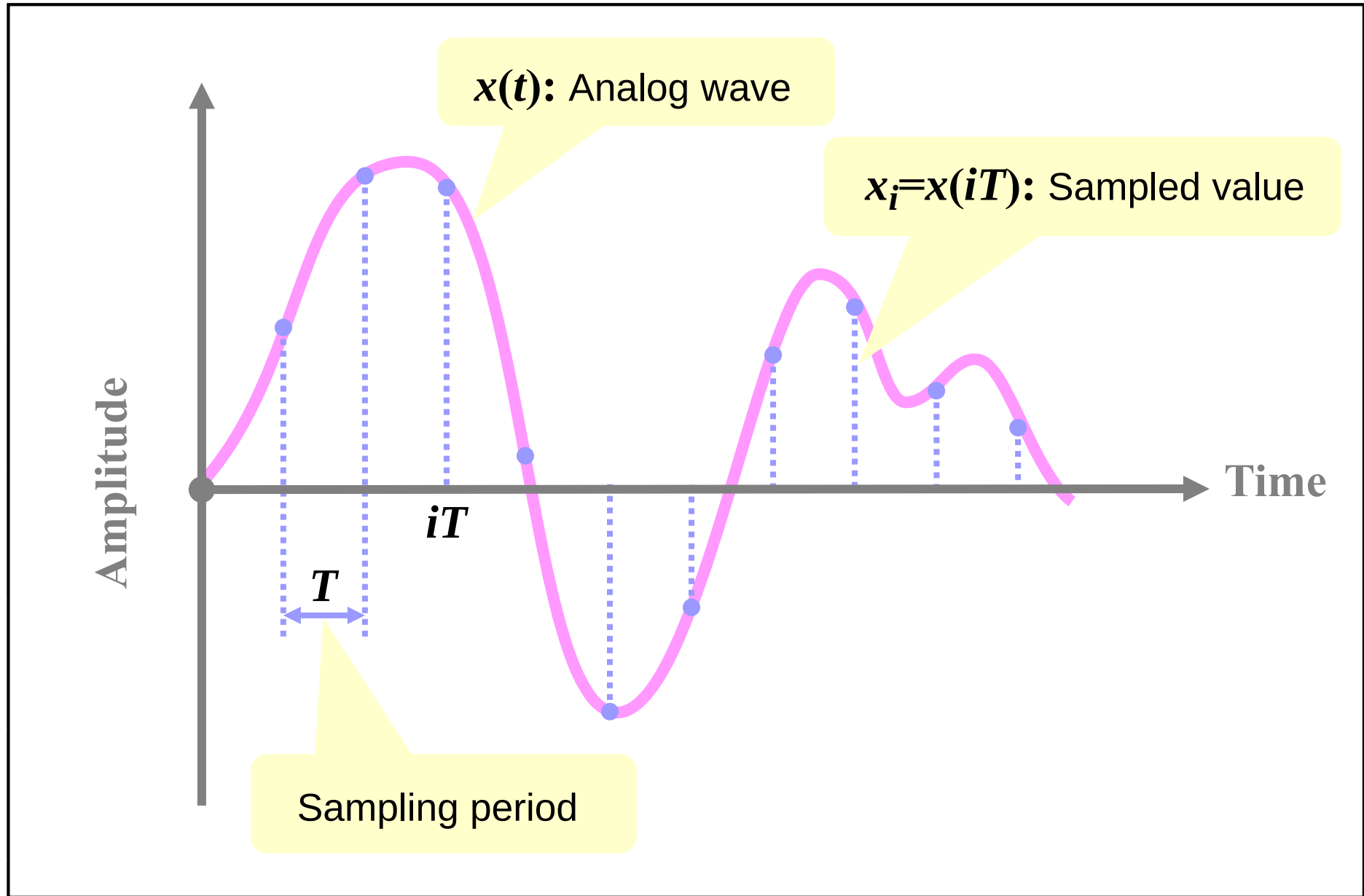


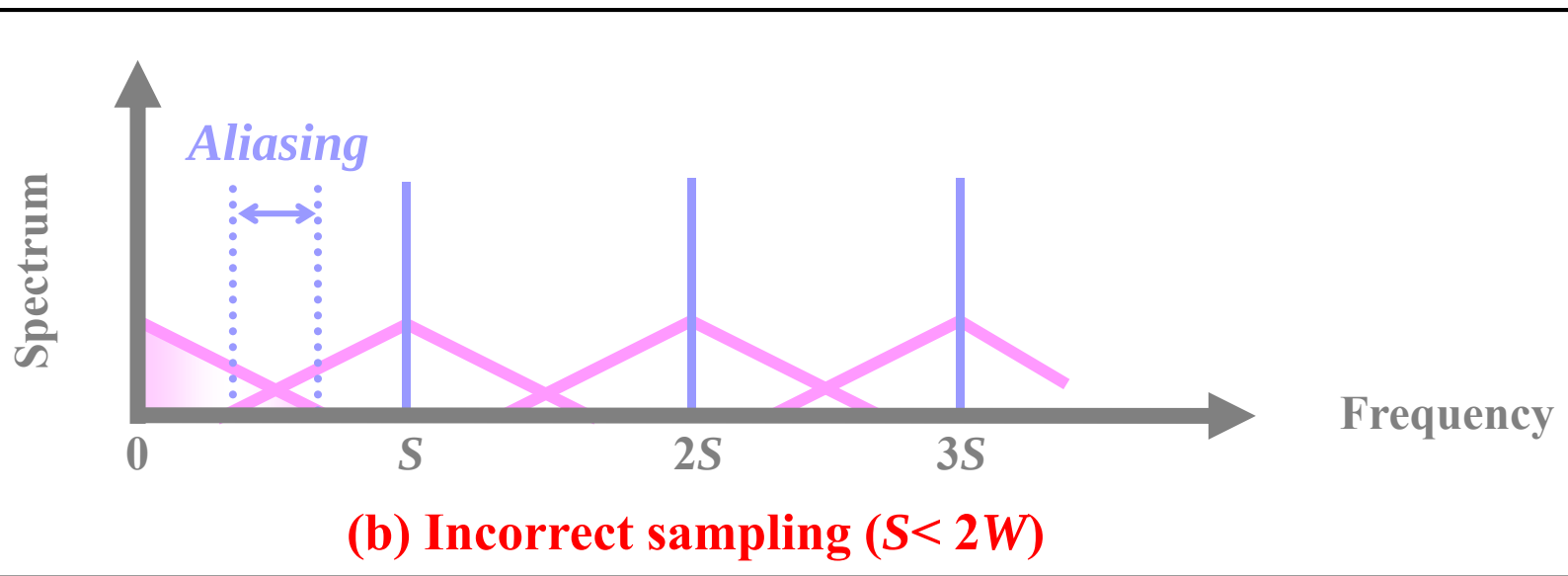
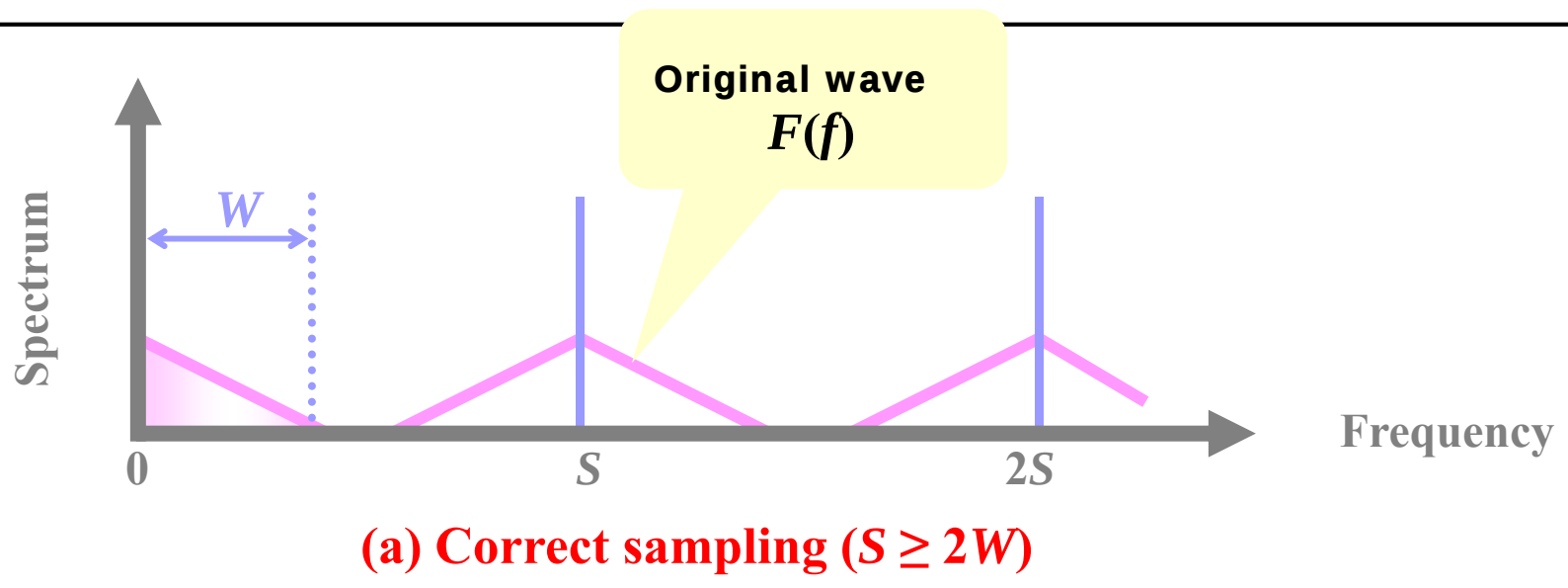
# Speech Analysis

*Sadaoki Furui*

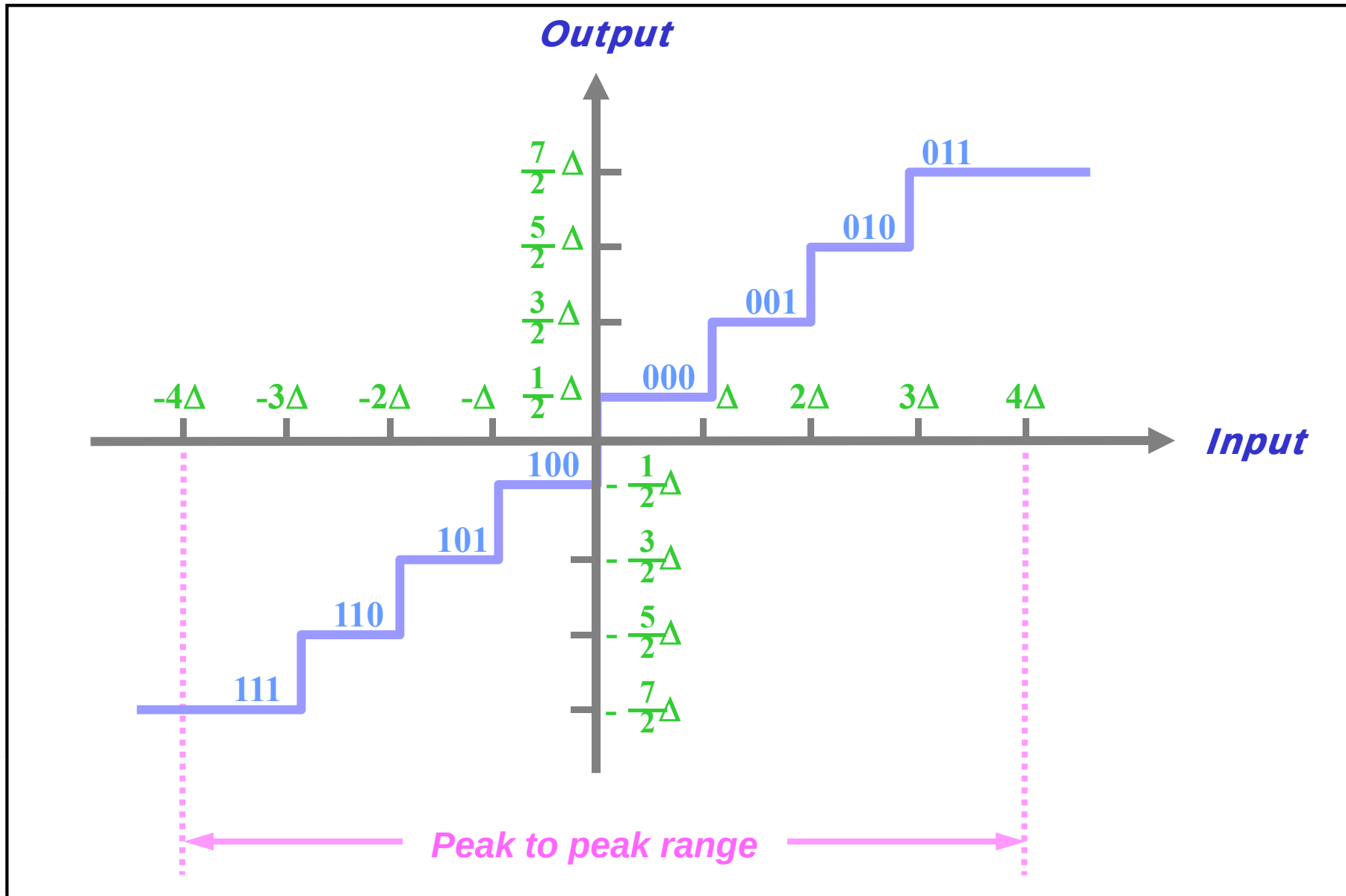
Tokyo Institute of Technology  
Department of Computer Science  
furui@cs.titech.ac.jp



