

Diamagnetism of an atom

Unpaired electrons → rotation around atomic orbitals

$$I = (-Ze) \left(\frac{1}{2\pi} \frac{eB}{m} \right) \frac{1}{2}$$

charge cyclotron frequency ω_c

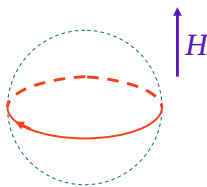
(magnetic moment) = $I \times (\text{area})$

$$\mu = -\frac{Ze^2 B}{4m} \langle x^2 + y^2 \rangle = -\frac{Ze^2 B}{6m} \langle r^2 \rangle$$

よって

$$\chi = \frac{N\mu}{B} = -\frac{NZe^2}{6m} \langle r^2 \rangle \quad \text{diamagnetism of an atom } \chi < 0$$

Given by the sum of the atomic Pascal diamagnetism.



Curie paramagnetism

Magnetic moment from an unpaired electron

$$\mu = \gamma \hbar S = -g \mu_B S$$

Zeemann splitting under the magnetic field, H

$$E = -g \mu_B H S = -\mu H$$

Split to two at $S=1/2$. The thermal distribution is

$$\frac{N_{\uparrow}}{N} = \frac{e^{\mu H / k_B T}}{e^{\mu H / k_B T} + e^{-\mu H / k_B T}} \quad \frac{N_{\downarrow}}{N} = \frac{e^{-\mu H / k_B T}}{e^{\mu H / k_B T} + e^{-\mu H / k_B T}}$$

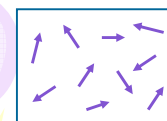
gives

$$M = \mu_B (N_{\uparrow} - N_{\downarrow}) = N\mu \tanh \frac{\mu H}{k_B T} \approx N\mu \left(\frac{\mu H}{k_B T} \right) \leftarrow \frac{\mu H}{k_B T} \ll 1$$

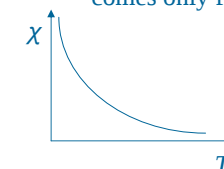
$$\chi = \frac{M}{H} = \frac{N\mu^2}{k_B T} = \frac{C}{T} \quad \text{Curie constant} \quad \text{For } S \neq 1/2 \quad C = \frac{NS(S+1)g^2 \mu_B^2}{3k_B}$$

χ is inversely proportional to T .

comes only from S .



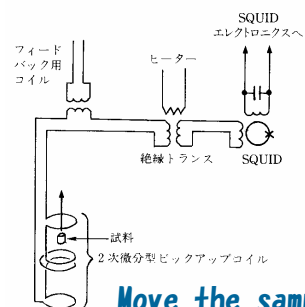
Random spins
Aligned under magnetic field.
More easily aligned
at low temperatures.



磁化測定: SQUID Superconductor Quantum Interference Device

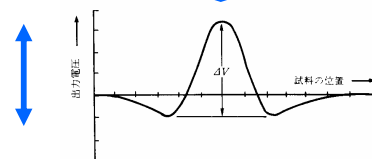


Measure magnetization M at $rt \sim 1.5$ K
several ten μ g sample



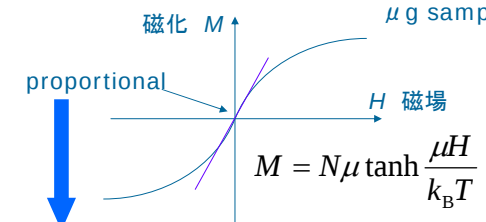
Move the sample by 10 cm
up and down.

磁化 M



磁化測定: SQUID Superconductor Quantum Interference Device

Measure magnetization M at $rt \sim 1.5$ K
several ten μ g sample



磁化率 $\chi = M/H$
Curie paramagnetism
 $\chi \propto 1/T > 0$
 $\chi = 10^{-3}$ emu/mol

Metals

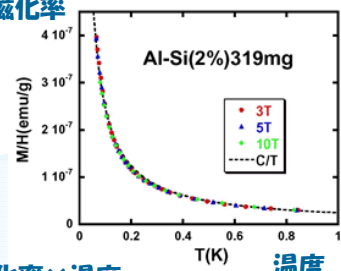
Pauli paramagnetism $\chi > 0$
 $\chi = 10^{-4}$ emu/mol

