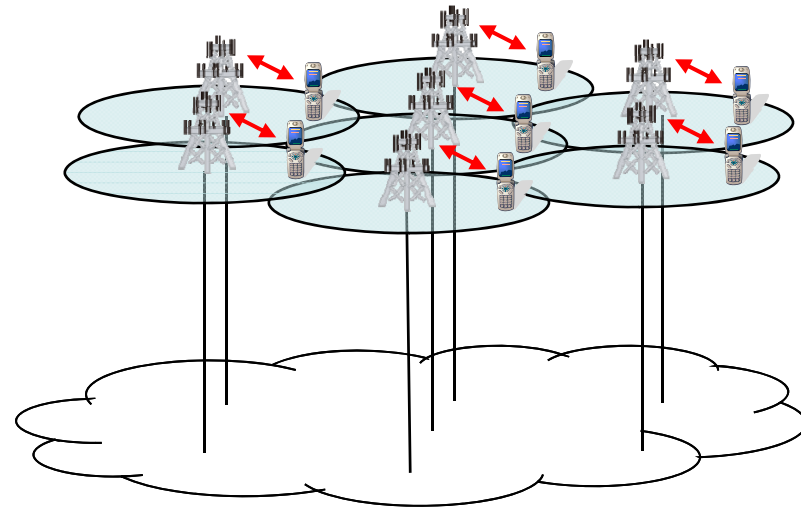
Cost of single BS

Cost of backbone



Problem of co-channel interference

Wireless Cellular network



High speed backbone network

Co-channel Interference & Frequency Reuse

Signal model

$$y_1 = h_1 s_1 + h_2 s_2 + n_1$$

Single frequency network

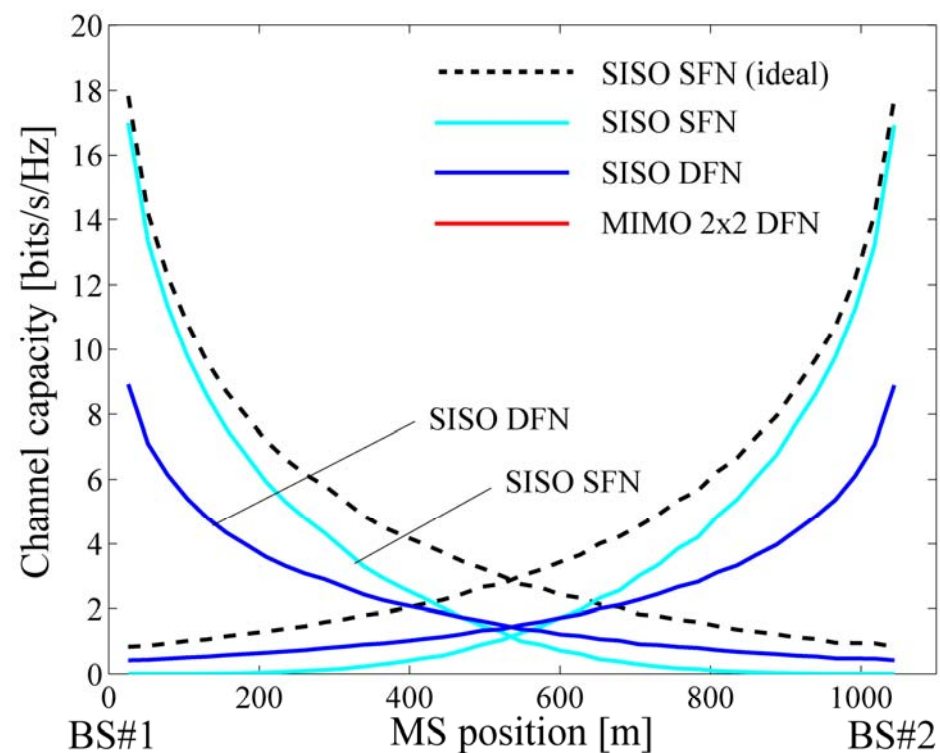
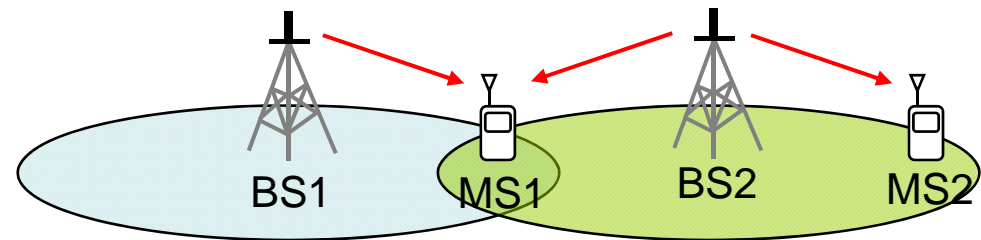
$$C_s = \log_2 \left(1 + \frac{P_1 |h_1|^2}{P_2 |h_2|^2 + \sigma^2} \right)$$

Dual frequency network

Frequency reuse factor = 2

$$C_D = \frac{1}{2} \log_2 \left(1 + \frac{P_1 |h_1|^2}{\sigma^2} \right)$$

Loss of channelization



Cellular Network with MIMO

Signal model

$$\mathbf{y}_1 = \mathbf{H}_1(f_1)\mathbf{s}_1 + \mathbf{n}_1$$

$$\mathbf{y}_2 = \mathbf{H}_2(f_2)\mathbf{s}_2 + \mathbf{n}_2$$

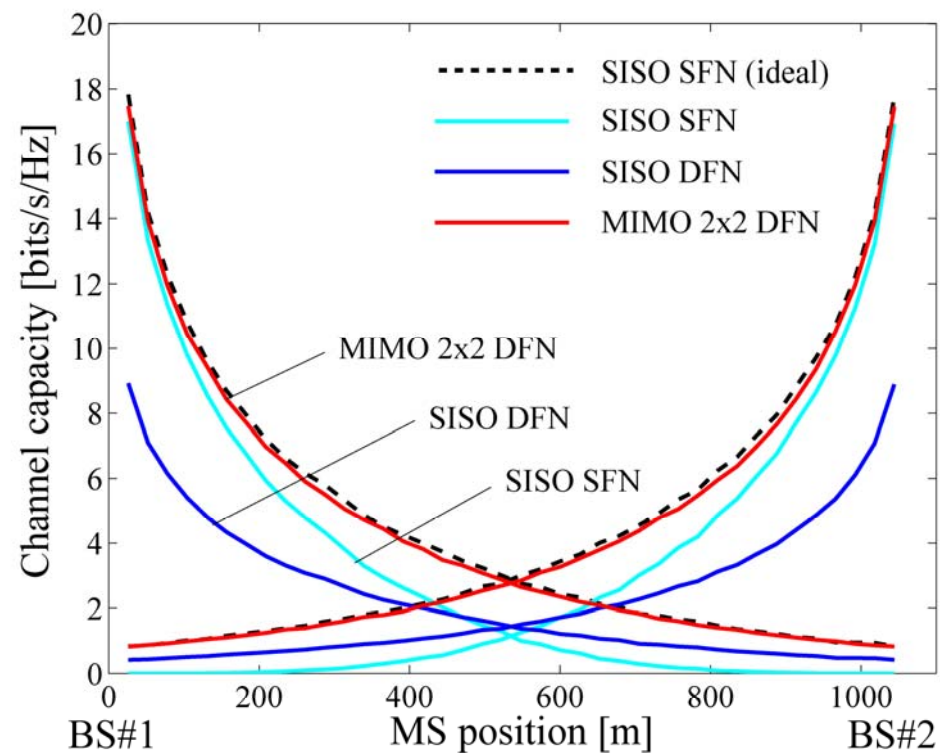
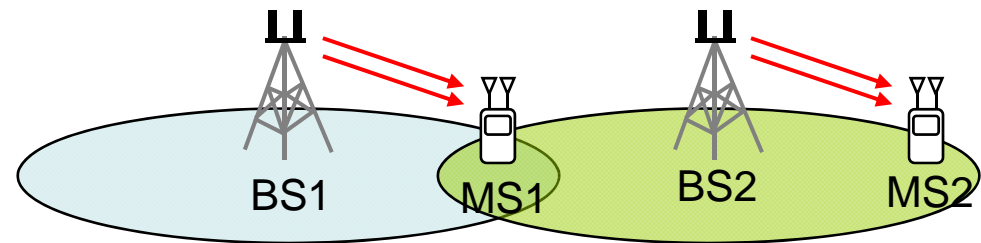
MIMO capacity

$$C_1 = \frac{1}{2} \log_2 \det \left(\mathbf{I} + \frac{P\mathbf{H}_1\mathbf{H}_1^H}{M_{\text{BS}}\sigma^2} \right)$$