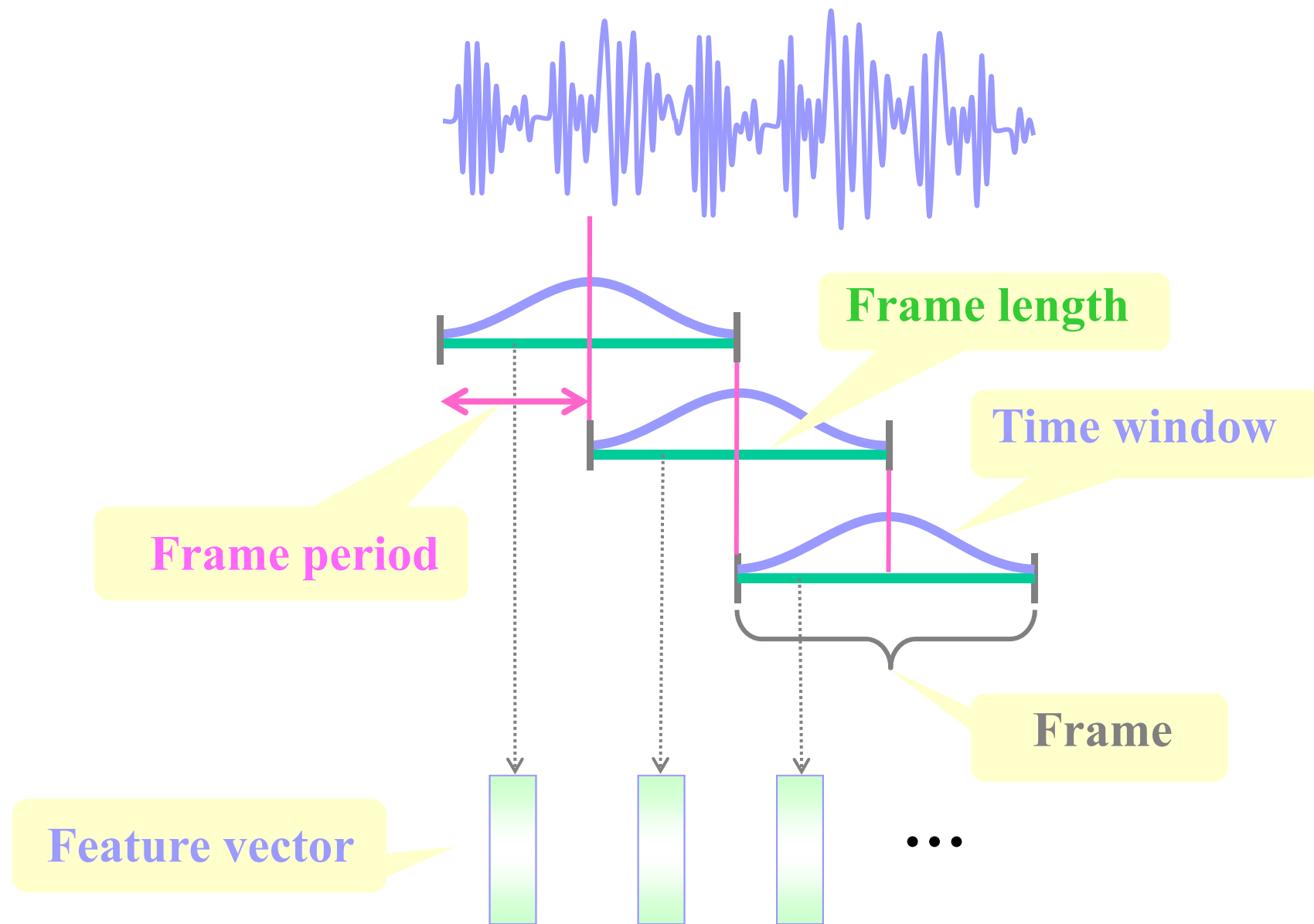
**Sampling in the time domain**



**Sampling in the frequency domain**



**An example of the input-output characteristics of eight-level (3-bit) quantization**

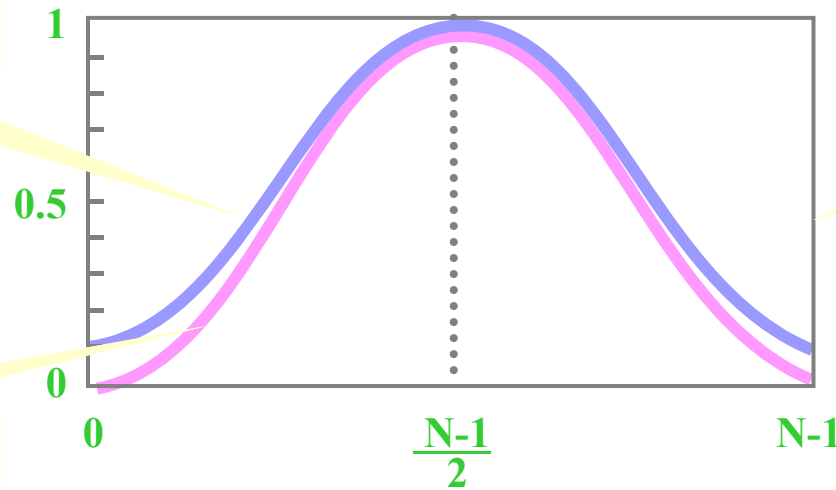


**Feature vector (short-time spectrum) extraction from speech**

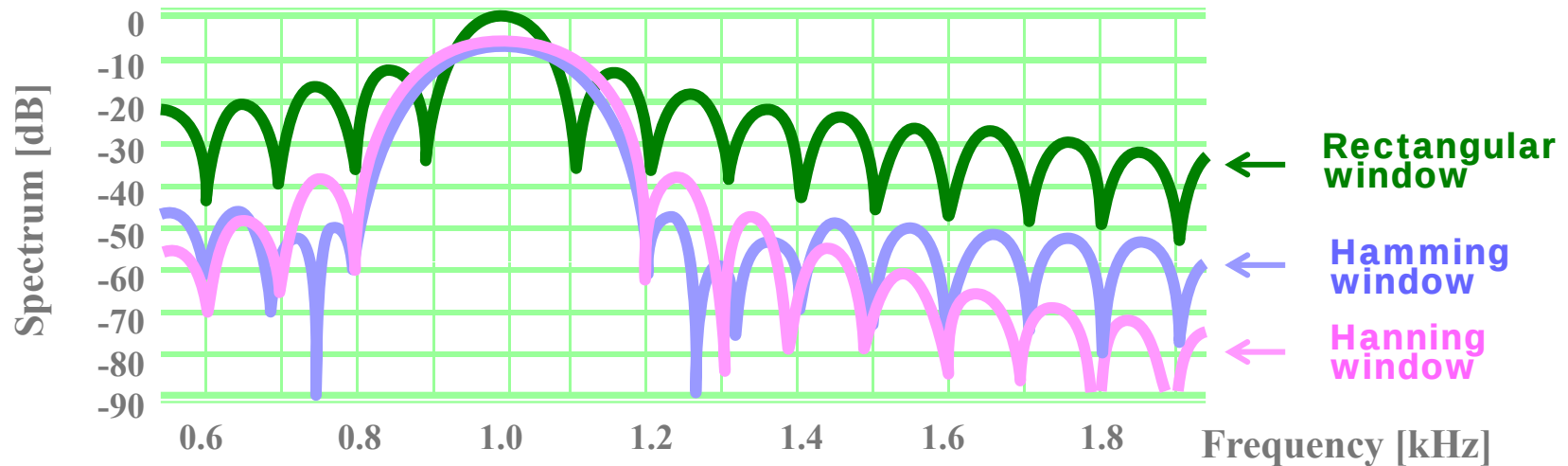
Hamming  
window

Rectangular  
window

Hanning  
window

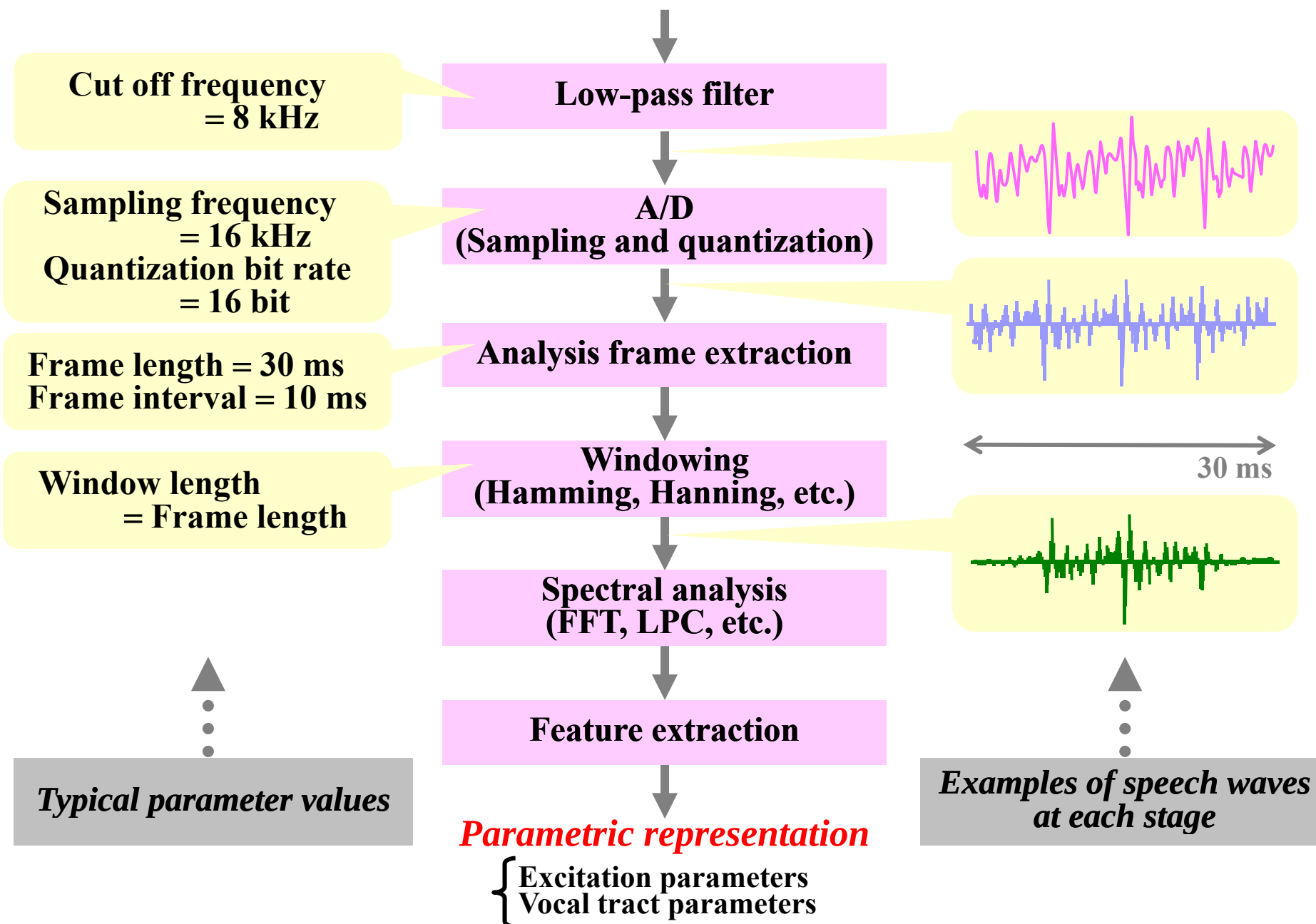


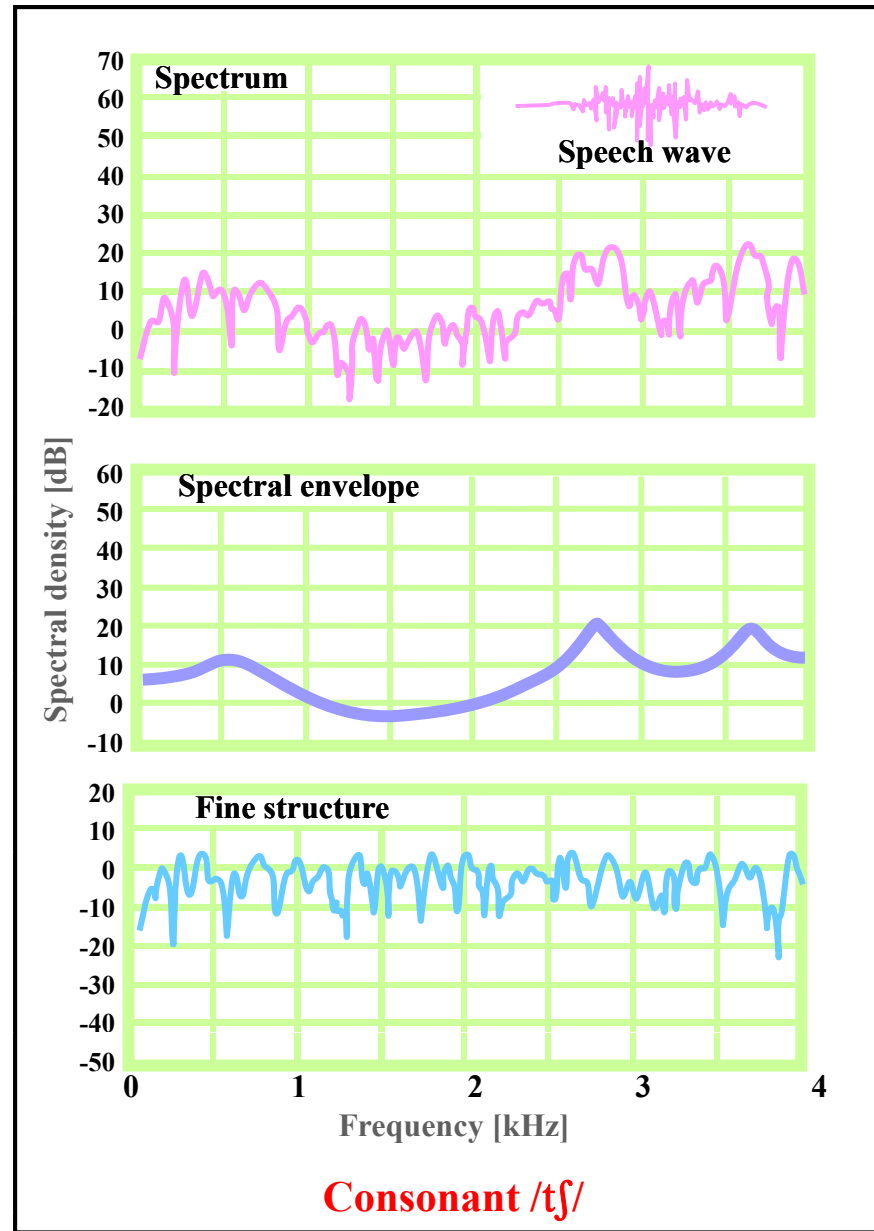
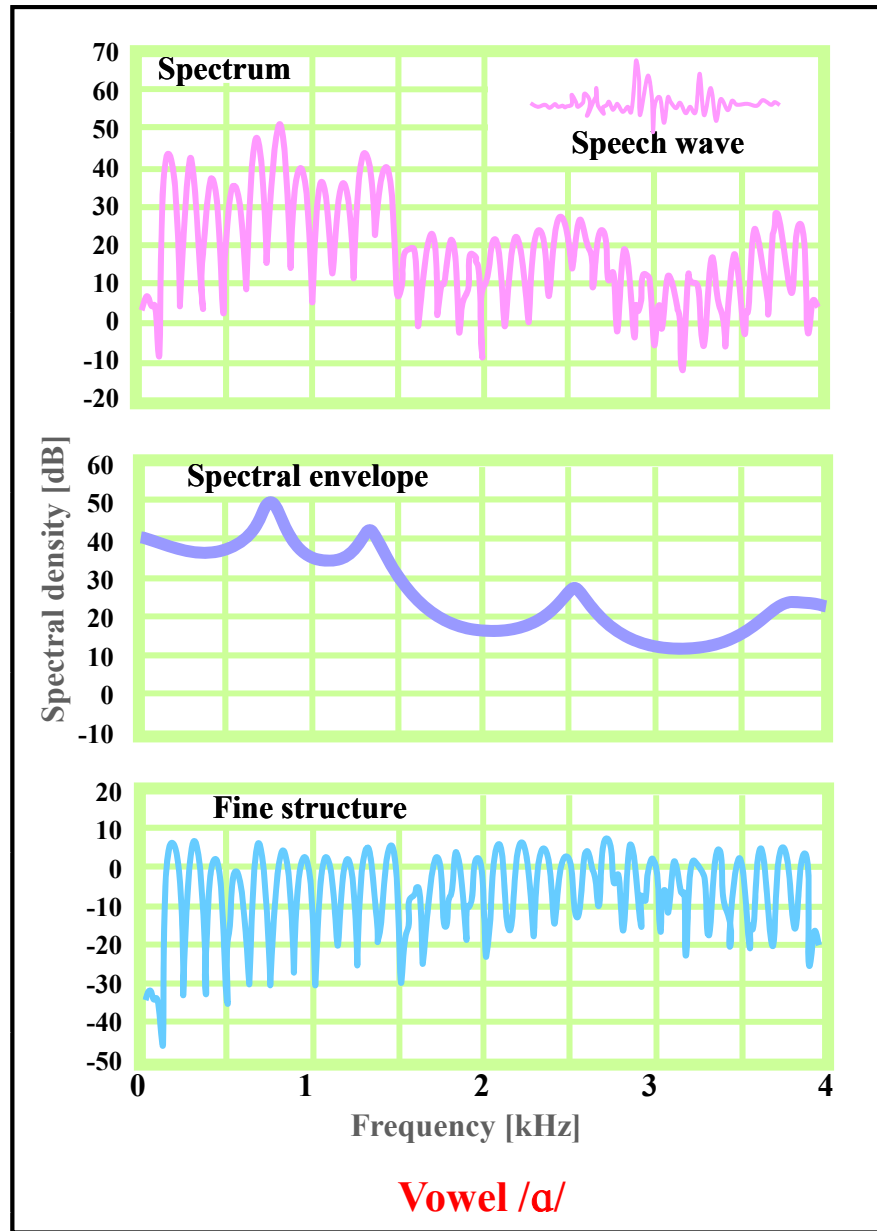
(a) Major window functions