Diamagnetism $\chi < 0$
Organic compounds without unpaired electrons

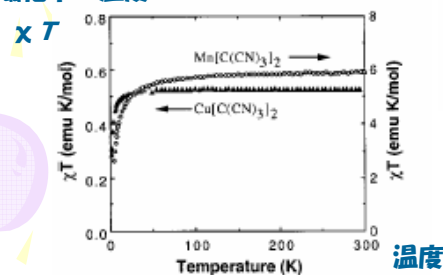
Curie paramagnetism

$$\chi = \frac{M}{H} = \frac{N\mu^2}{k_B T} = \frac{C}{T}$$

磁化率



磁化率×温度



磁化率

温度に反比例

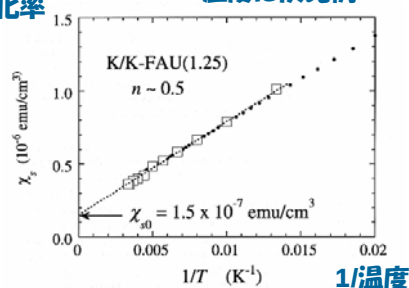


図3 ゼオライトFAU中のカリウムクラスターのスピン磁化率の温度依存性。温度に依存しない成分が顕著に現れる。

Pauli paramagnetism in Metals

磁場をかけると↓よりも↑の方が安定になる。

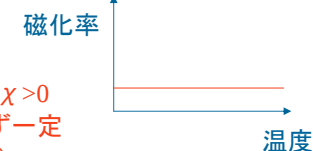
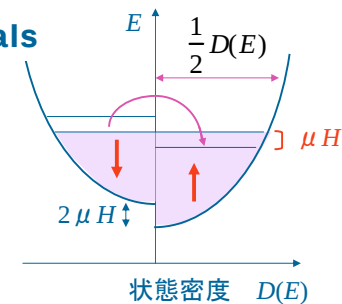
$$E_{\uparrow} = \frac{\hbar^2 k^2}{2m} - \mu H$$

$$E_{\downarrow} = \frac{\hbar^2 k^2}{2m} + \mu H$$

$$\text{磁化 } M = \mu(N_{\uparrow} - N_{\downarrow})$$

$$= \mu \frac{1}{2} D(E) \times 2\mu H$$

$$\text{磁化率 } \chi = \frac{M}{H} = \mu^2 D(E_F)$$



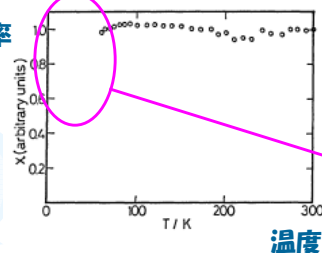
金属の常磁性 $\chi > 0$
は温度によらず一定
(パウリ常磁性)

Pauli paramagnetism in Metals

$$\chi = \mu_B^2 D(E_F)$$

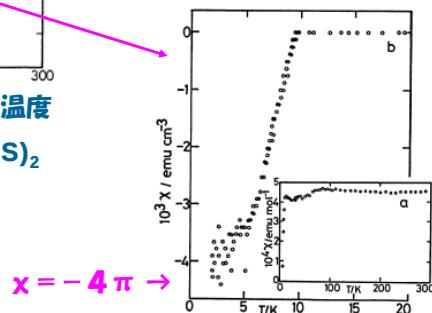
temperature independent

磁化率



κ-(BEDT-TTF)₂Cu(NCS)₂

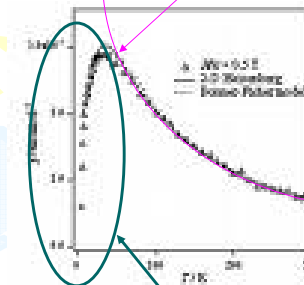
超伝導：完全反磁性 $\chi = -4\pi$



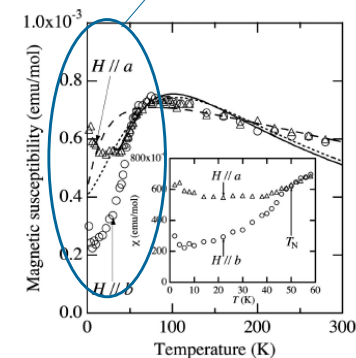
$\chi = -4\pi \rightarrow$

Curie paramagnetism

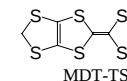
antiferromagnetism



antiferromagnetism

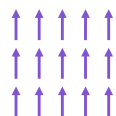


(MDT-TS)(AuI₂)_{0.441}



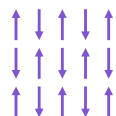
Magnetic order

Ferromagnetism: parallel spins
The material is a magnet.