Number of BS antennas



Ideal SISO SFN = MIMO DFN



Eigenmode Analysis of Cellular MIMO

Eigenmode decomposition

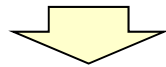
$$\mathbf{H} = \mathbf{U}\mathbf{\Lambda}\mathbf{V}^H$$

$$\mathbf{\Lambda} = \text{diag}[\sqrt{\lambda_1}, \dots, \sqrt{\lambda_M}]$$

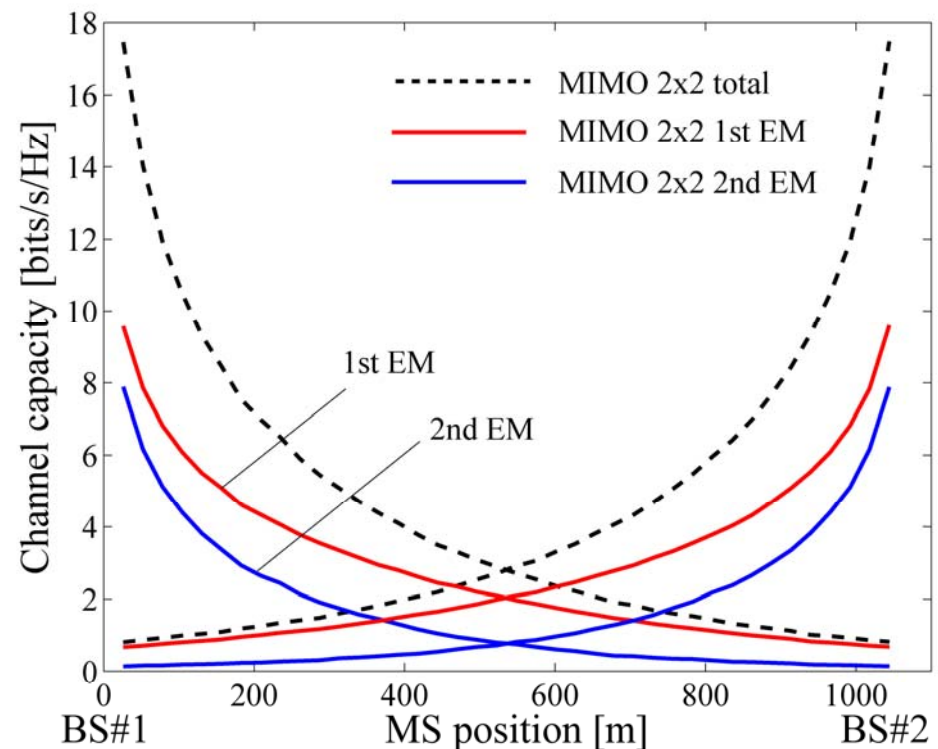
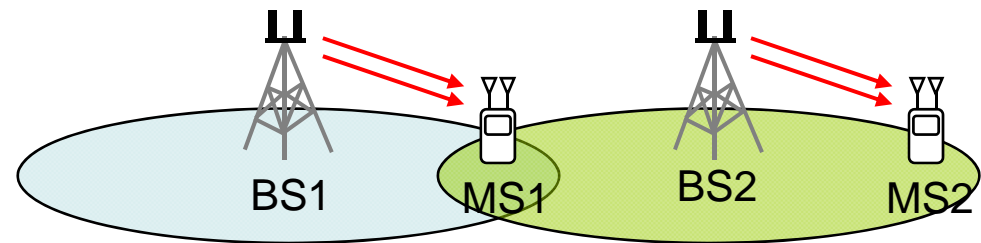
MIMO capacity

$$C = \sum_{i=1}^M C_i^{\text{em}}$$

$$C_i^{\text{em}} = \frac{1}{2} \log_2 \left(1 + \frac{P\lambda_i}{M\sigma^2} \right)$$



2nd EM vanishes at cell edge



Cellular Network with Terminal Adaptive Array

Signal model

$$\mathbf{y}_1 = \mathbf{h}_1 s_1 + \mathbf{h}_2 s_2 + \mathbf{n}_1$$

Interference from BS2

Terminal adaptive array

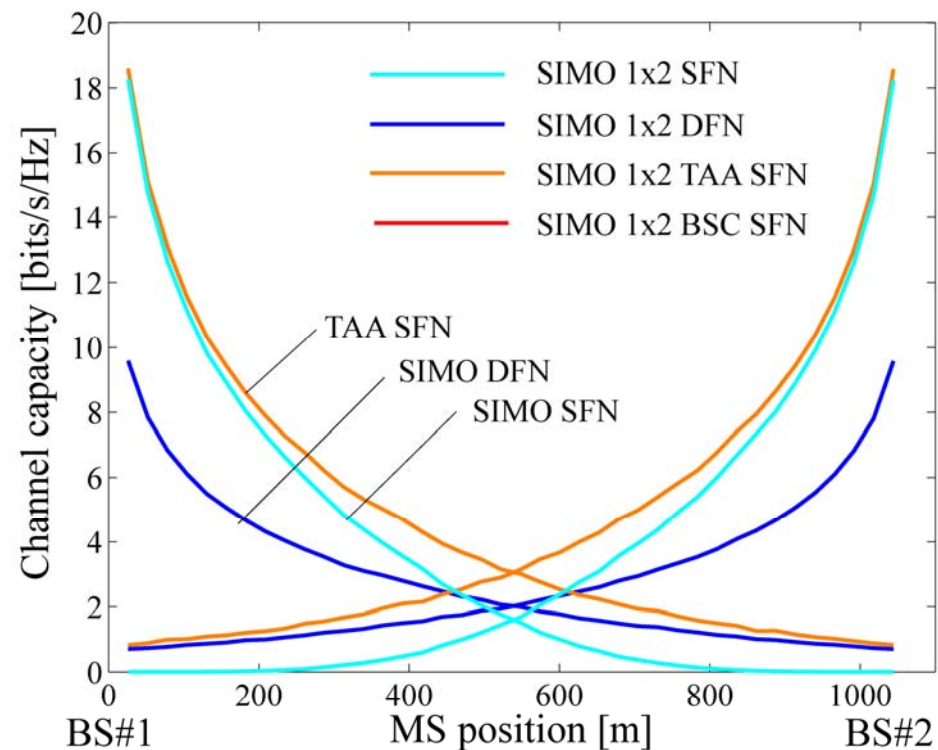
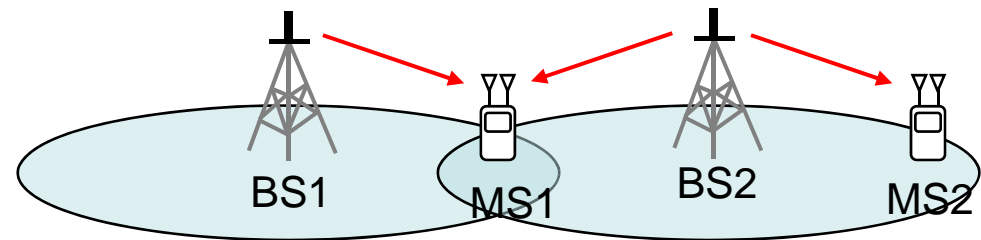
$$\mathbf{w}_1^r = (\mathbf{h}_2)^\perp, \quad \mathbf{w}_2^r = (\mathbf{h}_1)^\perp$$

Interference cancellation

$$\tilde{\mathbf{y}}_1 = (\mathbf{w}_1^r) \mathbf{y}_1 = h_1^e s_1 + \tilde{\mathbf{n}}_1$$



Almost same with MIMO DFN



Cellular Network with Base Station Cooperation MIMO

Signal model

$$\begin{aligned}\mathbf{y} &= \mathbf{h}_1 s_1 + \mathbf{h}_2 s_2 + \mathbf{n} \\ &= \begin{bmatrix} \mathbf{h}_1 & \mathbf{h}_2 \end{bmatrix} \begin{bmatrix} s_1 \\ s_2 \end{bmatrix} + \mathbf{n}_1\end{aligned}$$