(b) The spectrum for the 10 periods of a 1-kHz sinusoidal wave extracted using each of the windows

# Block diagram of a typical speech analysis procedure.





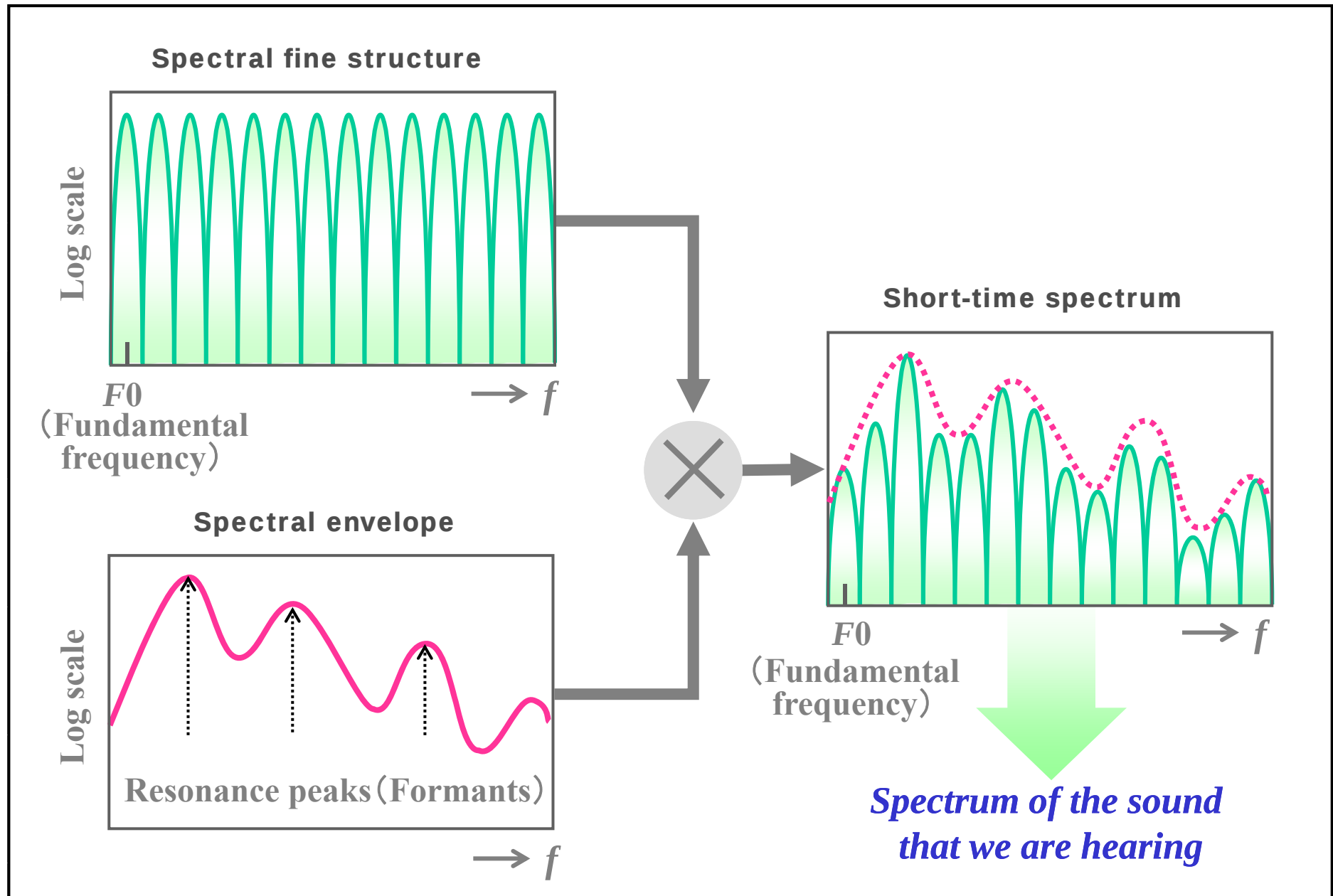
**Structure of short-time speech spectra for male voices when uttering vowel /a/ and consonant /tʃ/**

# Major methods for analyzing speech spectra and their principal features

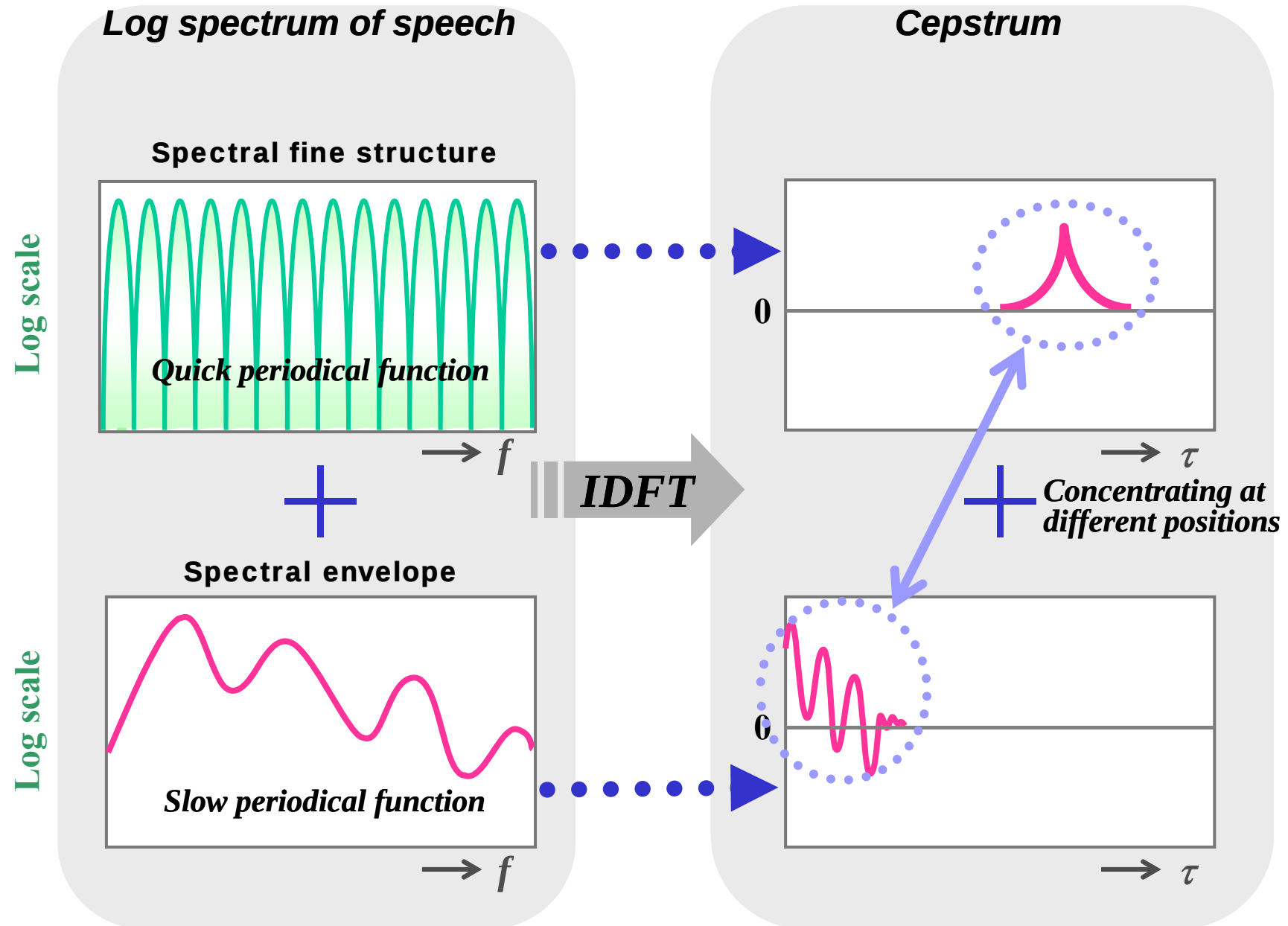
| Type       | Analysis methods               | Parameters                | Features                                                                                                             |
|------------|--------------------------------|---------------------------|----------------------------------------------------------------------------------------------------------------------|
| <b>NPA</b> | (i) Short-time autocorrelation | $\phi(m)$                 | Spectral envelope and fine structure are convoluted.                                                                 |
|            | (ii) Short-time spectrum       | $S(\omega)$               | Spectral envelope and fine structure are multiplied. Fast algorithm can be realized by FFT.                          |
|            | (iii) Cepstrum                 | $c(\tau)$                 | Spectral envelope and fine structure can be Separated in quefrency domain. Two FFTs and log transform are necessary. |
|            | (iv) Band-pass filter bank     | rms of filter output      | Global spectral envelope can be obtained.                                                                            |
|            | (v) Zero-crossing analysis     | Zero-crossing rate        | Formant freq. Can be obtained by Combination with (iv). Realized by simple hardware.                                 |
| <b>PA</b>  | (i) Analysis-by-synthesis      | Formant, band-width, etc. | Precise modeling is possible. Accurate formant freq. can be obtained. Complicated iteration is necessary.            |
|            | (ii) Linear predictive coding  |                           | Simple all-pole spectrum modeling. Parameters can be estimated from auto-corr. or ovariance without iteration.       |

## Major methods for analyzing speech spectra and their principal features (continued)

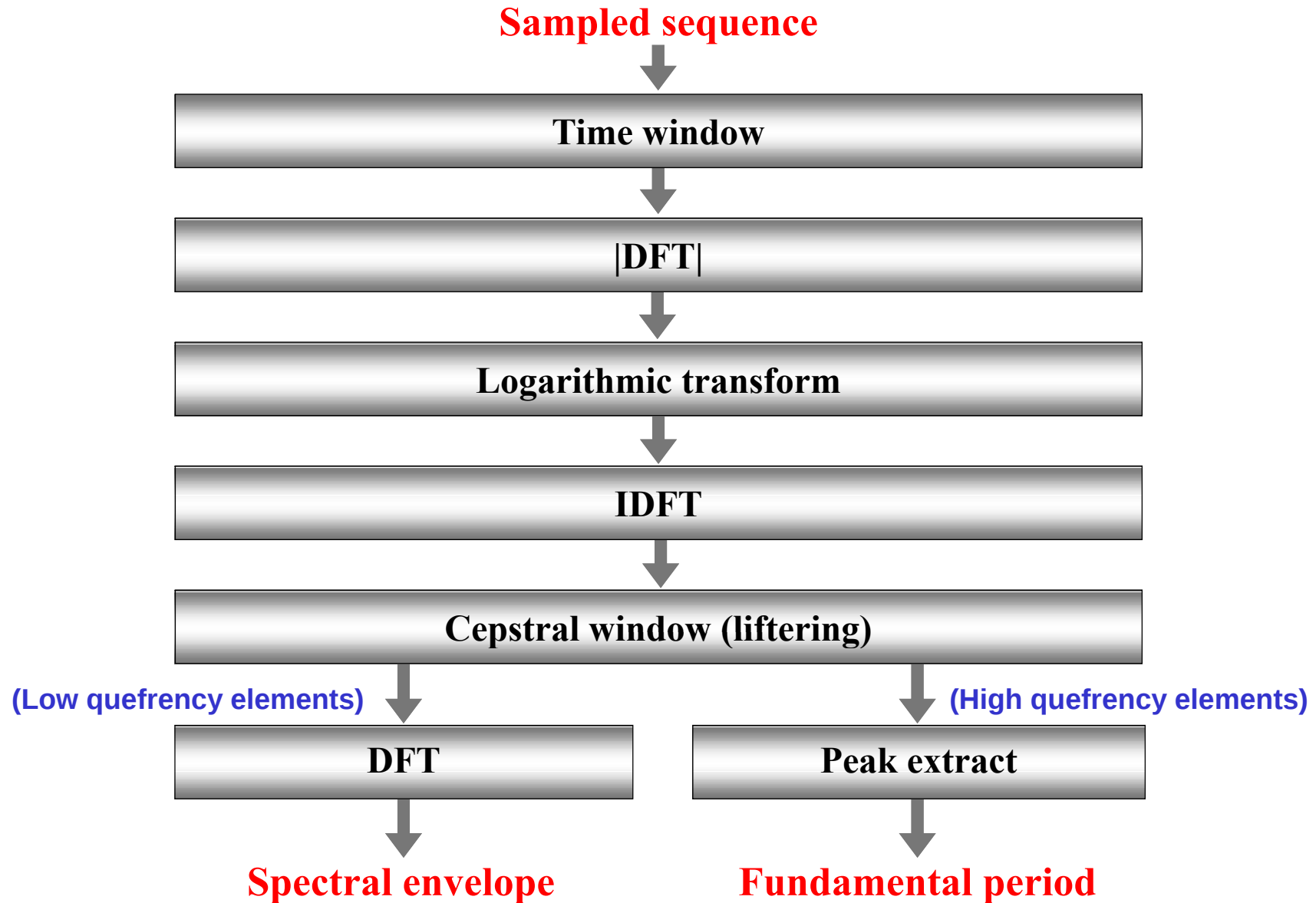
| Type                  | Analysis methods                    | Parameters | Features                                                                                                                                  |
|-----------------------|-------------------------------------|------------|-------------------------------------------------------------------------------------------------------------------------------------------|
| <b>PA<br/>(cont.)</b> | (ii-a)<br>Maximum likelihood method | $\alpha_i$ | Stability of synthesis filter is guaranteed.<br>Time window is necessary.<br>Number of calculations $\propto p^2$                         |
|                       | (ii-b)<br>Convariance method        | $\alpha_i$ | Stability of synthesis filter is not guaranteed.<br>Suitable for short-time analysis.<br>Number of calculations $\propto p^3$             |
|                       | (ii-c)<br>PARCOR method             | $k_i$      | Normal equation can be solved by lattice filter.<br>Equivalent to (a) and (b).<br>Number of calculations $\propto p^2$                    |
|                       | (ii-d)<br>LSP method                | $\omega_i$ | Quantization and interpolation characteristics are good. Similar to formant.<br>Number of calculation is slightly larger than for PARCOR. |