$J > 0$
 $S_i // S_j$ parallel is stable

Antiferromagnetism:
alternately antiparallel spins
Not a bulk magnet.

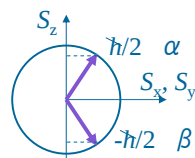


$J < 0$
 $S_i \nparallel S_j$ antiparallel is stable

Spin Hamiltonian

$$\hat{H} = - \sum_{i,j} 2J_{ij} \bar{S}_i \bar{S}_j - g\mu_B H \sum_i \bar{S}_i$$

Interaction Zeemann splitting



S_i is a vector like (S_x, S_y, S_z) (Heisenberg model).

Large magnetic anisotropy (the spin is always aligned in a particular direction (S_z) by the crystal field) $\rightarrow$ only S_z (Ising model)

$S_i = 1/2, S_j = 1/2 \rightarrow -J/2$
 $S_i = 1/2, S_j = -1/2 \rightarrow J/2$ } energy difference J

(Old literatures define $H = - \sum_{i,j} J_{ij} \bar{S}_i \bar{S}_j$ make J duplicated.)

Molecular field approximation

We can sum up $\sum_j$ and use the average.



$$\hat{H} = \sum_i S_i (- \sum_j 2J_{ij} S_j - g\mu_B H) = -g\mu_B (H_{\text{eff}} + H) \sum_i S_i$$

$$H_{\text{eff}} = \frac{1}{g\mu_B} \sum_j 2J_{ij} \langle S_j \rangle \quad \text{average effective (internal) field on } S_i, \text{ generated by the surrounding } S_j$$

S_j should be time dependent, but we use the average value $\langle S_j \rangle$.
(molecular-field or mean-field approximation)

Thermal distribution similarly obtained as Curie paramagnetism gives:

$$M = \frac{N\mu^2 H}{k_B T} \xrightarrow{H \rightarrow H_{\text{eff}} + H} M = \chi_0 (H_{\text{eff}} + H) \quad \text{molecular field coefficient}$$

using $M = Ng \mu_B \langle S \rangle$

$$H_{\text{eff}} = \frac{\sum_j 2J_{ij}}{N(g\mu_B)^2} M = aM$$

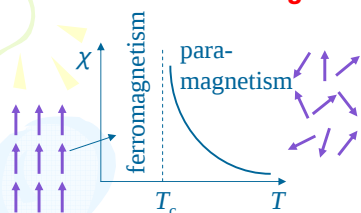
put this to the above eq.

$$M = \chi_0 (aM + H) \quad M \left[(1 - \chi_0 a) \right] = \chi_0 H \rightarrow \chi = \frac{M}{H} = \frac{\chi_0}{1 - \chi_0 a} = \frac{C}{T - \theta} \quad \text{Curie-Weiss role}$$

$$\theta = \frac{1}{k_B} \sum_j 2J_{ij} = \frac{2zJ}{k_B} \quad \leftarrow \text{Coordination number } z \text{ for nearest neighbor } J.$$

Weiss temperature

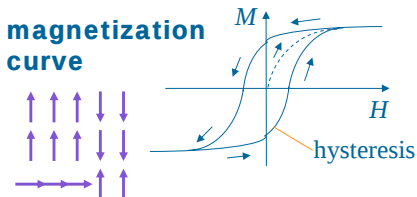
$J > 0 \rightarrow \theta > 0$ **Ferromagnetism**



Curie temperature

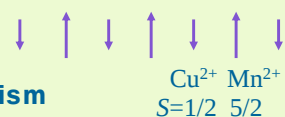
$\chi \rightarrow \infty$ at $T \rightarrow T_c$
 $M \neq 0$ even at $H=0$ at $T < T_c$
 $\rightarrow$ spontaneous magnetism
 T_c Fe 1043 K Ni 627 K

magnetization curve



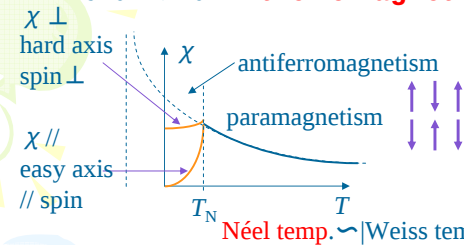
Usually small domains are randomly oriented.
Magnetic fields align the domain spins,
to make the material a bulk magnet.