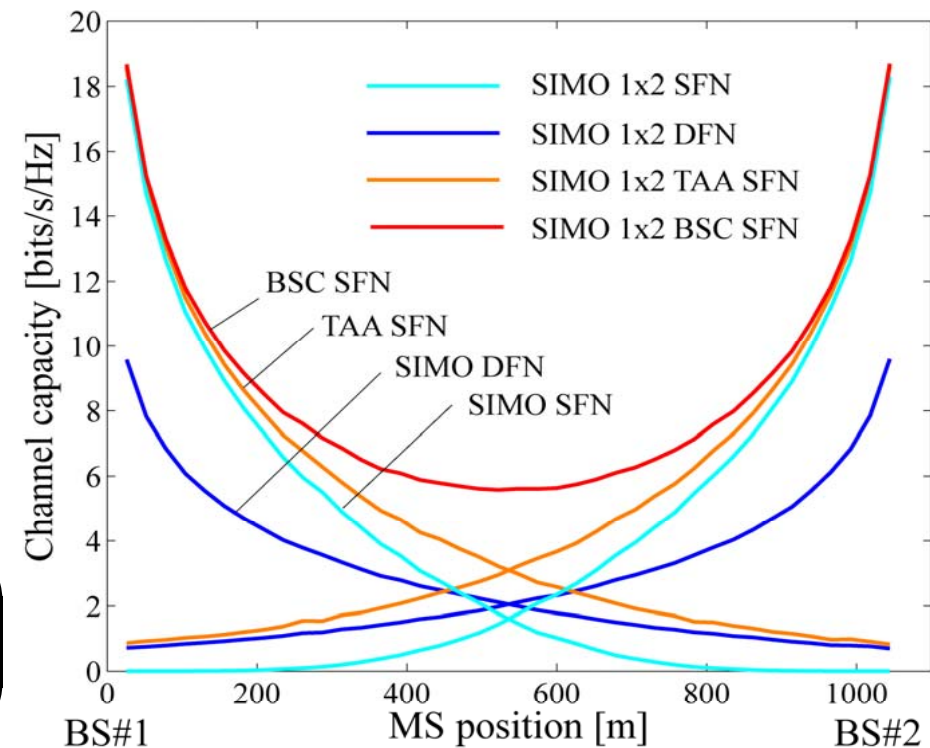
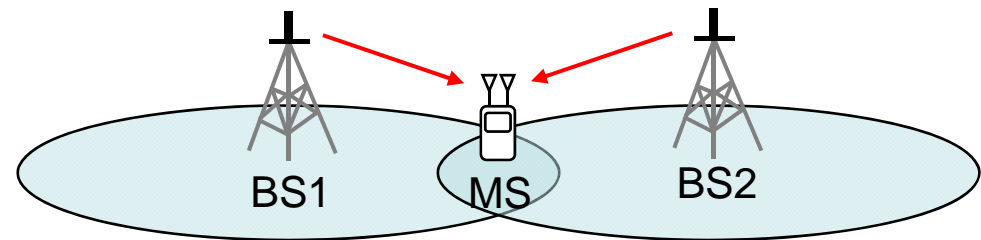
Cooperative MIMO channel

$$\mathbf{H} = \begin{bmatrix} \mathbf{h}_1 & \mathbf{h}_2 \end{bmatrix}$$

$$M = \min[N_{\text{BS}} M_{\text{BS}}, M_{\text{MS}}]$$

BSC MIMO capacity

$$C_{\text{BSC}} = \log_2 \det \left(\mathbf{I} + \frac{N_{\text{BS}} P \mathbf{H} \mathbf{H}^H}{M_{\text{MS}} \sigma^2} \right)$$



Eigenmode Analysis of Base Station Cooperation MIMO

Eigenmode decomposition

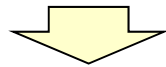
$$\mathbf{H} = [\mathbf{h}_1 \quad \mathbf{h}_2] = \mathbf{U}\mathbf{\Sigma}\mathbf{V}^H$$

$$\mathbf{\Lambda} = \text{diag}[\sqrt{\lambda_1}, \dots, \sqrt{\lambda_M}]$$

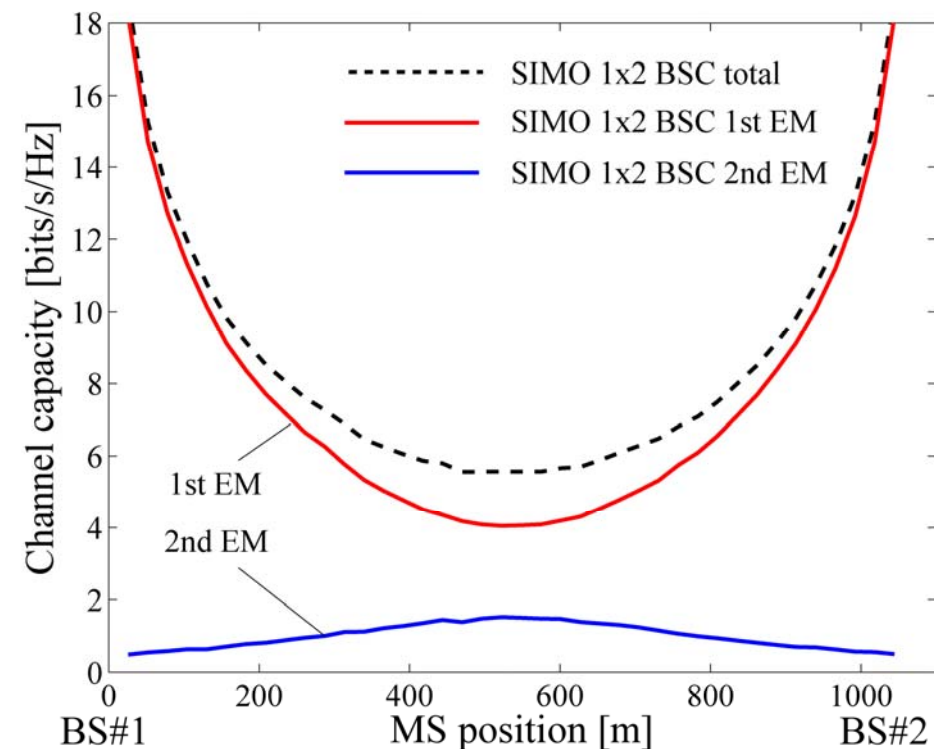
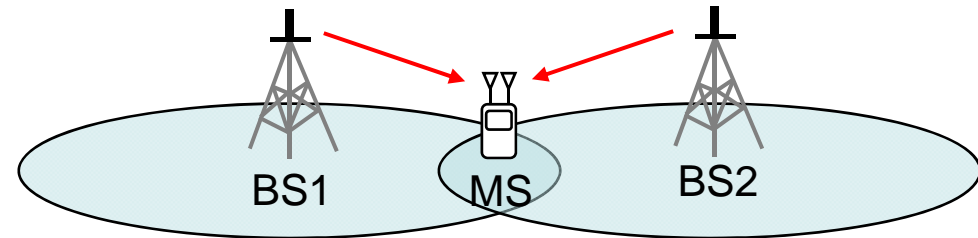
MIMO capacity

$$C = \sum_{i=1}^M C_i^{\text{em}}$$

$$C_i^{\text{em}} = \frac{1}{2} \log_2 \left(1 + \frac{P\lambda_i}{M\sigma^2} \right)$$



2nd EM is effective at cell edge



Hybrid Normal MIMO & Base Station Cooperation MIMO

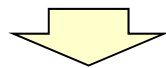
Signal model

$$\mathbf{y} = \mathbf{H}_1 \mathbf{s}_1 + \mathbf{H}_2 \mathbf{s}_2 + \mathbf{n}$$