## Spectral structure of speech

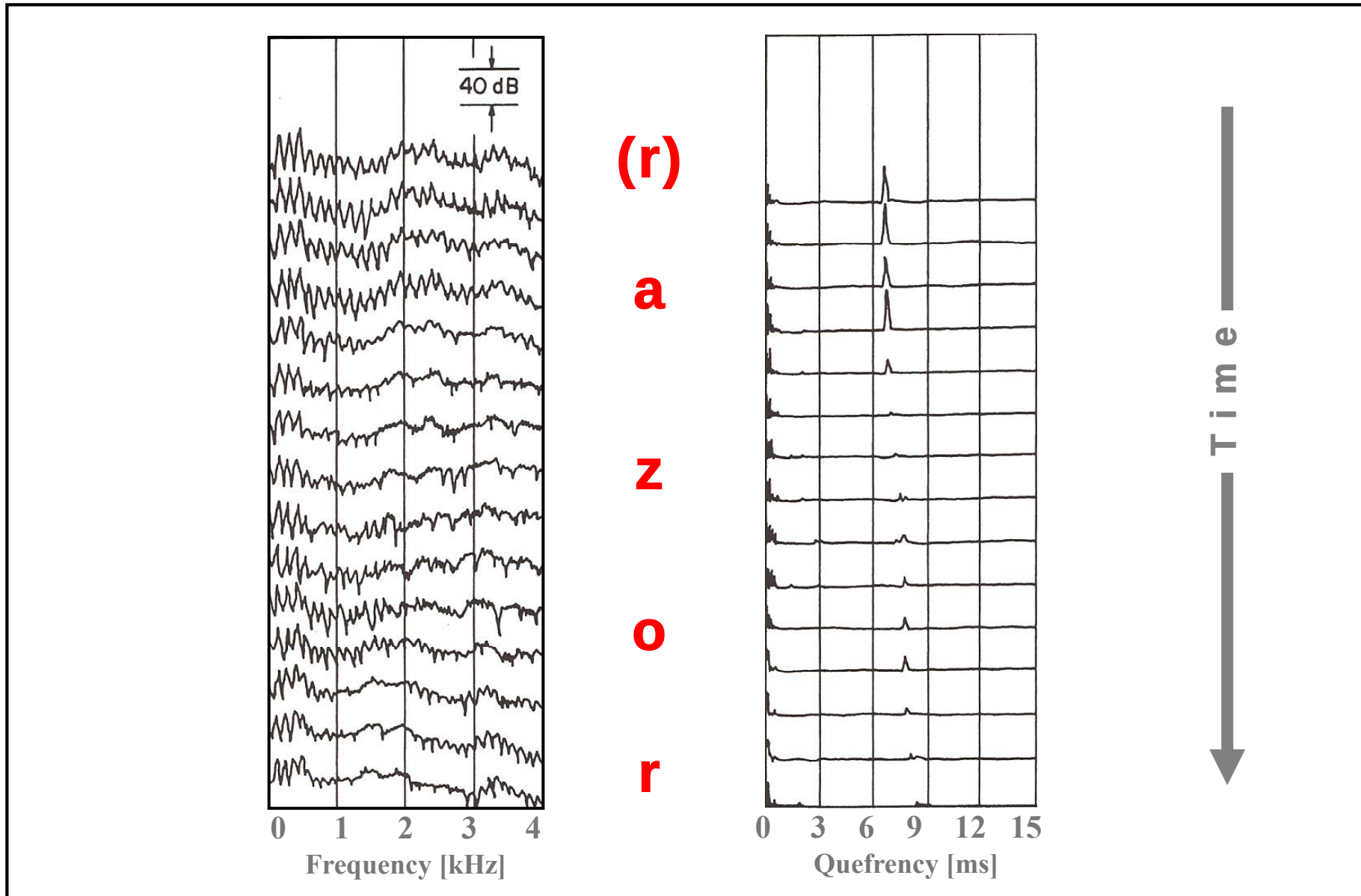


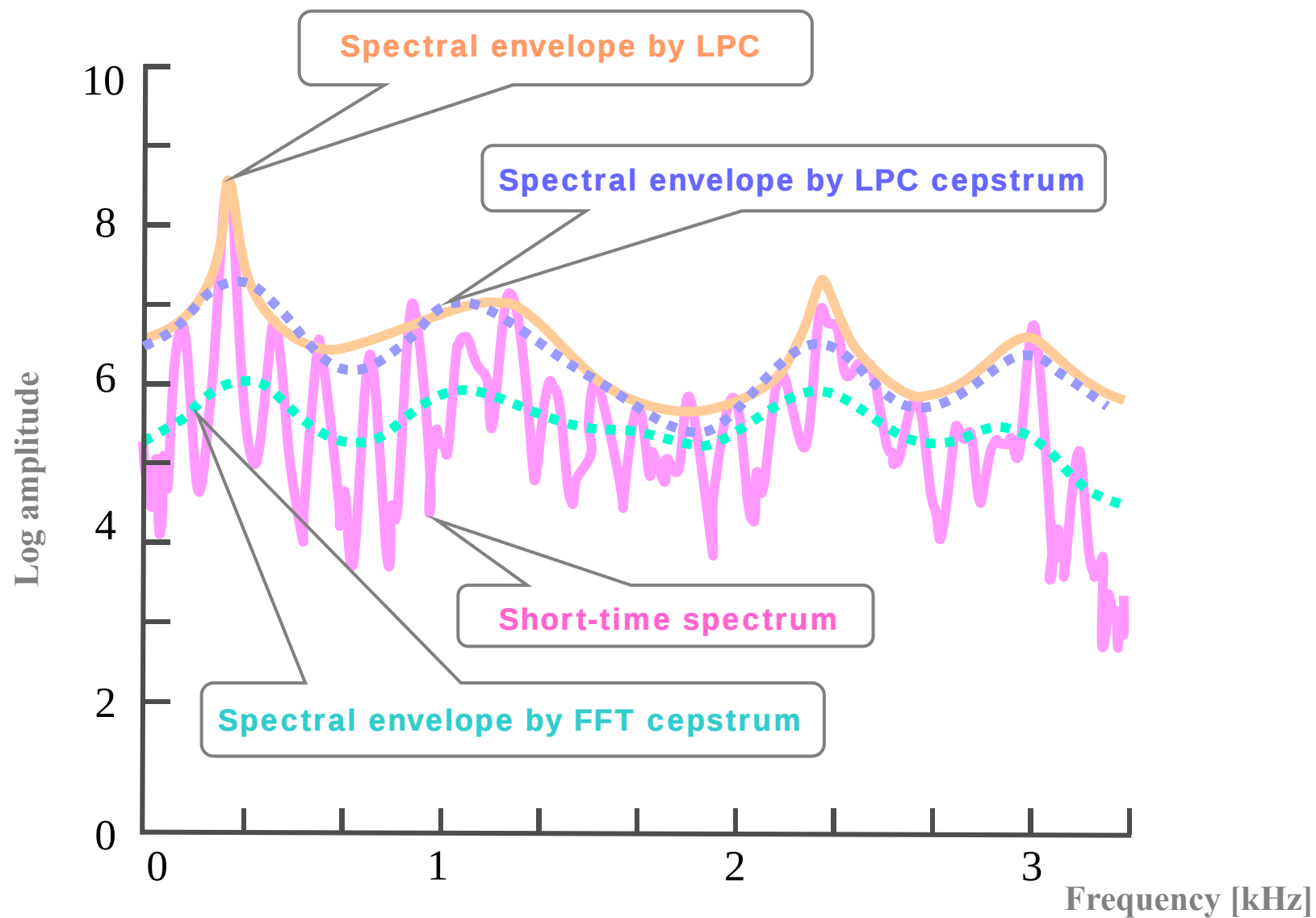
**Log spectrum and Cepstrum**



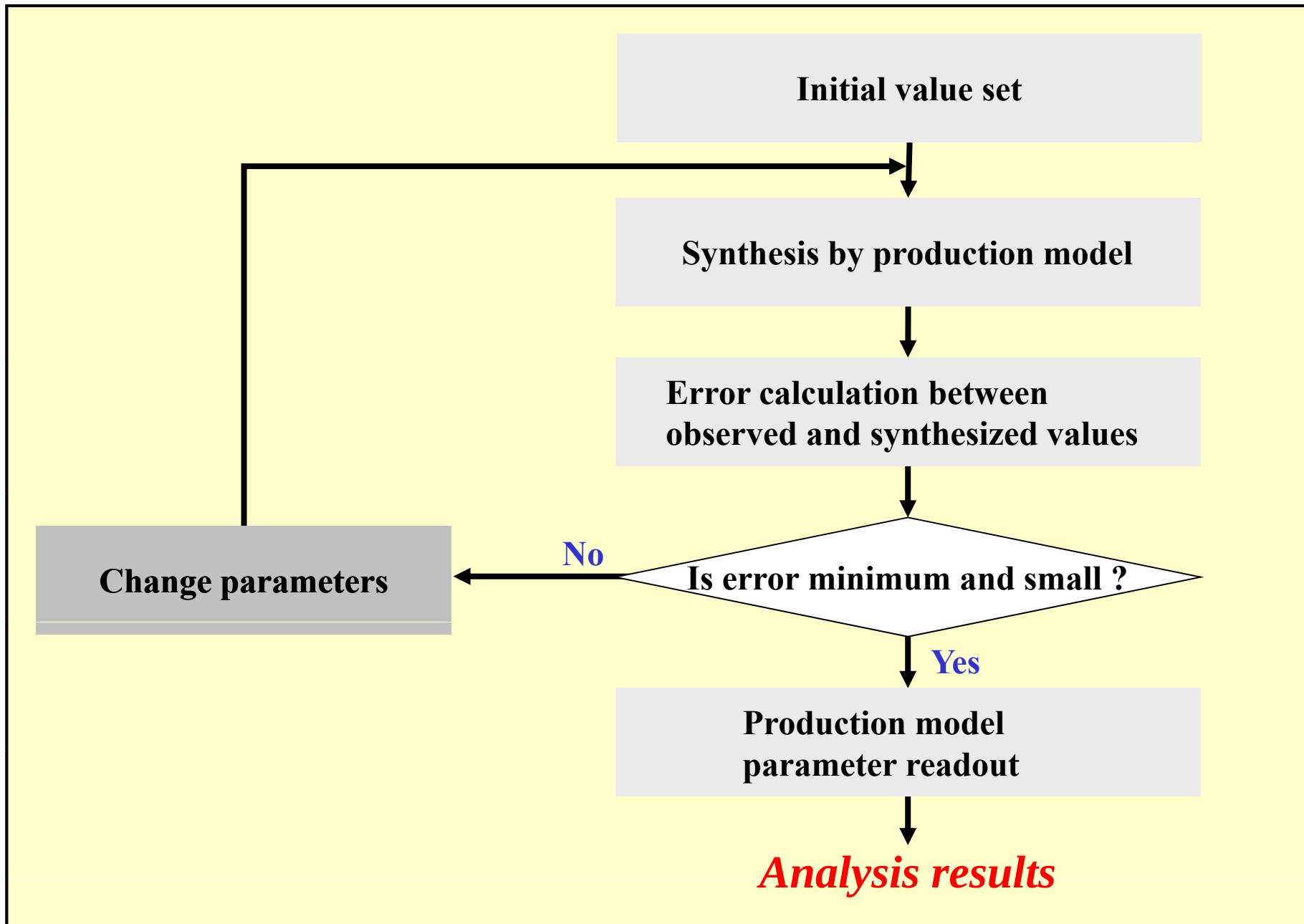
**Block diagram of cepstrum analysis  
for extracting spectral envelope and fundamental period**

**Examples of short-time spectra (left) and cepstra (right) for male voice when uttering “(r)azor”. Sampling frequency 10kHz; Hamming window length 40ms; frame interval 10ms.**





**Comparison of spectral envelopes by LPC, LPC cepstrum, and FFT cepstrum methods**



**Principle of analysis-by-synthesis (A-b-S) method**

## Linear prediction

(Time-domain representation)

$$x_t + \underbrace{\sum_{i=1}^p \alpha_i x_{t-i}}_{-\hat{x}_t} = \varepsilon_t$$

$$x_t - \hat{x}_t = \varepsilon_t$$

LMS estimation

## All-pole/Auto-regression model

(Spectral-domain representation)

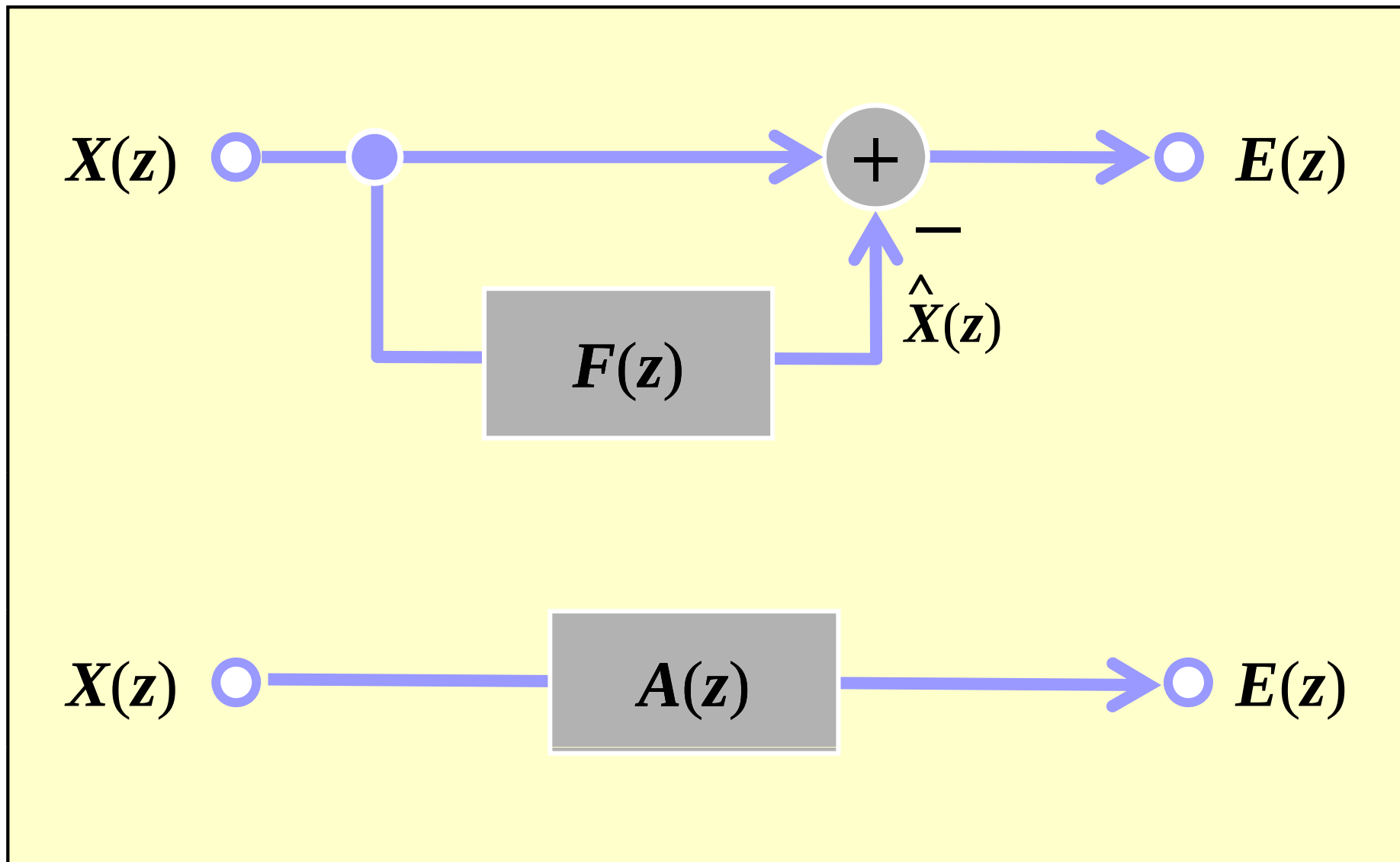
$$H(z) = \frac{1}{1 + \sum_{i=1}^p \alpha_i z^{-i}} = \frac{1}{\prod_{i=1}^p (1 - \frac{z}{z_i})}$$