Ferrimagnetism



Alternating antiparallel alignment of different spins makes net bulk magnetism.
e.g. Ferrite Fe_3O_4 has Fe^{3+} and Fe^{2+} .

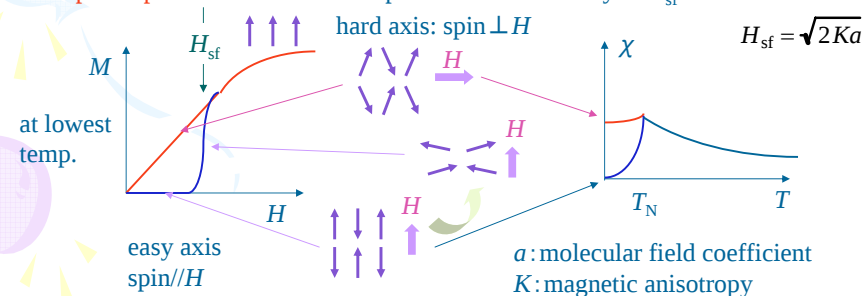
$J < 0 \rightarrow \theta < 0$ Antiferromagnetism



Easy axis in an antiferromagnet

Spin in an antiferromagnetism is restricted in a particular direction, due to
1) the dipole-dipole interaction, or 2) crystal field.

spin flop: increase H makes a spin $\perp H$ state suddenly at H_{sf} .



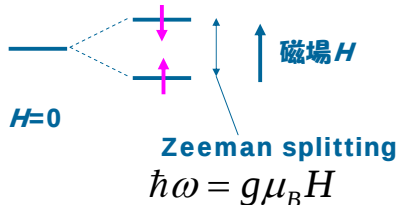
$$H_{\text{sf}} = \sqrt{2Ka}$$

a : molecular field coefficient
 K : magnetic anisotropy

Electron Spin Resonance (ESR)



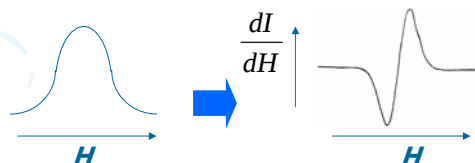
more sensitive than SQUID
one crystal



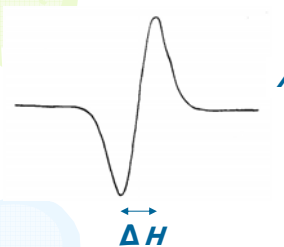
$g = 2.0023$
for free electron

9.5 GHz $\rightarrow H = 3400$ gauss (X band)
35 GHz $\rightarrow H = 12500$ gauss (Q band)

microwave
absorption
 I



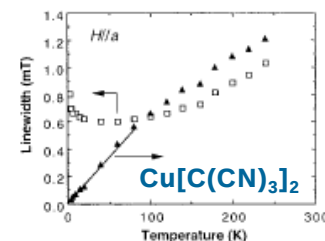
Lorentzian



Electron Spin Resonance (ESR)

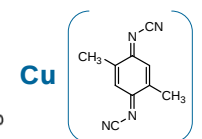
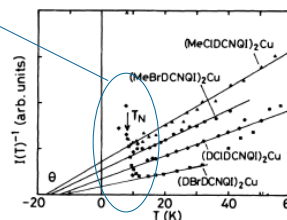
Intensity $I \propto A(\Delta H)^2$

$\rightarrow I \propto$ spin susceptibility χ



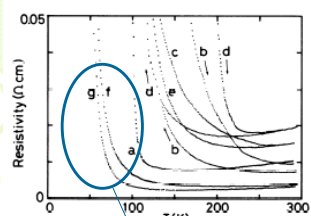
$\chi = \frac{C}{T}$

antiferromagnetism



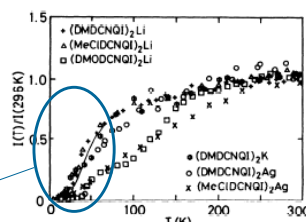
Electron Spin Resonance (ESR)

linewidth



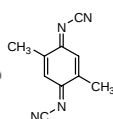
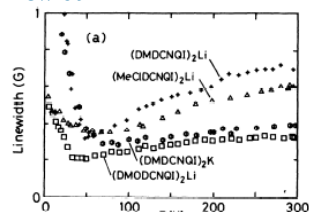
metal-insulator
transition