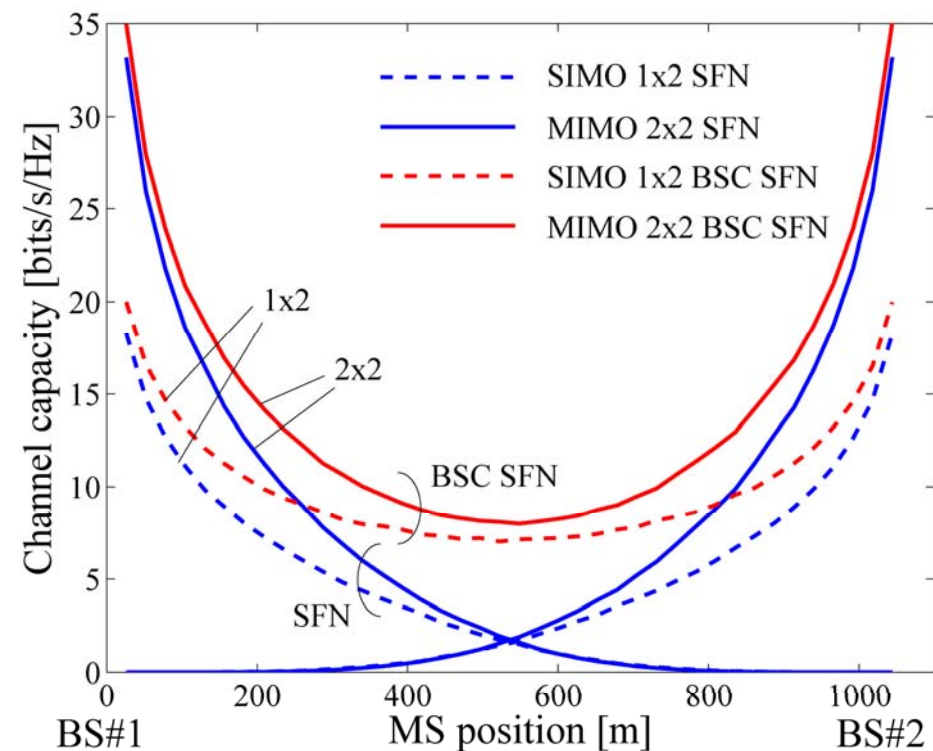
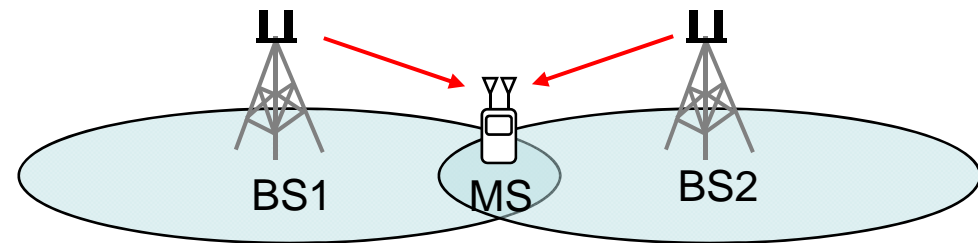
$$= \begin{bmatrix} \mathbf{H}_1 & \mathbf{H}_2 \end{bmatrix} \begin{bmatrix} \mathbf{s}_1 \\ \mathbf{s}_2 \end{bmatrix} + \mathbf{n}$$

BSC MIMO capacity

$$C_{\text{BSC}} = \log_2 \det \left(\mathbf{I} + \frac{N_{\text{BS}} \mathbf{P} \mathbf{H} \mathbf{H}^H}{M_{\text{MS}} \sigma^2} \right)$$



- Normal MIMO at cell center
- Cooperation MIMO at cell edge



Multi-hop Relay Network

End-to-end capacity

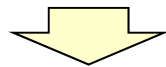
$$C_{mh} \cong \frac{1}{2} C_{sz}$$

Loss of half duplex

Required cost

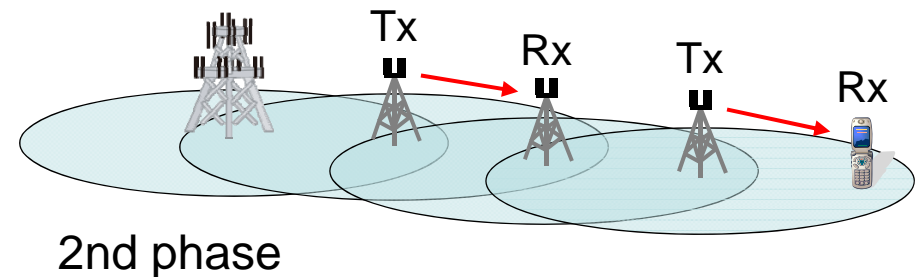
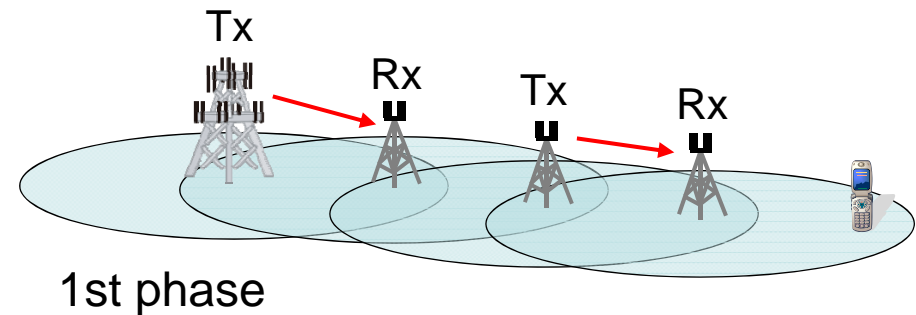
$$Y_{mh} \cong (N_{RS} + 1) Y_{sz}$$