Maximum-likelihood estimation

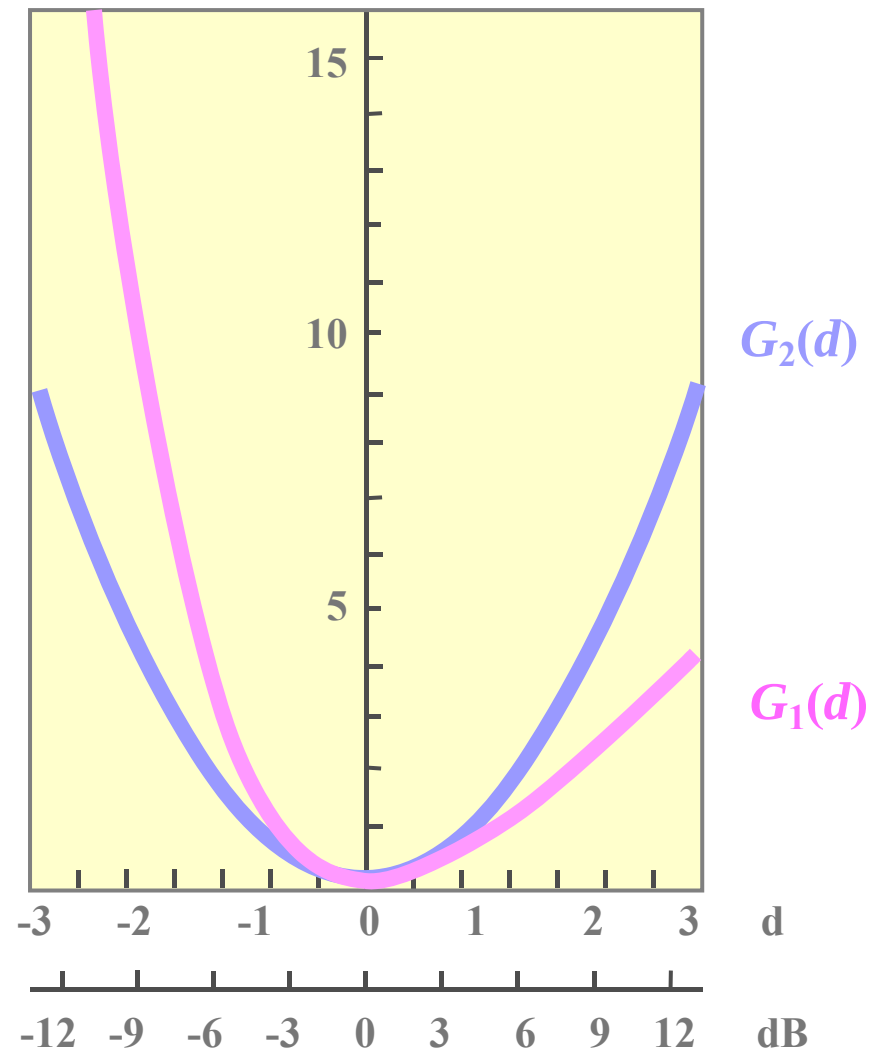
Normal equation

$$\begin{bmatrix} r(0) & r(1) & \cdots & r(p-1) \\ r(1) & r(0) & \cdots & r(p-2) \\ \vdots & \vdots & \ddots & \vdots \\ r(p-1) & r(p-2) & \cdots & r(0) \end{bmatrix} \begin{bmatrix} \alpha_1 \\ \alpha_2 \\ \vdots \\ \alpha_p \end{bmatrix} = - \begin{bmatrix} r(1) \\ r(2) \\ \vdots \\ r(p) \end{bmatrix}$$

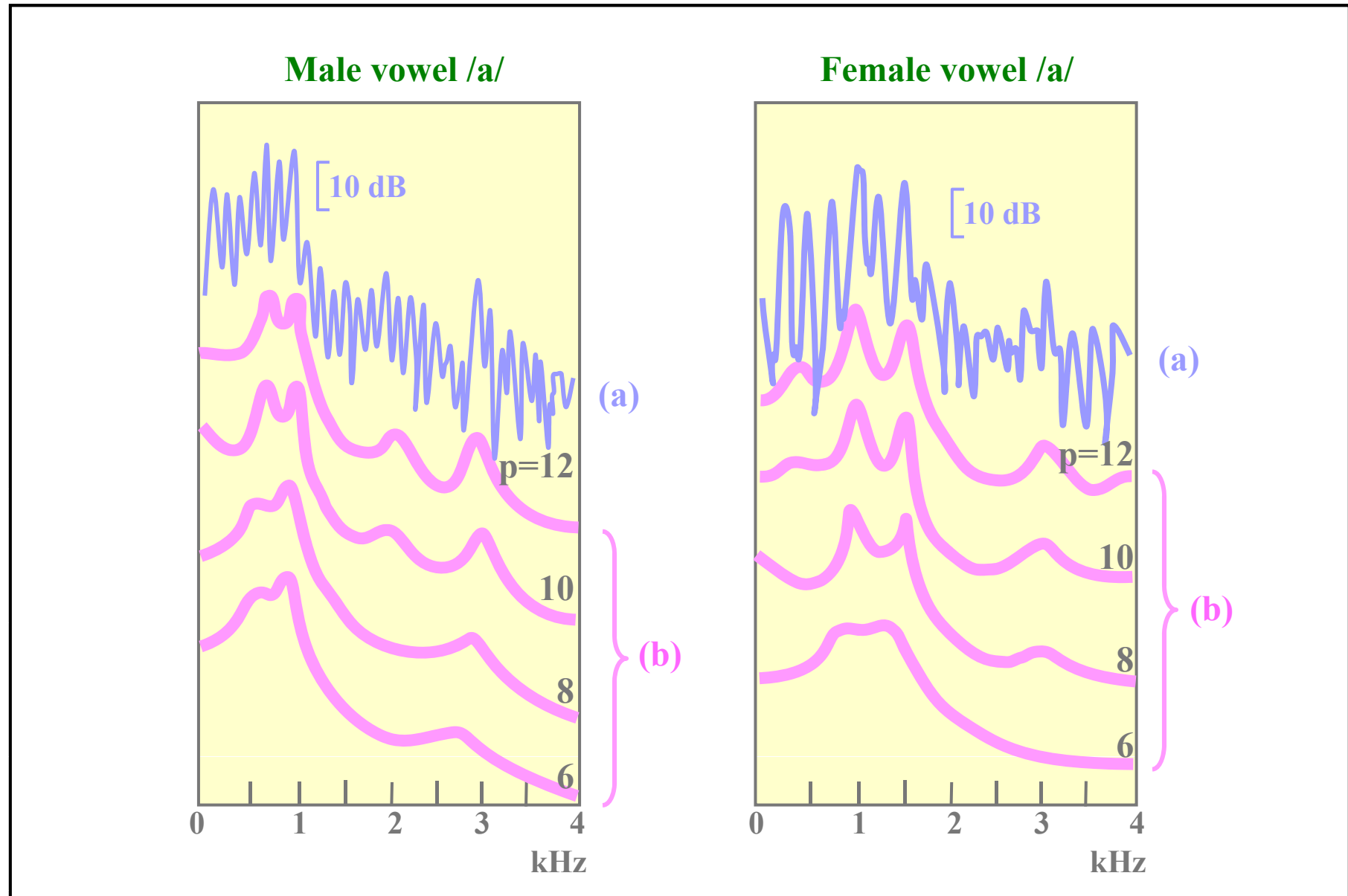
# Principles of LPC analysis



**Linear prediction model block diagram**

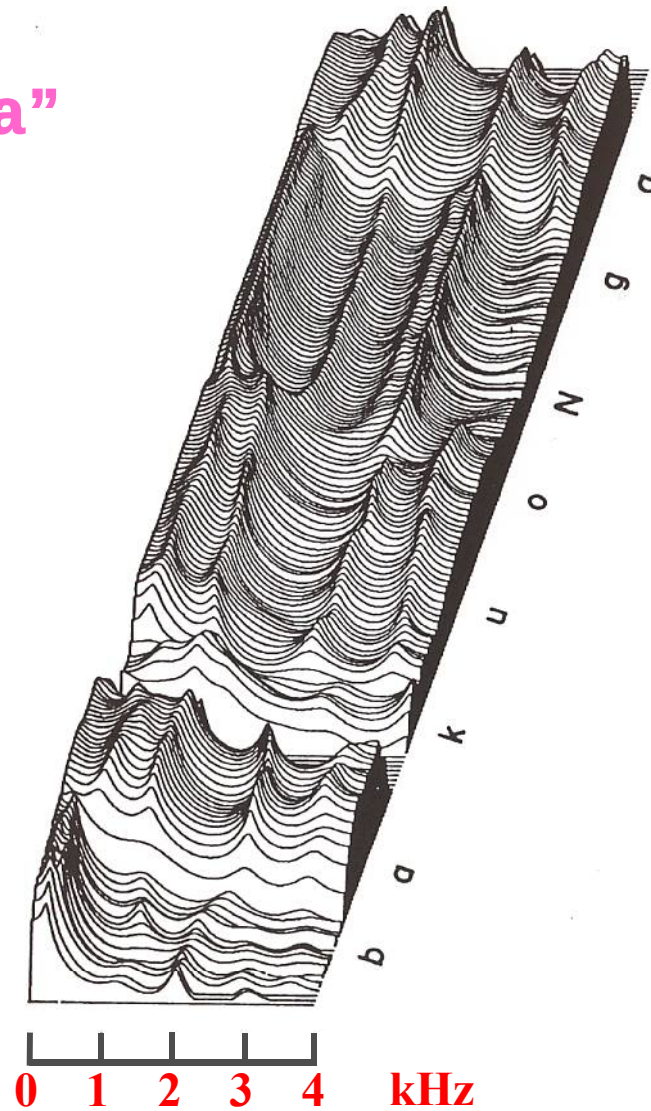


**Comparison of matching error measure in maximum likelihood method,  $G_1(d)$ , with that in analysis-by-synthesis (A-b-S) method,  $G_2(d)$ .  
 $d = \log\{f(\lambda) / \hat{f}(\lambda)\}$ ;  $f(\lambda)$  = model spectrum;  $\hat{f}(\lambda)$  = short-term spectrum.**



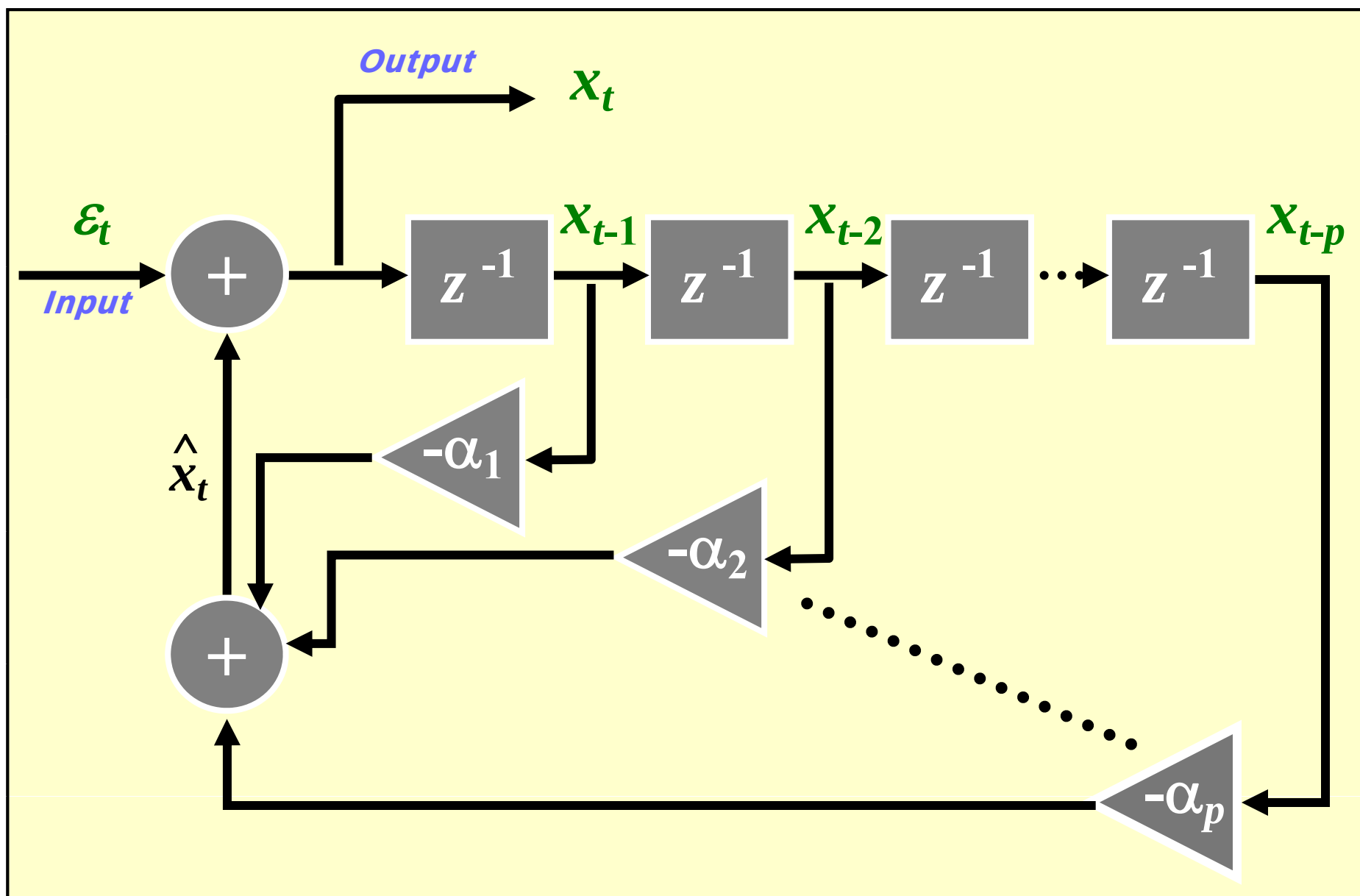
**Comparison of (a) short-term spectra and (b) spectral envelopes obtained by the maximum likelihood method**

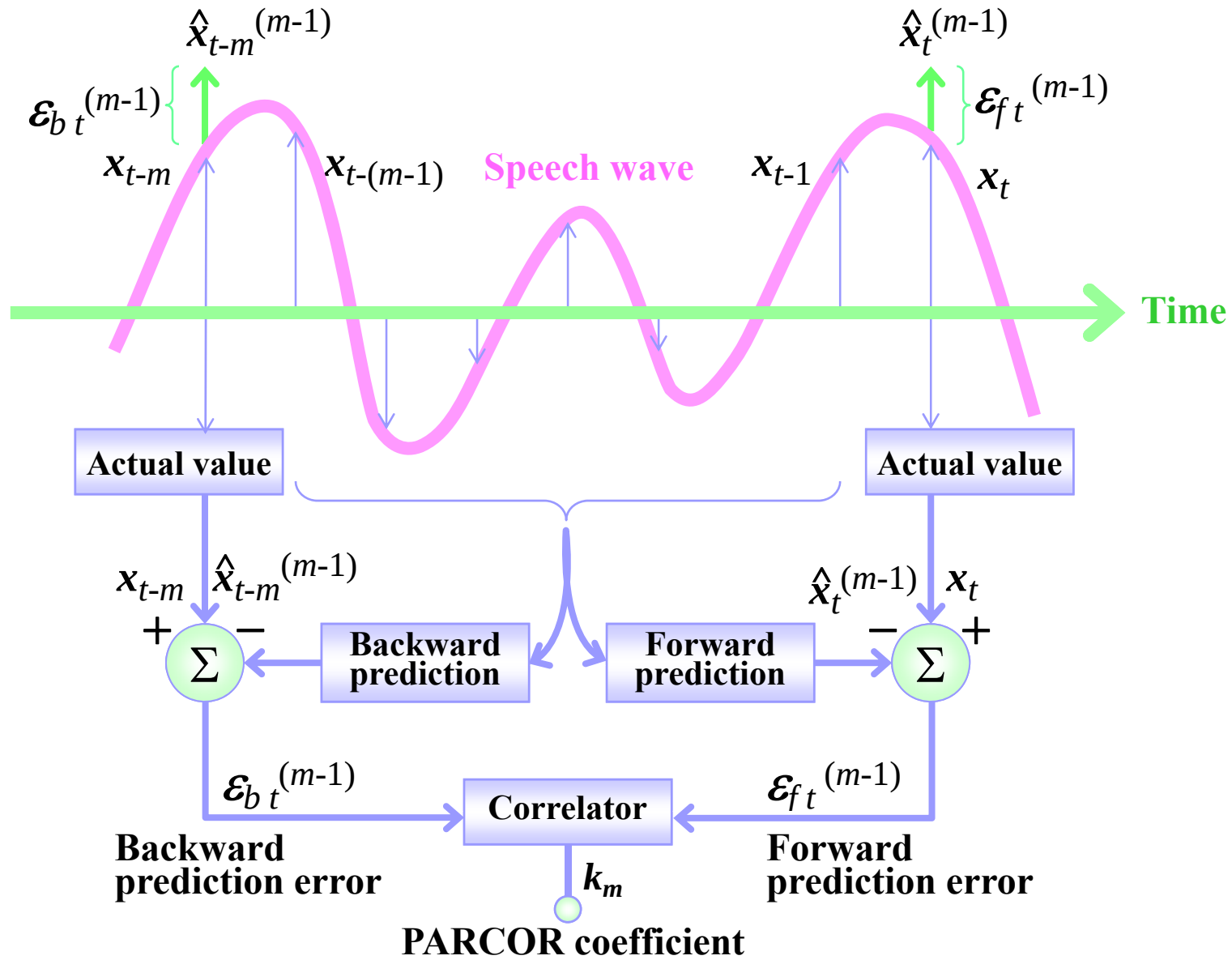
“bakuoNga”