ESR Intensity



Pauli
paramagnetism
 $\chi = \text{const.}$
(metal)

linewidth



Linewidth : relaxation time
of the electron spin
large in heavy atoms

narrow for mobile electrons
motional narrowing

very large for magnetic order

Generating Low Temperatures

195 K dry ice
77 K

liquid N_2

1.5 K 4.2 K

pumping

^4He

0.3 K

^3He
pumping

$^3\text{He}/^4\text{He}$ dilution
refrigerator



Liquid Helium
in a CLOS

**Bot
dec**



Pt resistor

Thermocouple

Ge resistor

Carbon resistor

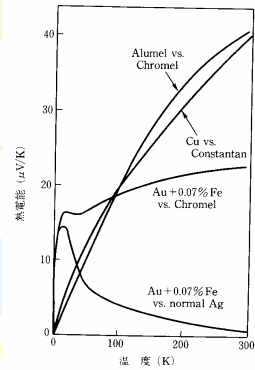
 ^3He
pressure

Ruthenium oxide

Cernox

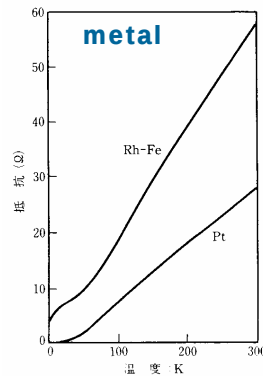


Thermocouple



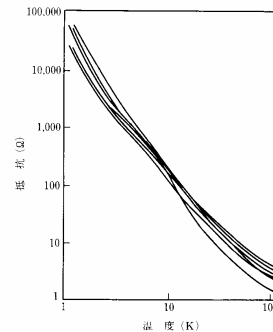
Almel · chromel
Cu · constantan
Au/Fe · chromel

60~400 K
60~400 K
4~400 K



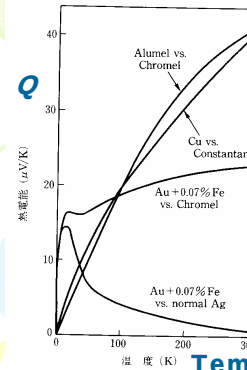
Pt resistor

semiconductor



Carbon resistor

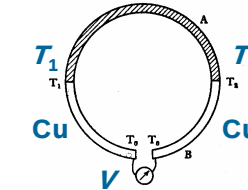
Thermocouple 熱電対



Almel · chromel
Cu · constantan
Au/Fe · chromel

60~400 K
60~400 K
4~400 K

constantan



Connect two kinds of metals, apply temp. diff. between T_1 , and T_2 .

Standard T_2
0°C(ice), LN₂, rt
 T_1 is measured.

Temp. Thermopower Seebeck effect

$$Q = \frac{\Delta V}{\Delta T}$$

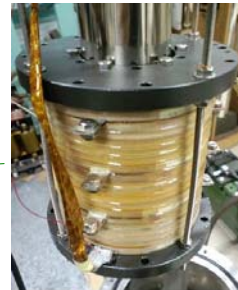
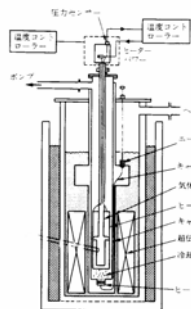
$$Q = \frac{\pi^2 k_B^2 T}{3e} \left[\frac{\partial \ln \sigma(E)}{\partial E} \right] = \frac{\pi^2 k_B^2 T}{6e E_F} \propto T \quad \text{metal}$$

$$Q = \frac{\pi^2 k_B^2 T}{3e} \frac{E_g}{T} \quad \text{semiconductor}$$

insensitive at LT

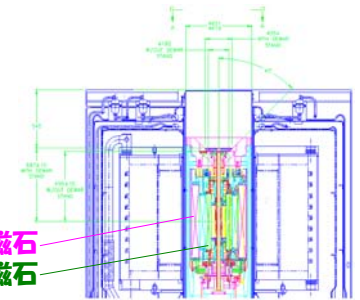
Q : entropy of electron = curvature of energy band

強磁場：超伝導マグネット ～ 15 T



強磁場

物材機構：35 T ハイブリッド磁石



外側 超伝導磁石
内側 常伝導磁石

フロリダ 国立強磁場施設：
45 T ハイブリッド磁石