Number of relay stations



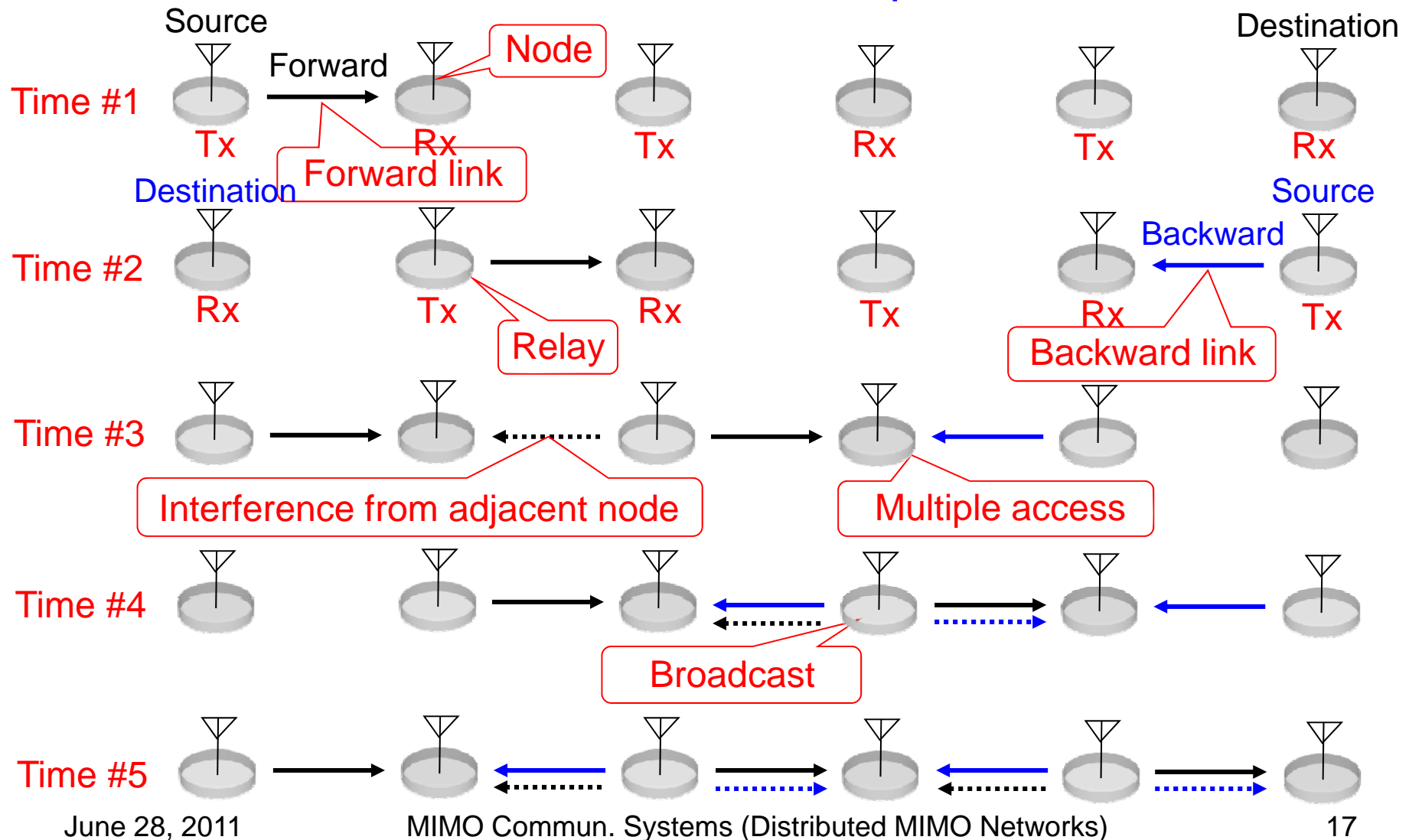
Problem of co-channel interference

Half duplex multi-hop network



Technology in multi-hop network

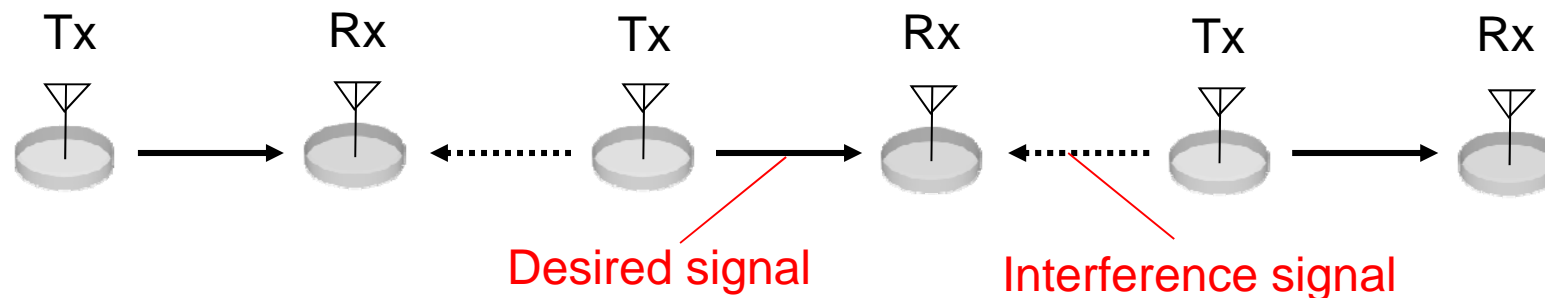
1-dimensional 6-node wireless multi-hop network



Multi-hop Relay with Frequency Reuse

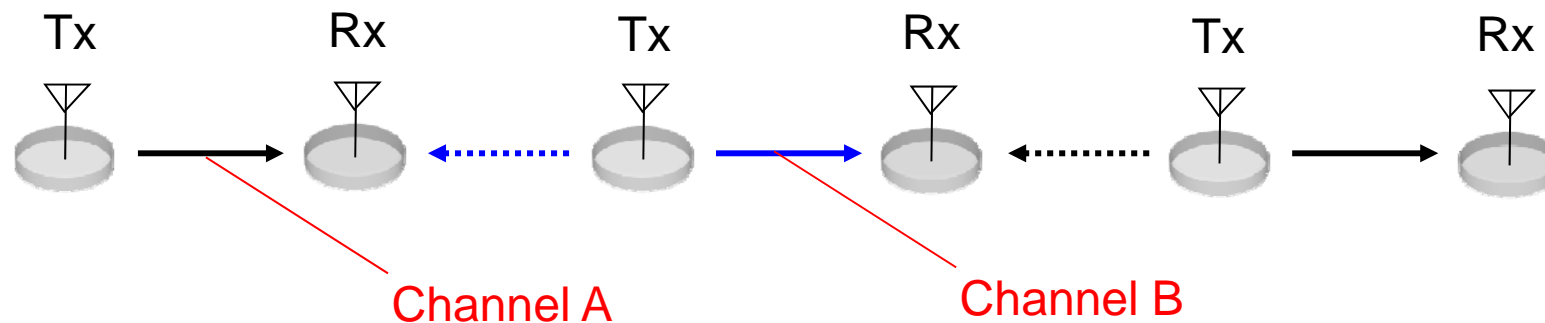
Single channel multi-hop network

Interference from adjacent node is severe



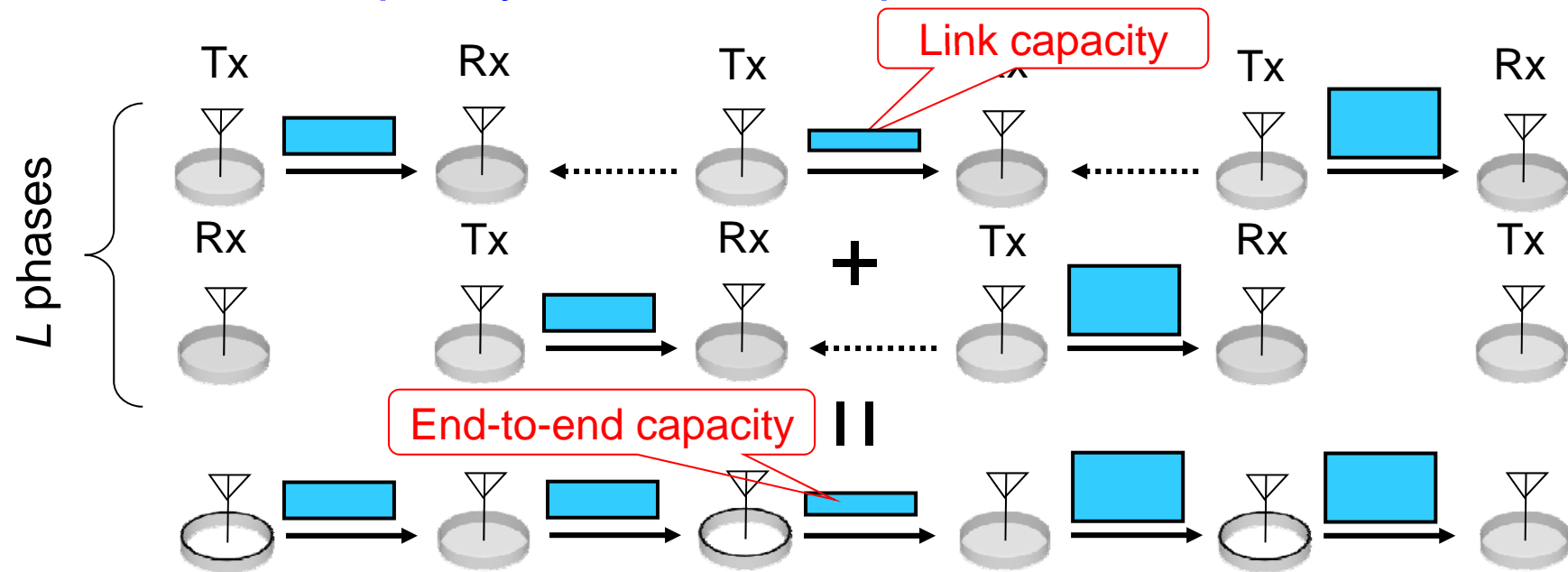
Multi channel multi-hop network

Channelization loss of 1/2



End-to-end capacity

End-to-end capacity for decode, spool, and forward network



• Link capacity

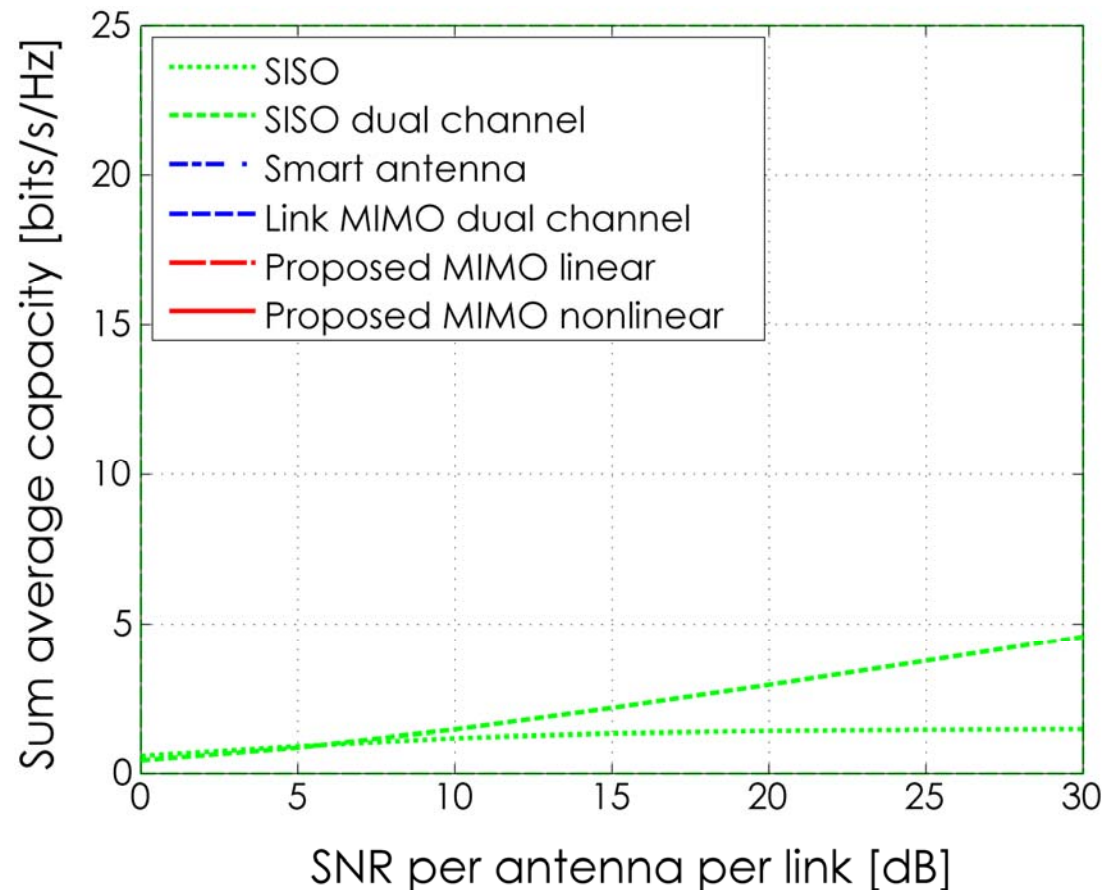
$$C_i^{\text{av}} = \mathbb{E} \left[\log_2 \left[1 + \frac{P_i g_{(i+1)i}}{\sum_{j \neq i} P_j g_{(i+1)j} + \sigma^2} \right] \right]$$