**Time function of spectral envelopes for the Japanese phrase  
/bakuoNga/ uttered by a male speaker**

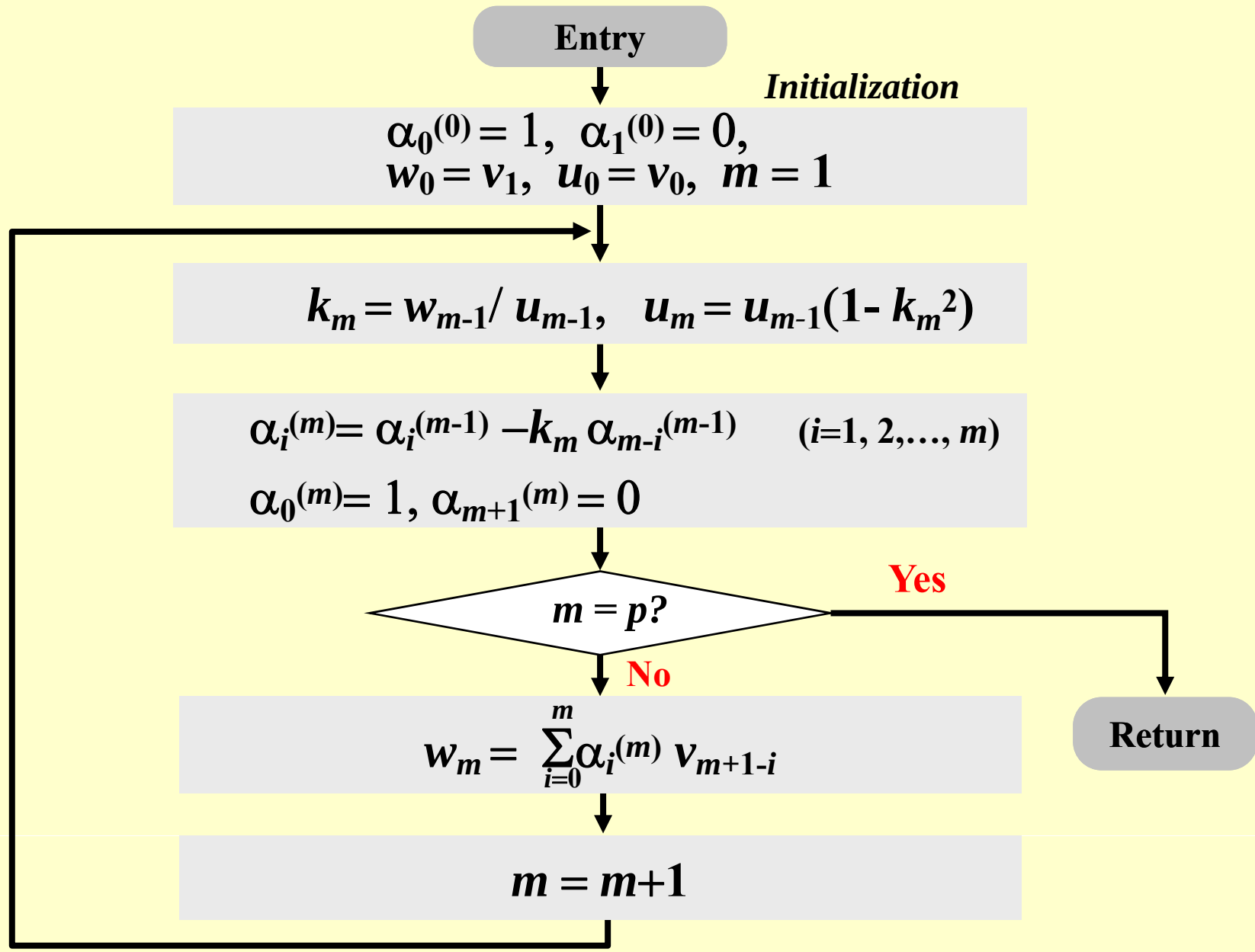
# Speech synthesis circuit based on linear predictive analysis method

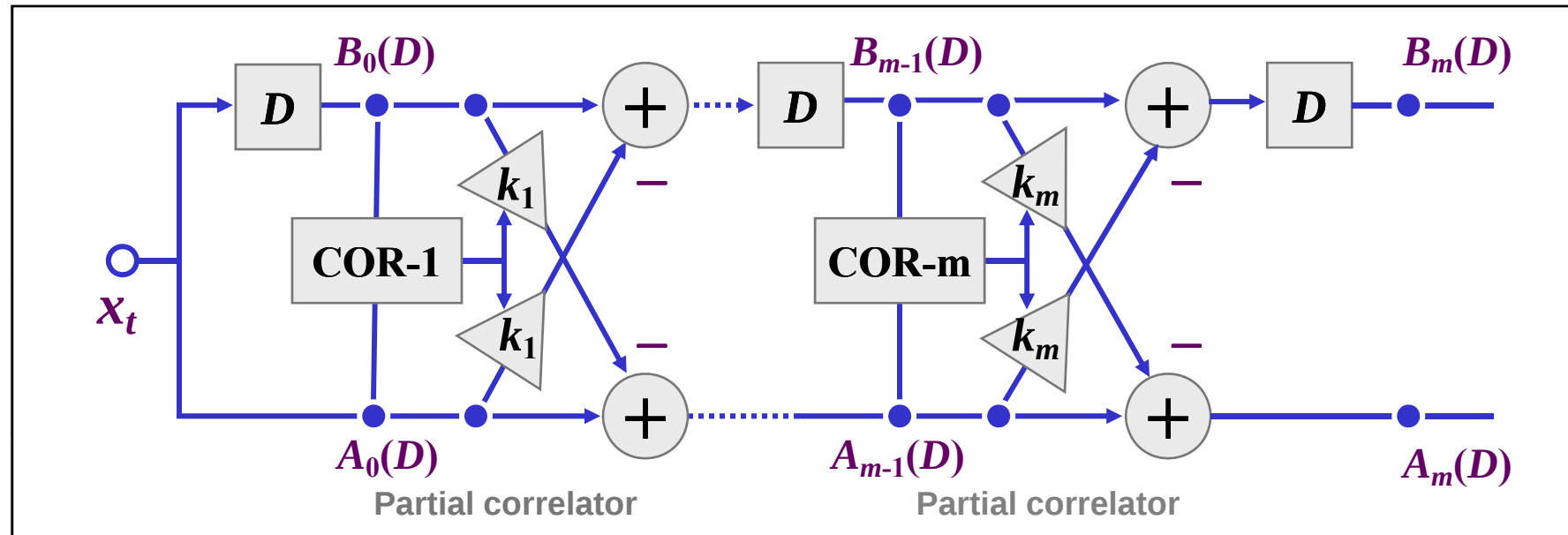




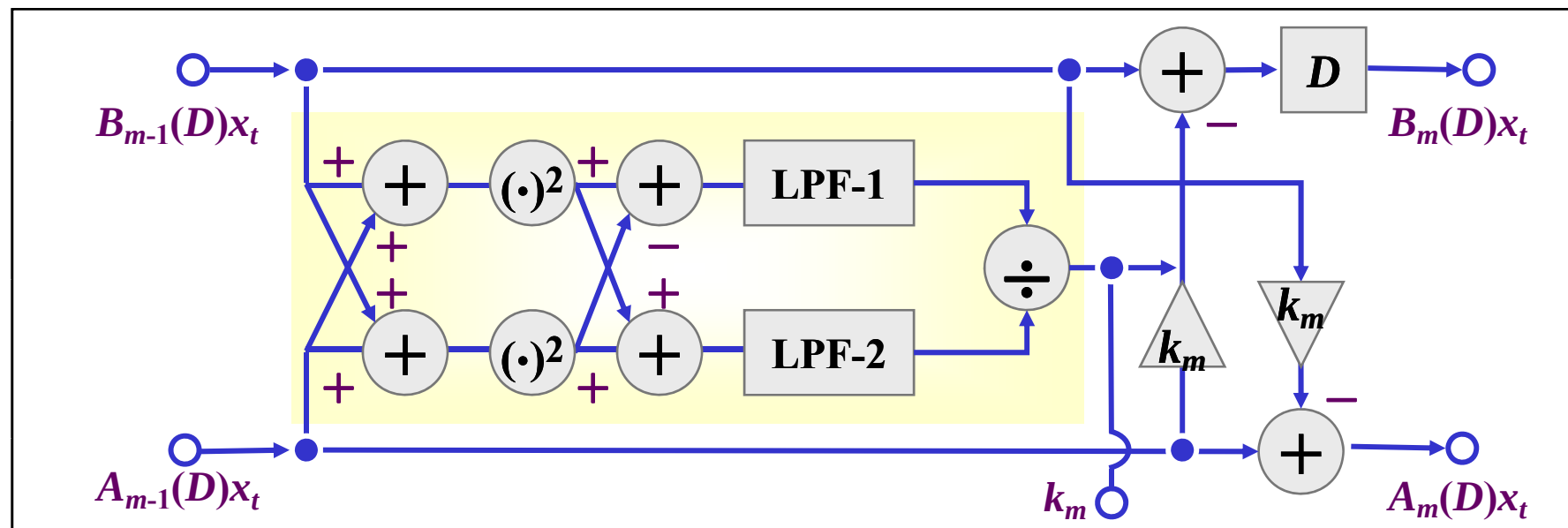
## Definition of PARCOR coefficients

# Flowchart for calculating $\{k_m\}_{i=0}^p$ and $\{\alpha_i\}_{i=0}^p$ from $\{v_i\}_{i=0}^p$

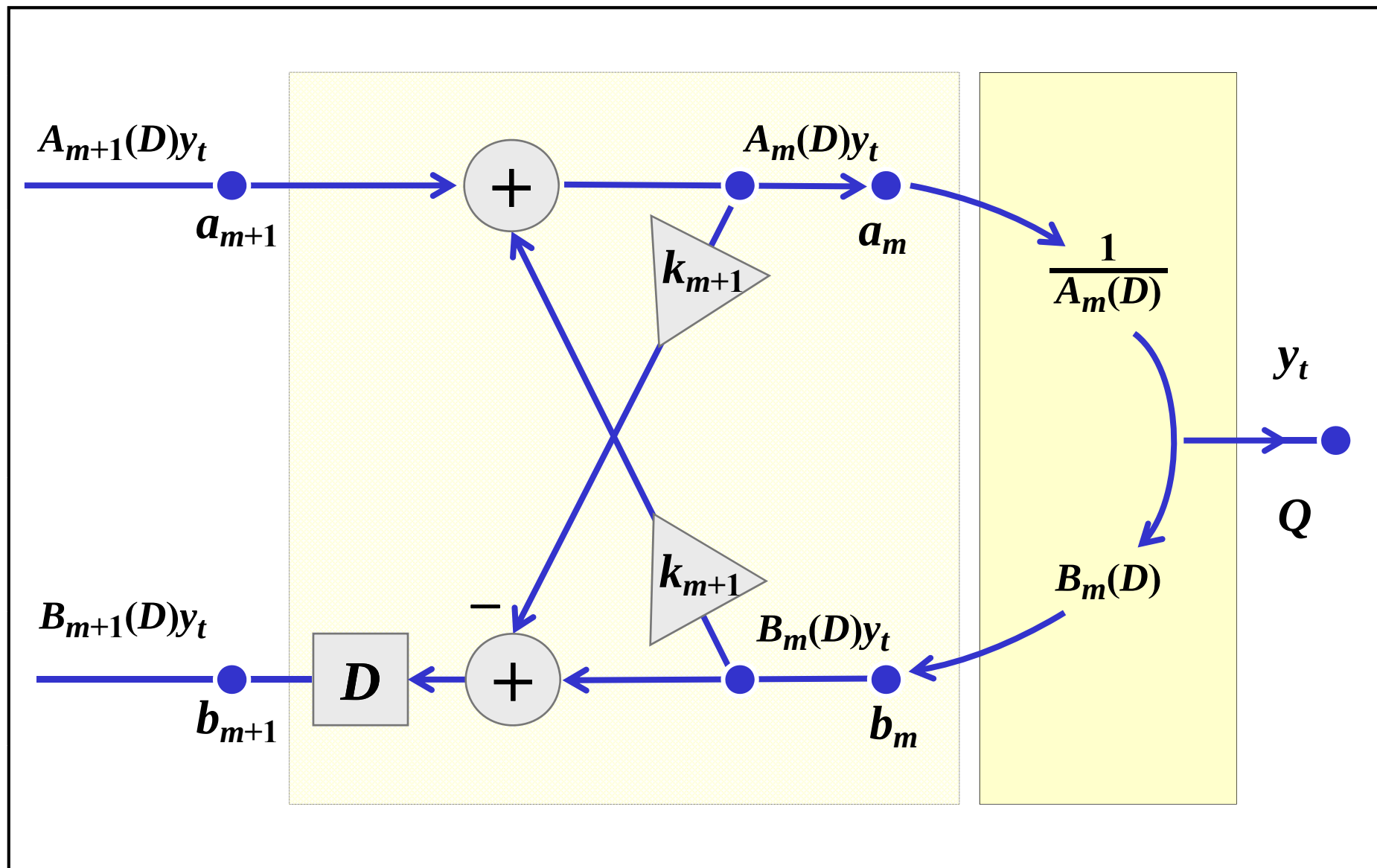




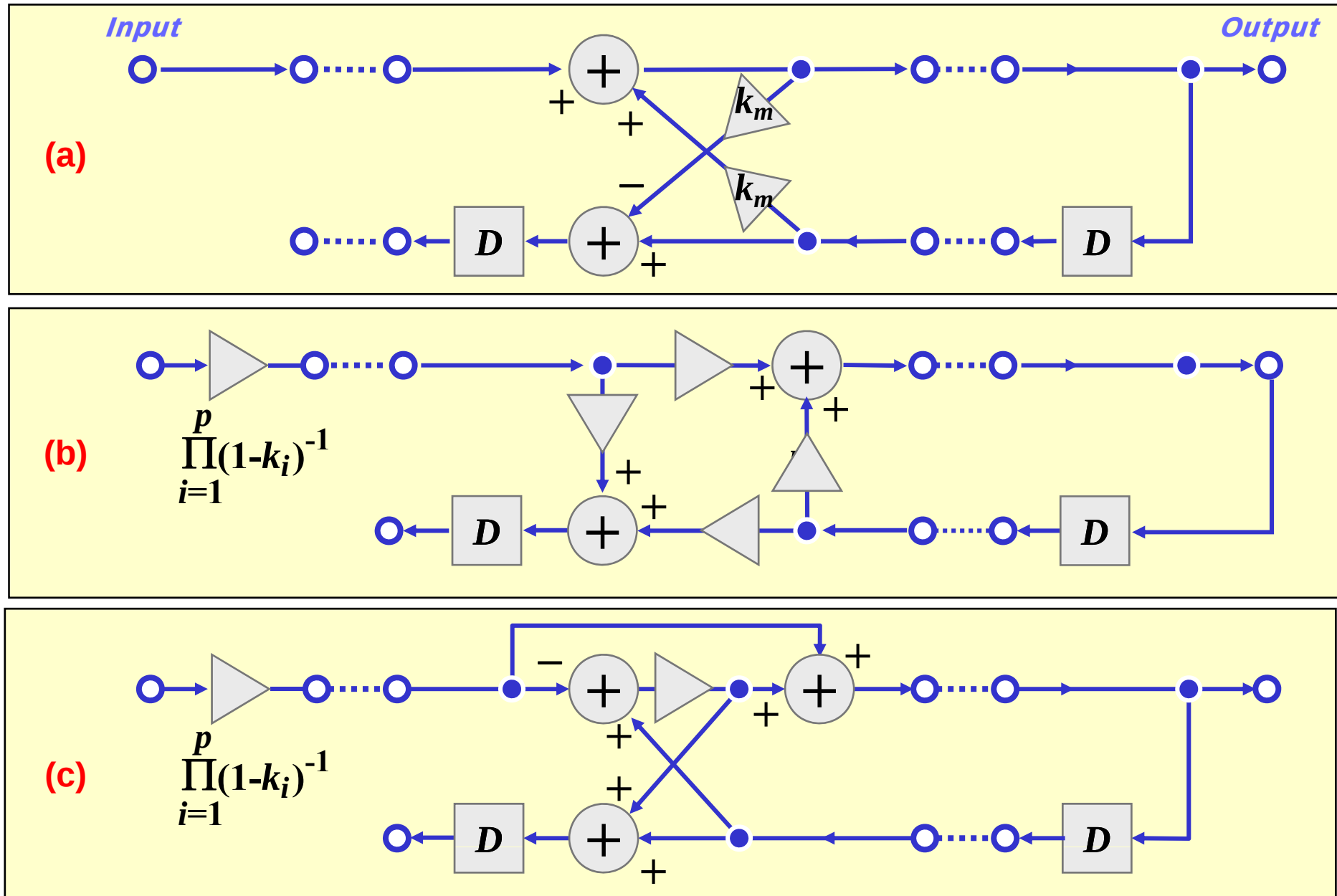
(a) PARCOR coefficient extraction circuit constructed by cascade connection of partial autocorrelators



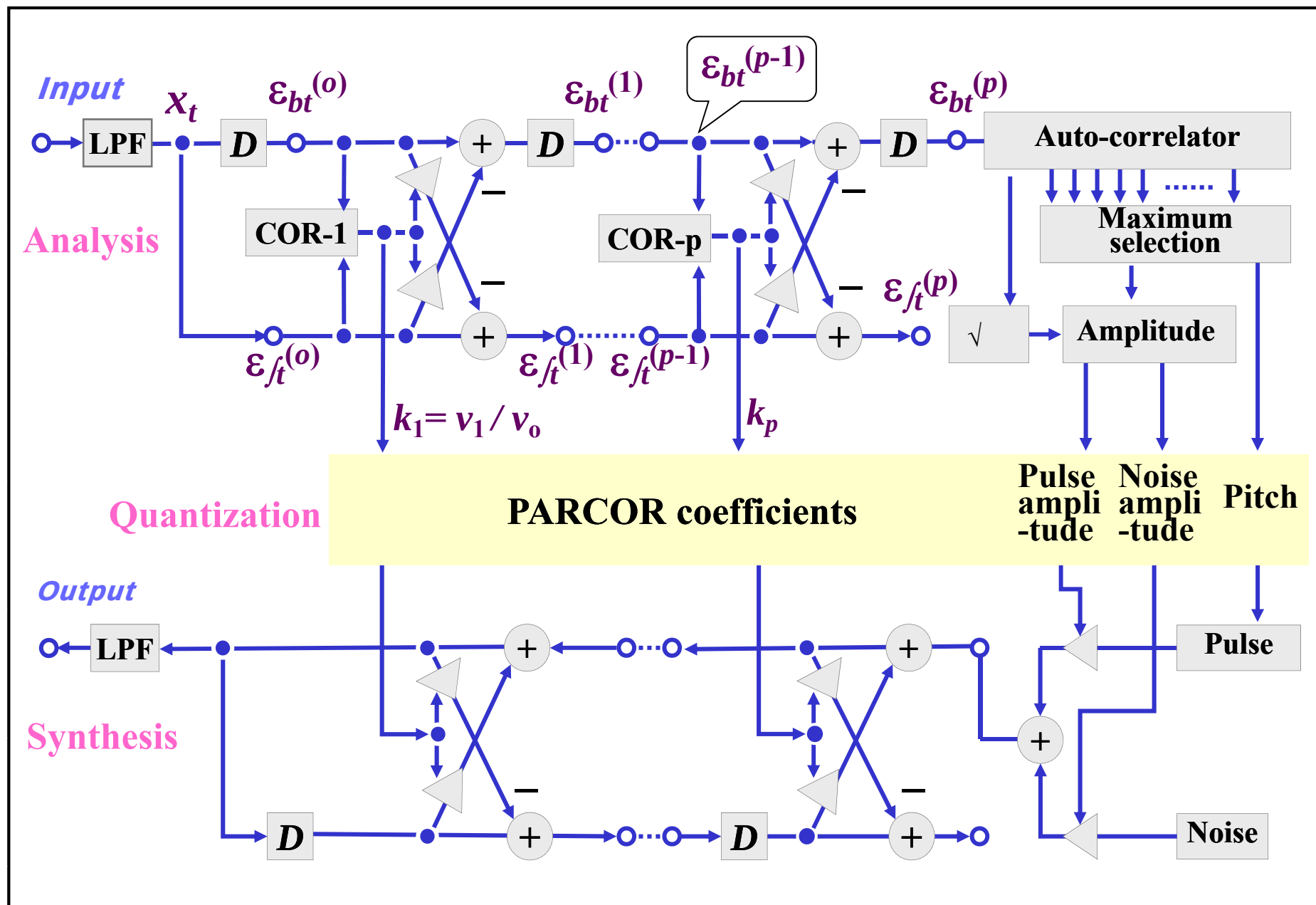
(b) Construction of each partial autocorrelator



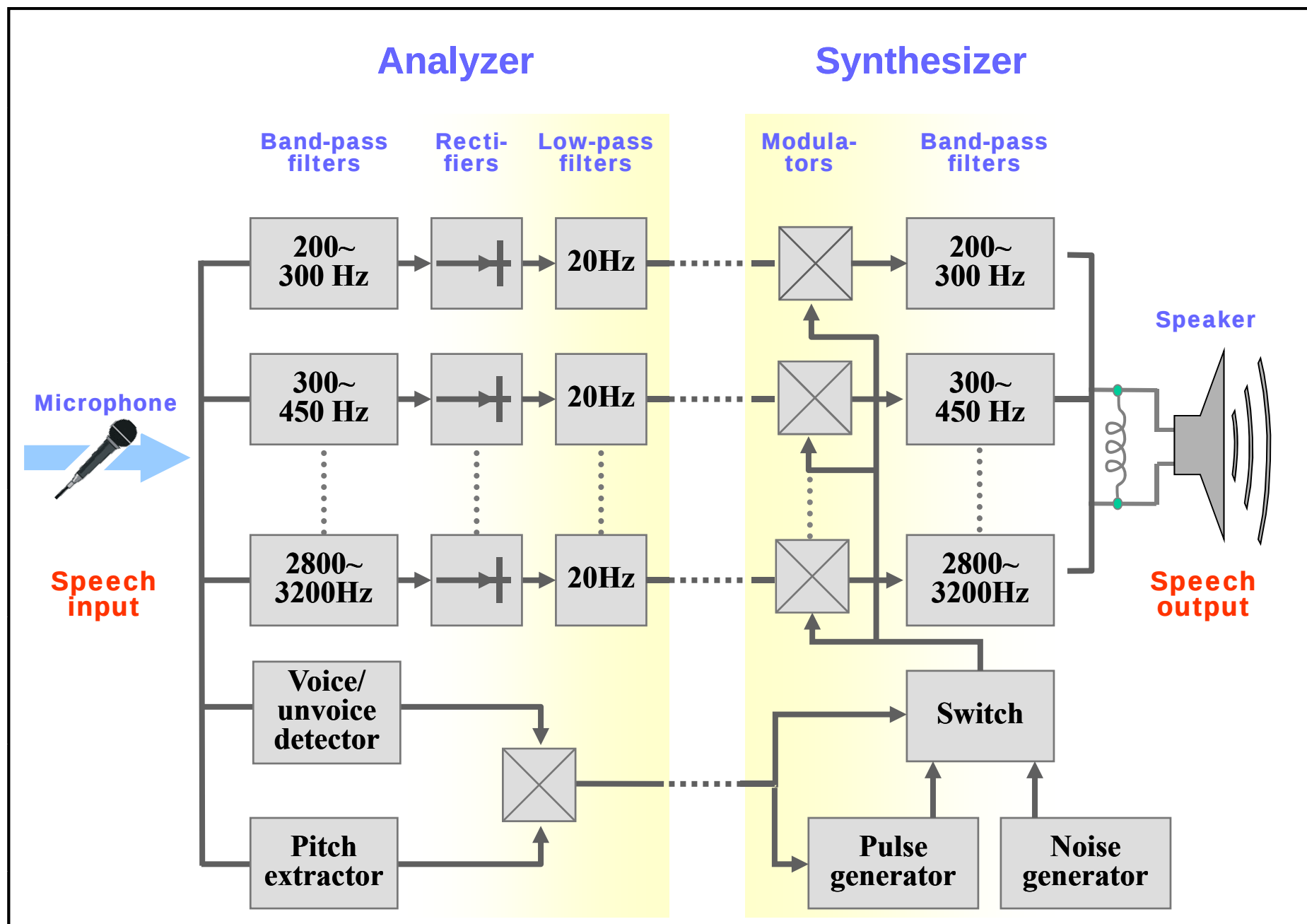
Principal construction features of synthesis filter  
using PARCOR coefficients



**Equivalent transformations for lattice-type digital filter**

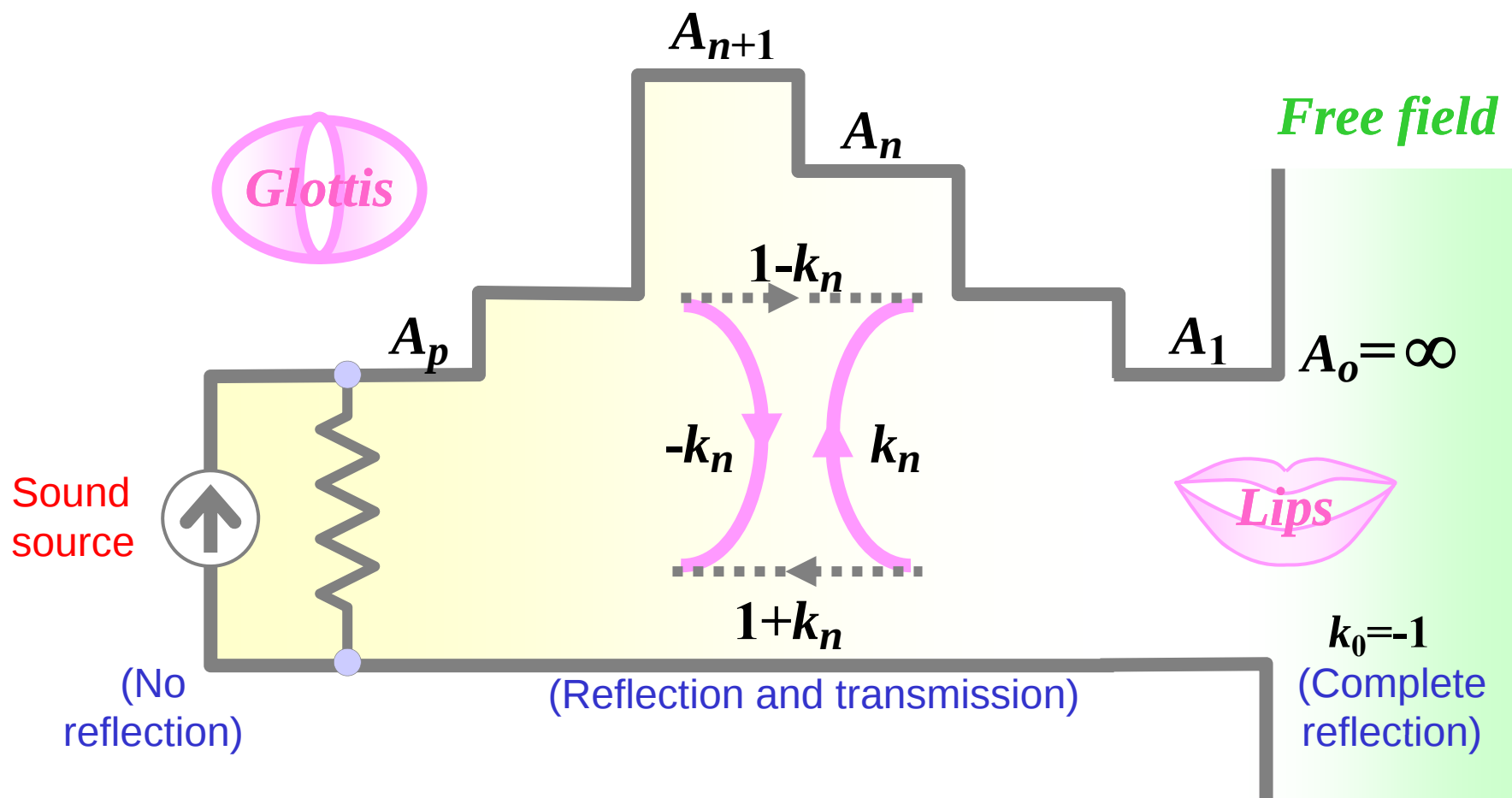


Structure of PARCOR analysis-synthesis system



**Structure of the (channel) vocoder**

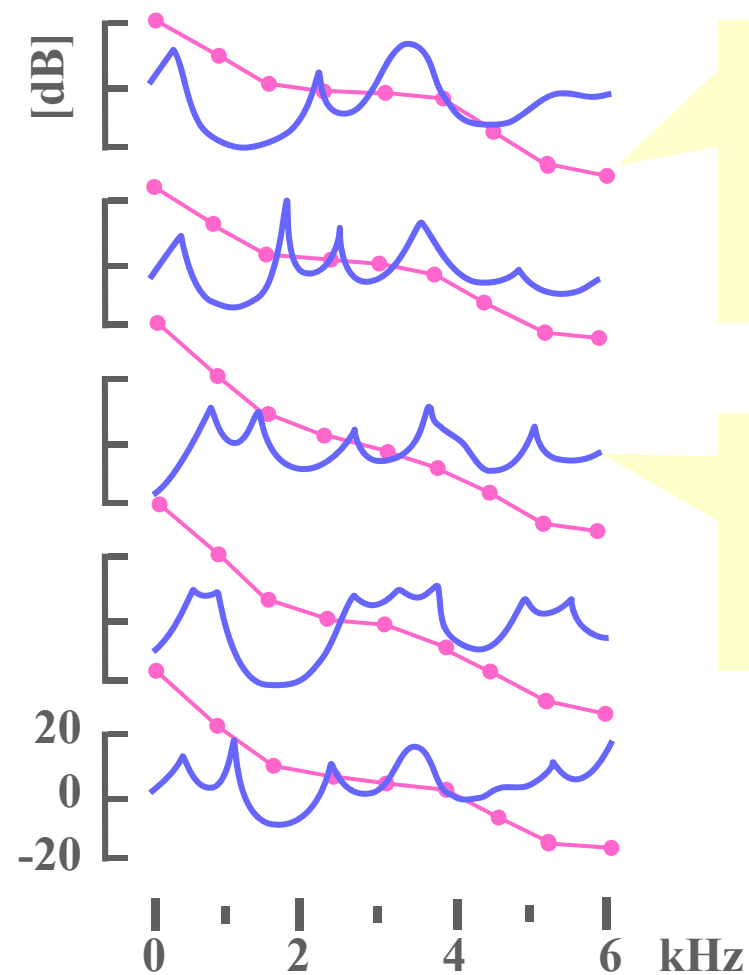
# Relationship between PARCOR coefficients $\{k_n\}$ and vocal tract area function $\{A_n\}$