• End-to-end capacity

$$C_i^{\text{av}} = \min \left[\frac{1}{L} C_i^{\text{av}} \right]$$

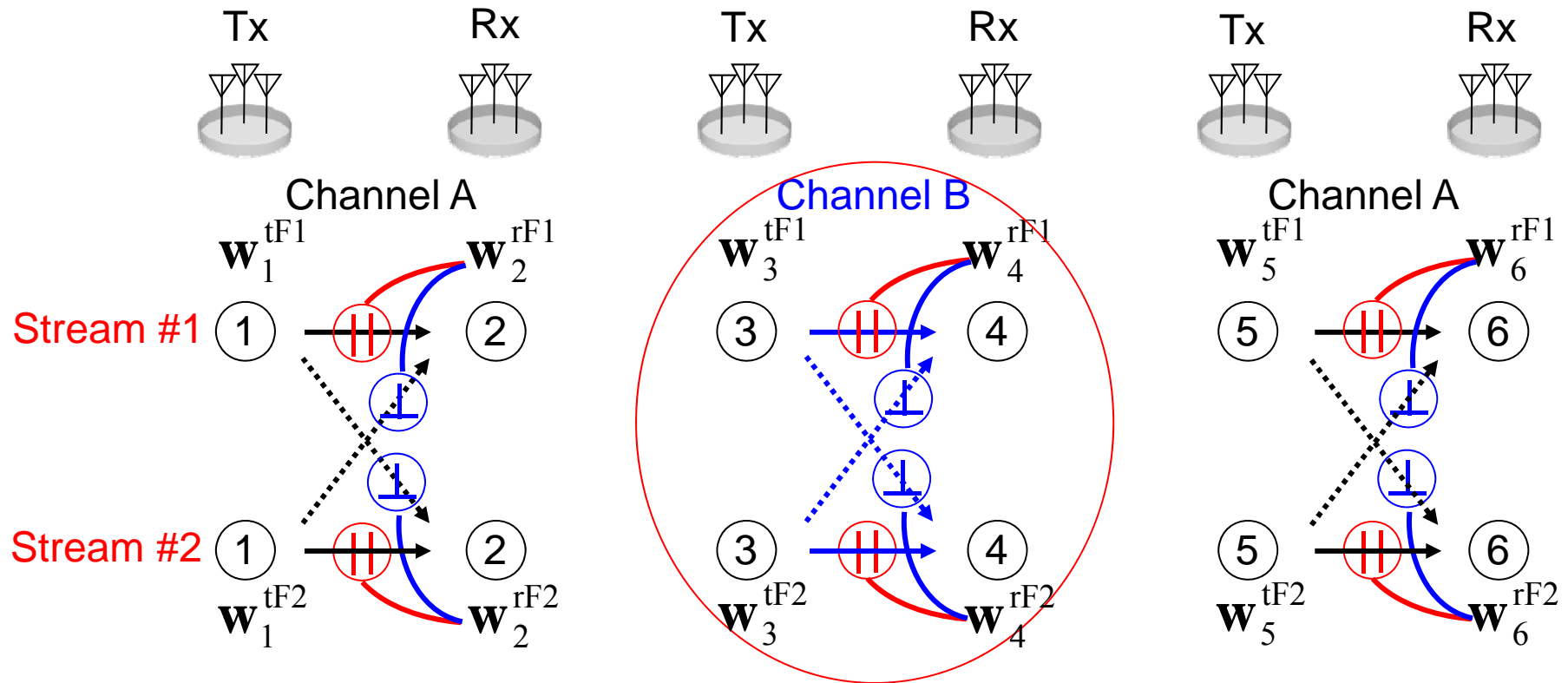
E2E throughput performance

- Negligible throughput of single channel multi-hop network due to strong interference from adjacent node
- Introduction of multi-channel strategy improves the throughput performance



Multi-hop Relay with MIMO

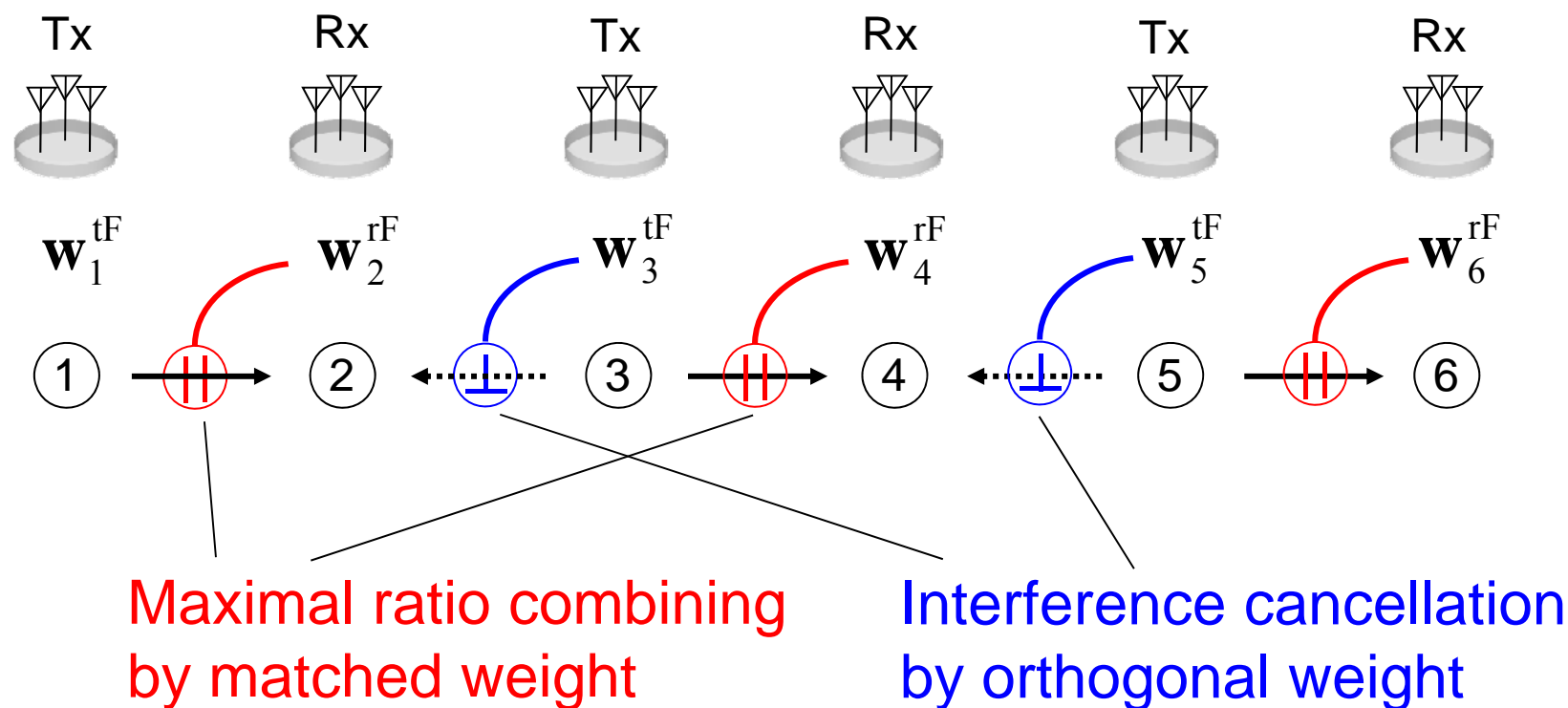
- Increase spectral efficiency by spatial multiplexing within a link
- Recover the disadvantage of multi-channel networks



MIMO spatial multiplexing

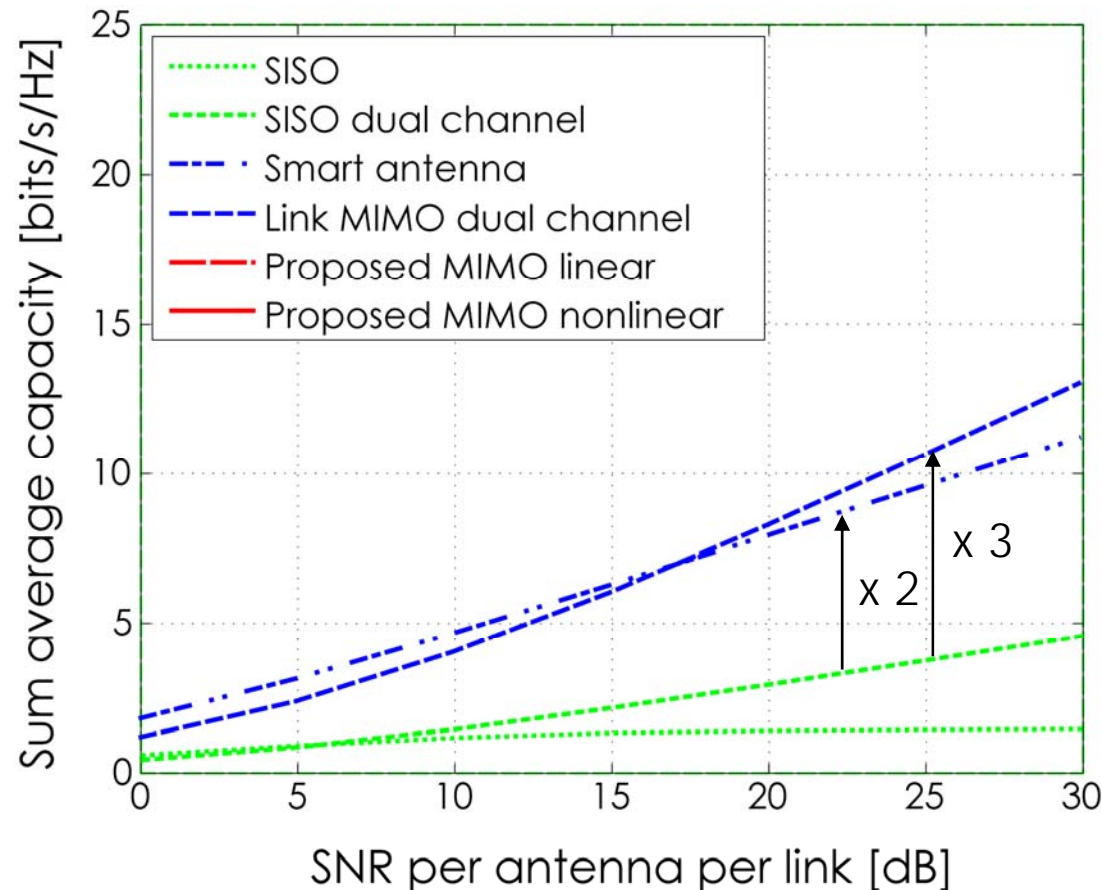
Multi-hop Relay with Adaptive Array

- Achieve transmit & receive interference cancellation and diversity
- Realize single channel multi-hop network



E2E throughput performance

- Throughput performance of link-by-link MIMO scales linearly with respect to the number of antennas per node
- Introduction of adaptive antenna compensates the channelization loss

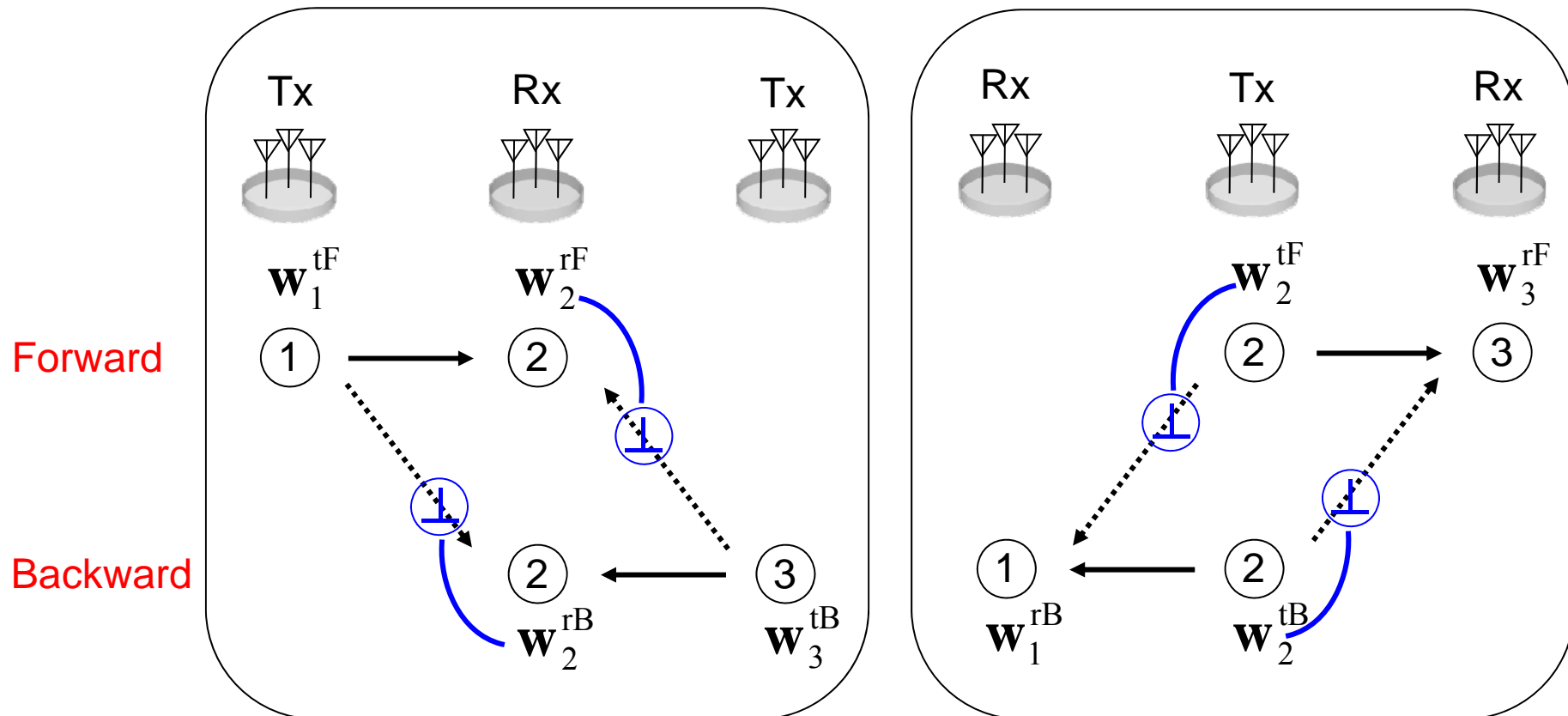


Two-way MIMO Relay (Two-hop)

- Two-way streams (forward & backward) are multiplexed in a relay network
- Recover the loss of half duplex by two-way multiplexing