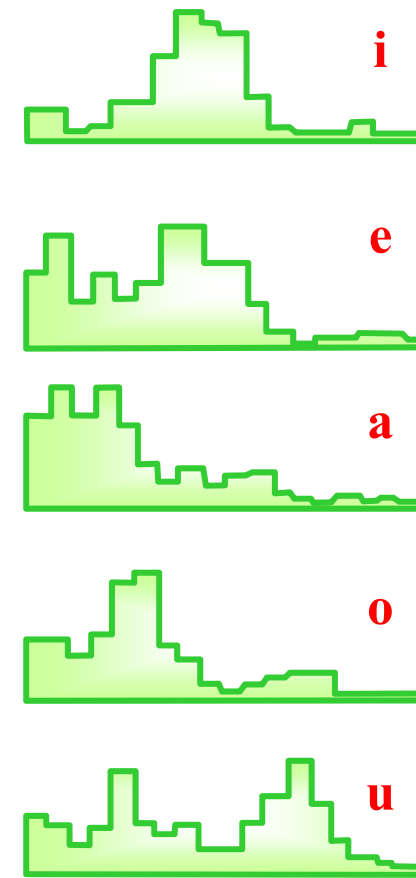
$$k_n = \frac{A_{n+1} - A_n}{A_{n+1} + A_n}$$

# Examples of spectral envelopes and estimated area function for five vowels

0106-17

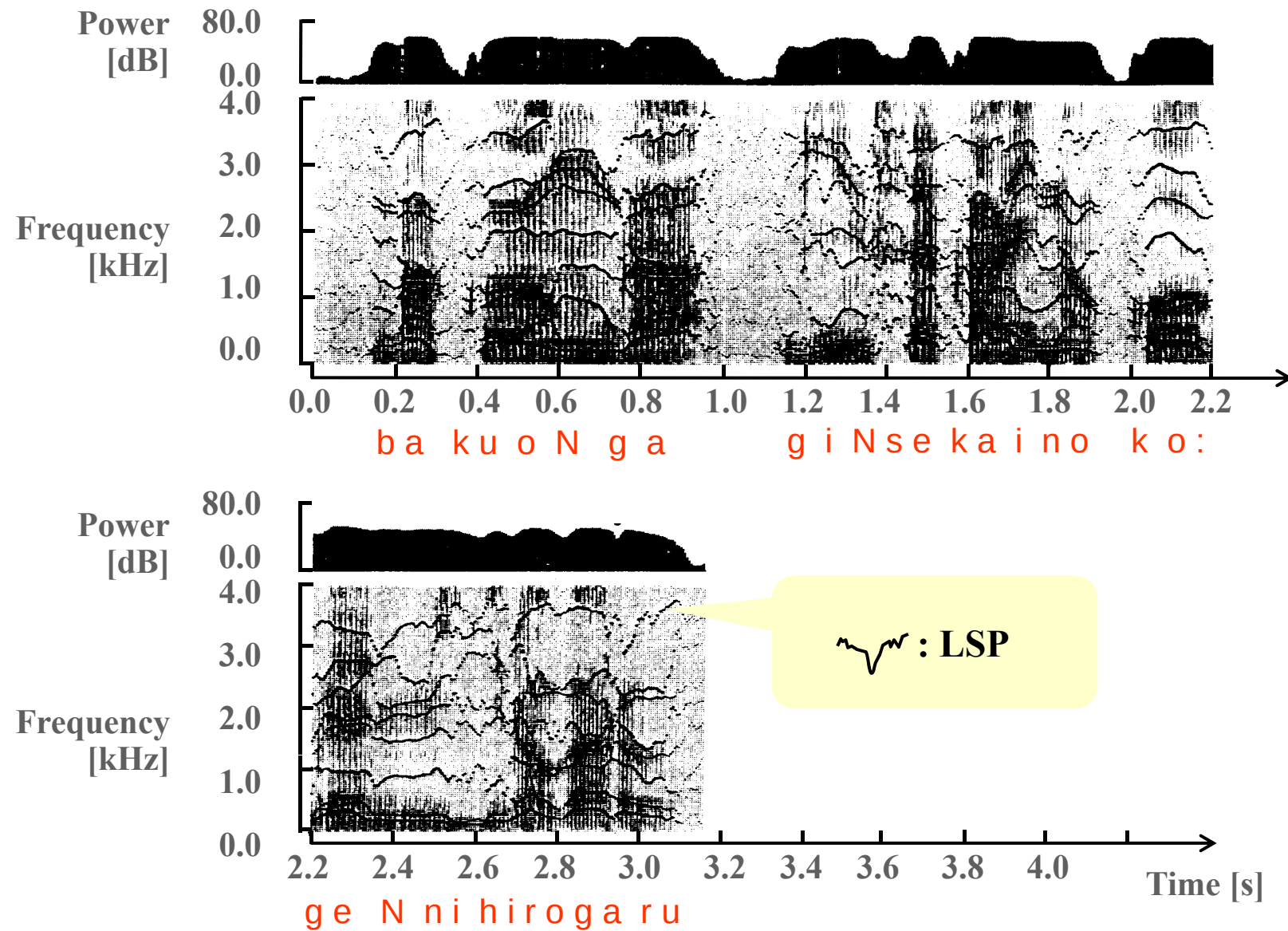


Spectrum

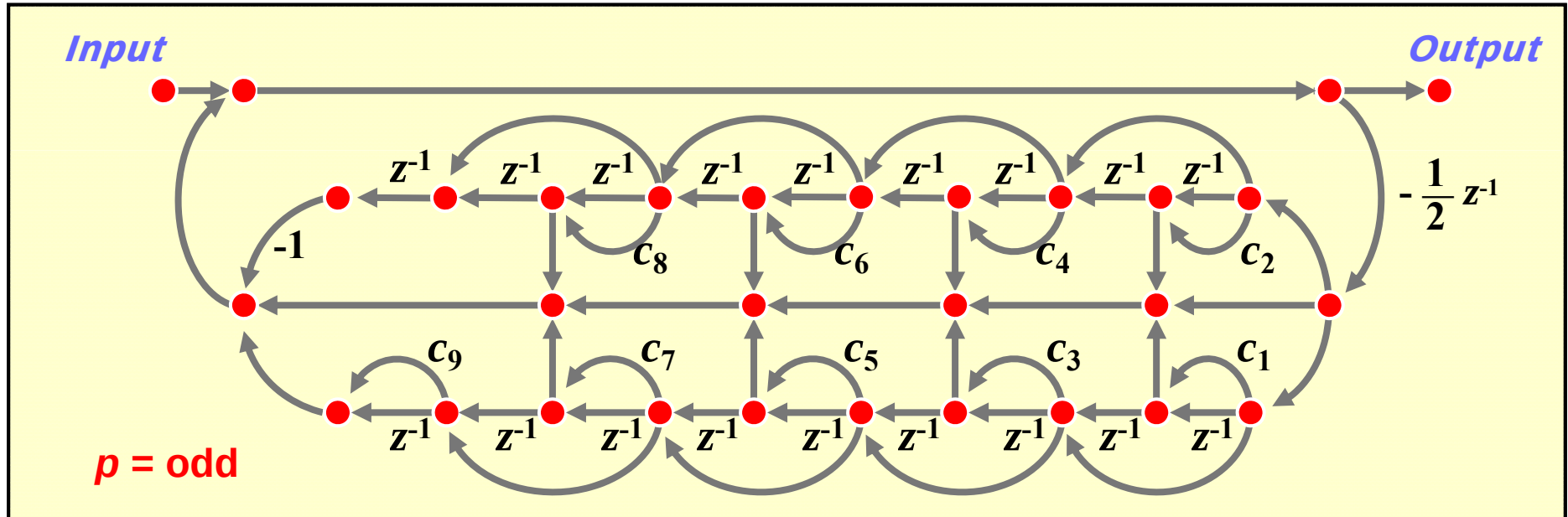
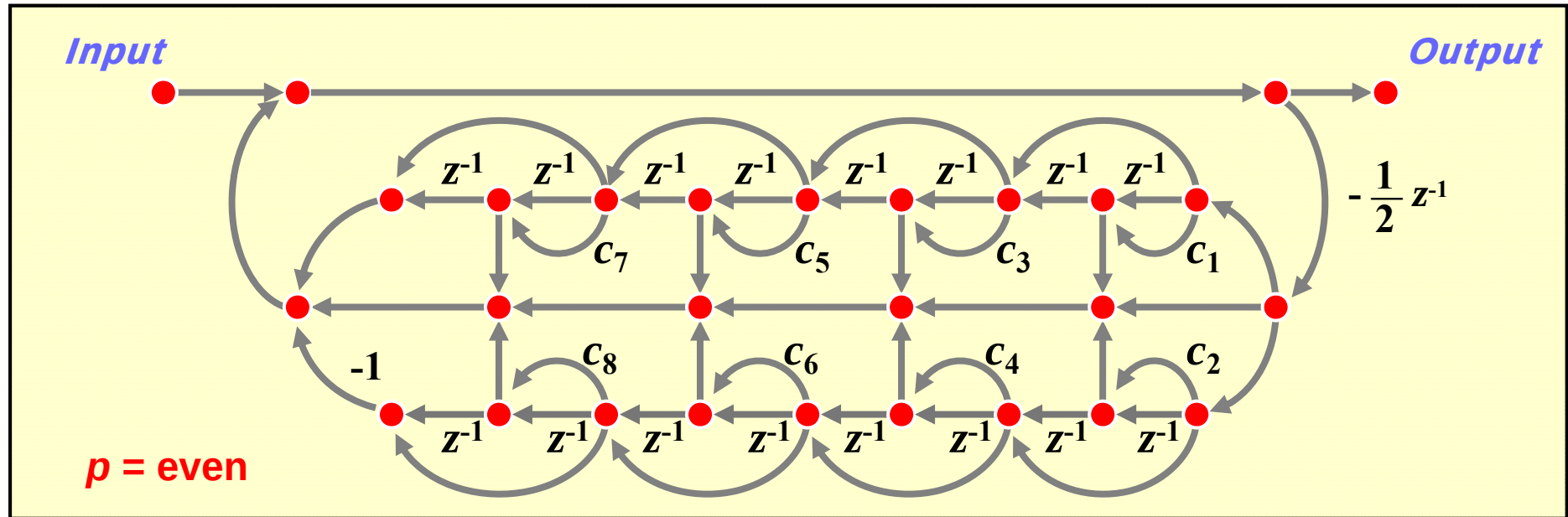


Estimated area function

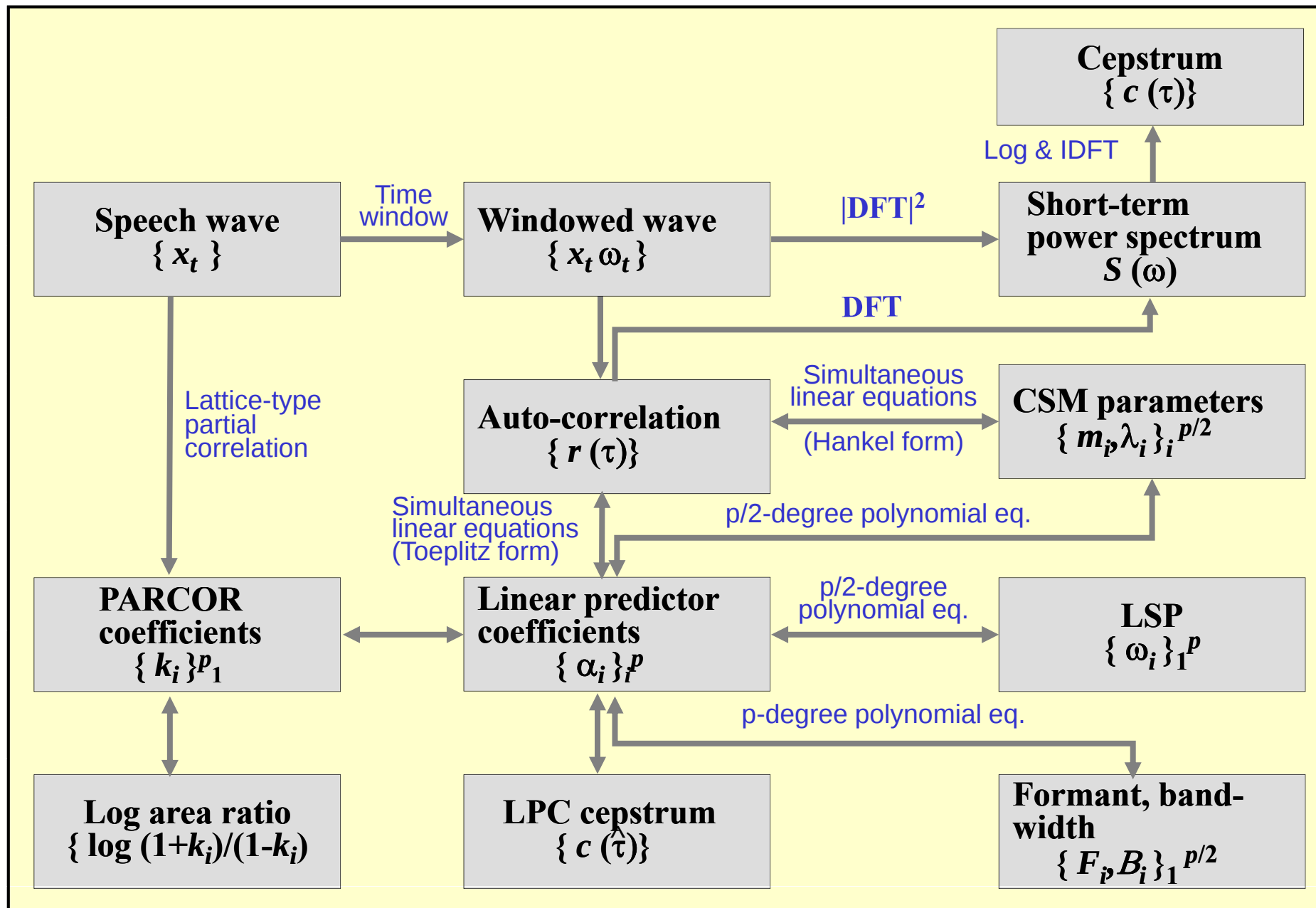




An example of LSP analysis



Signal flow graph of LSP synthesis filter



**Mutual relationships between parameters  
based on all-pole spectrum modeling**