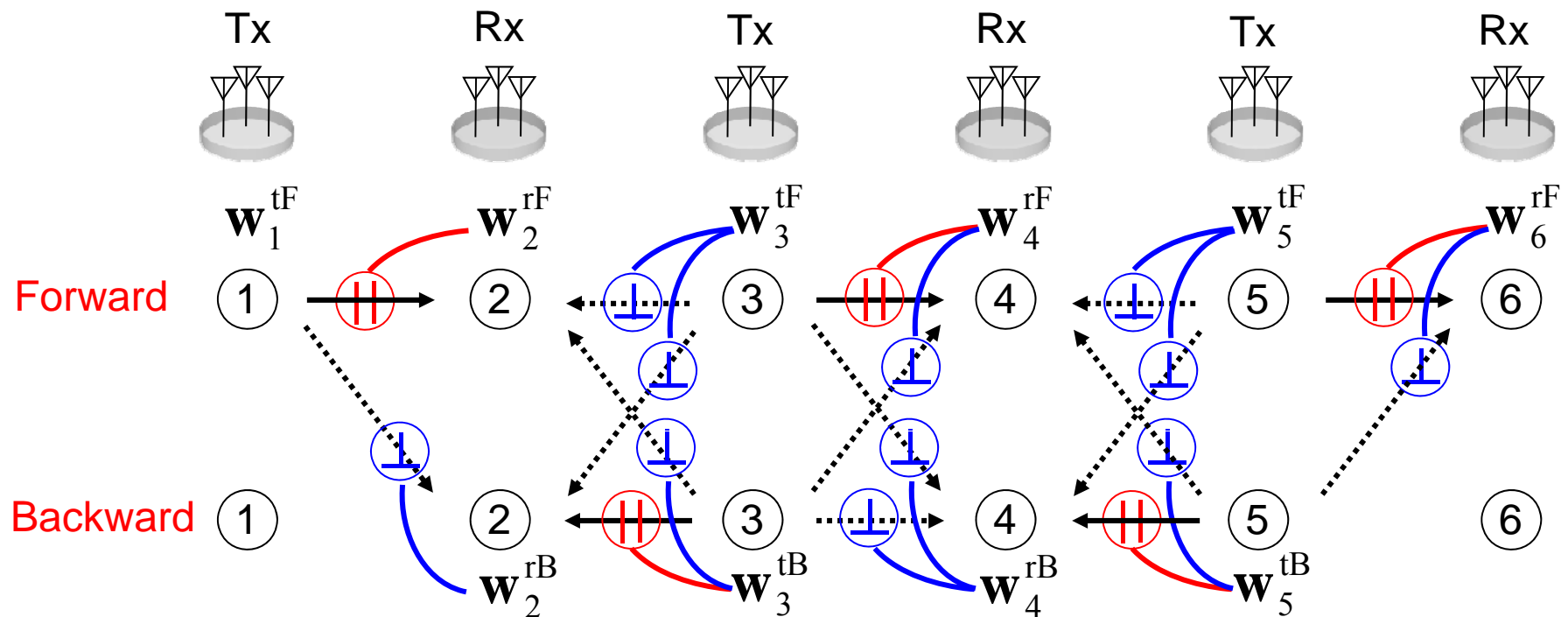
Phase 1 (multiple access)

Phase 2 (broadcast)



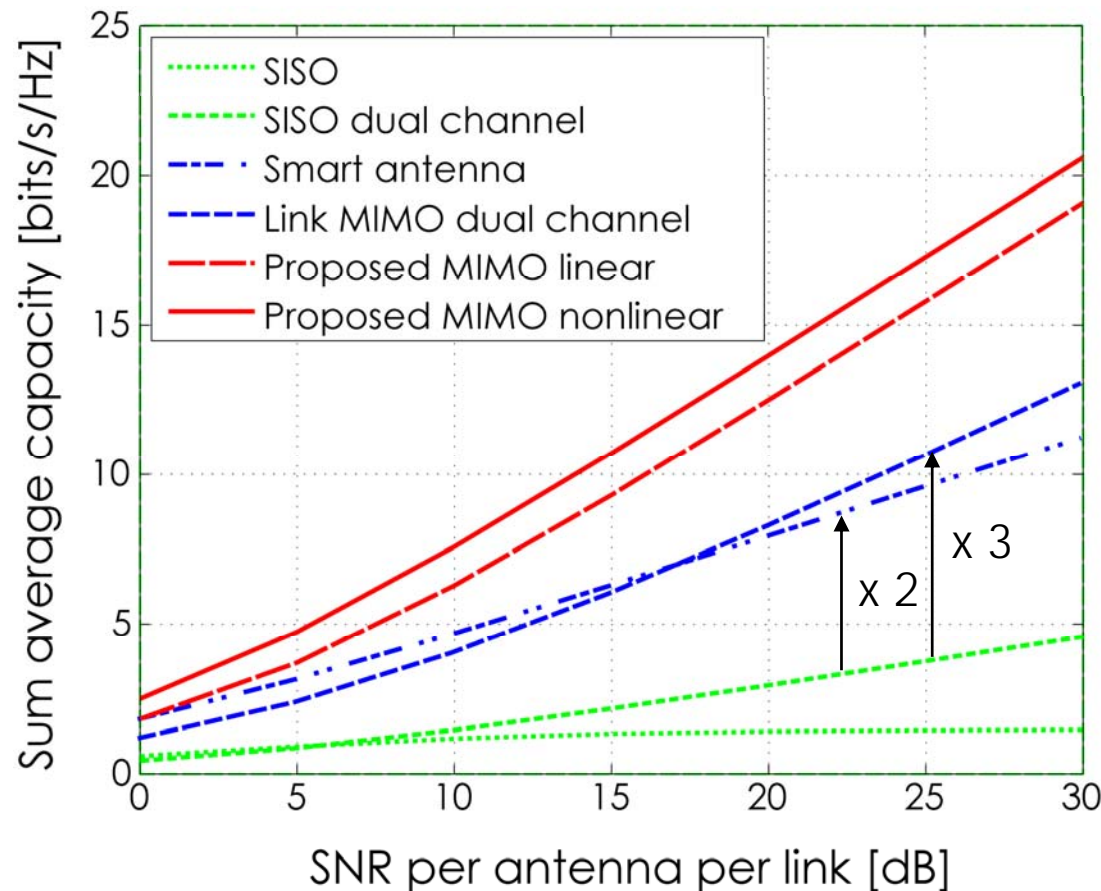
Two-way MIMO Multi-hop Relay

- Two-way transmission by spatial multiplexing of forward & backward streams
- Network oriented interference cancellation by a combination of transmit & receive weights
- Simultaneous realization of diversity, transmit & receive interference cancellation, and spatial multiplexing



E2E throughput performance

- Throughput performance of two-way MIMO multi-hop network is the best
- 2-times improvement due to realization of single channel network and further 2-times improvement due to two-way streams multiplexing



Multi-flow Multi-hop Relay Network

Network capacity

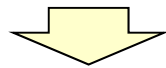
$$C_{\text{mfmh}} \cong N_{\text{flow}} C_{\text{twmh}}$$

Number of flows

E2E capacity of two-way
multi-hop network

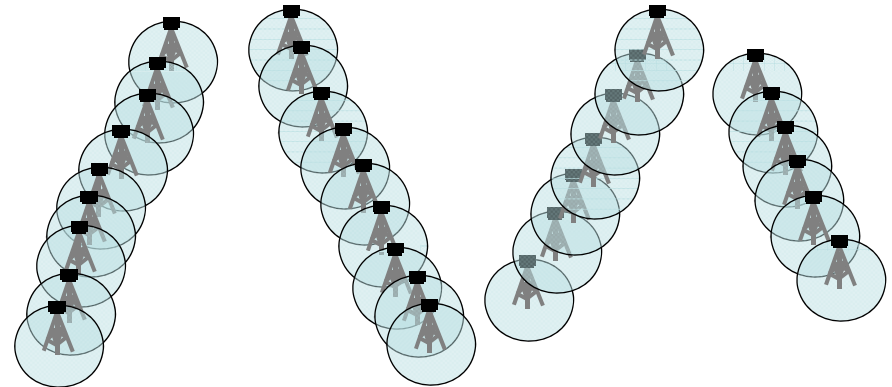
Required cost

$$Y_{\text{mfmh}} \cong N_{\text{flow}} (N_{\text{RS}} + 1) Y_{\text{sz}}$$



Effective for local networks

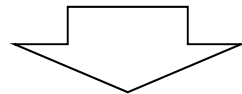
Co-existence of
several flows of multi-hop network



Power reduced multi-hop networks

Summary

- Distributed MIMO networks
 - Wireless networks to achieve wide area coverage
 - Wide zone, cellular networks, multi-hop networks
 - Link-by-link application of single user MIMO is not efficient
 - Base station cooperation MIMO cellular network
 - Cooperative MIMO to achieve better performance at cell edge
 - Two-way MIMO multi-hop relay
 - Network MIMO to achieve single channel two-way relay



Application of MIMO technology to commercial products

Standardization of MIMO in IEEE & 3GPP