



# Computational Fluid Dynamics

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## Schedule (1)

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- Classification of Partial Differential Equations
- Discretization in space and time
- Finite Difference Method
- Diffusion Equation
- Advection Equation
- Poisson Equation

2

- 1-D and 2-D Burgers Equations
- Shallow Water Equation
- Incompressible Navier-Stokes Equation
- Visualization

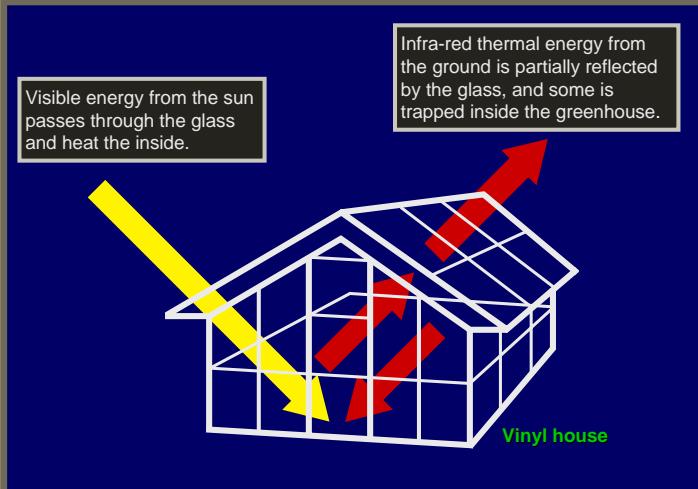


In XXXX, Manhattan, New York



3

# GREENHOUSE EFFECT



# Environmental Problems

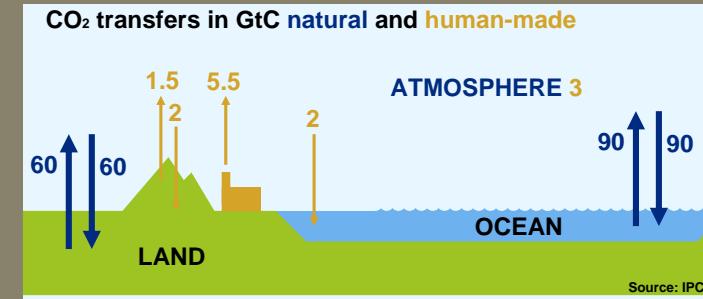
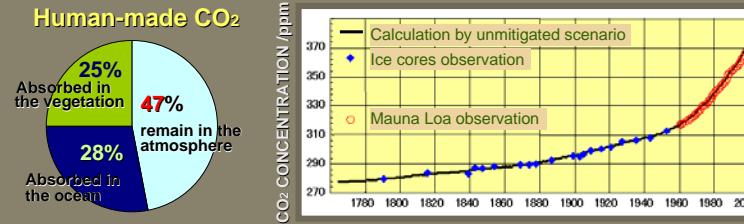
## Human activity

- Climate Change
    - global warming
  - Air pollution
    - Acid rain
    - Ozone hole

## Natural Phenomena

- Meteorological Disasters
    - Heavy rain, Drought
  - Diastrophism
    - Earthquake
    - Volcanism

# NATURAL AND HUMAN-MADE CYCLE OF CARBON



Source: IPCC

# Fastest Supercomputer in the world



In 2002 June

No.1	Earth Simulator	Japan (Jamstec)	(NEC)	35.86 TFlops
No.2	ASCI White	USA (LLNL)	(IBM Power 3)	7.23 TFlops
No.3	Alpha Server	USA (Pittsburg SC)	(Alpha)	4.46 TFlops



# Latest Top500

2005 November

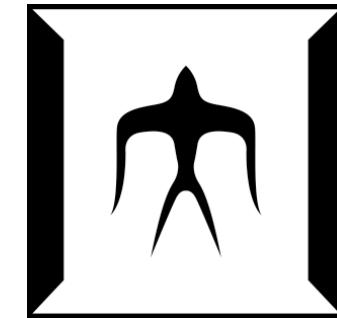
No.1	BlueGene/L	USA (DOE) (IBM)	280.60 TFlops
No.2	BlueGene/L	USA (IBM Watson) (IBM)	91.29 TFlops
No.3	ASCI -Purple	USA (DOE) (IBM)	63.39 TFlops
No.4	Colombia	USA (NASA) (SGI)	51.87 TFlops
No.5	Thunderbird	USA (Sandia) (Dell)	38.27 TFlops
No.6	Red Storm d	USA (Sandia) (Cray)	36.19 TFlops
No.7	Earth Simulator	Japan (Jamstec) (NEC)	35.86 TFlops
No.8	MareNostrum	Spain (Balserona) (IBM)	27.91 TFlops

BlueGene/L - eServer (IBM)      Power 4 × 131,072 CPU



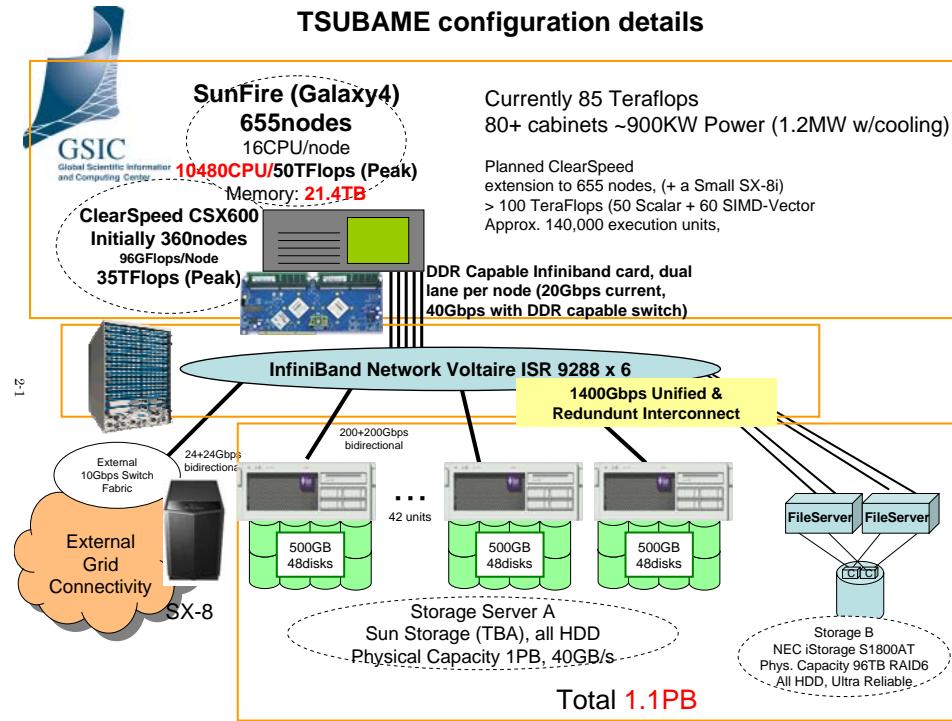
## TSUBAME Grid Cluster

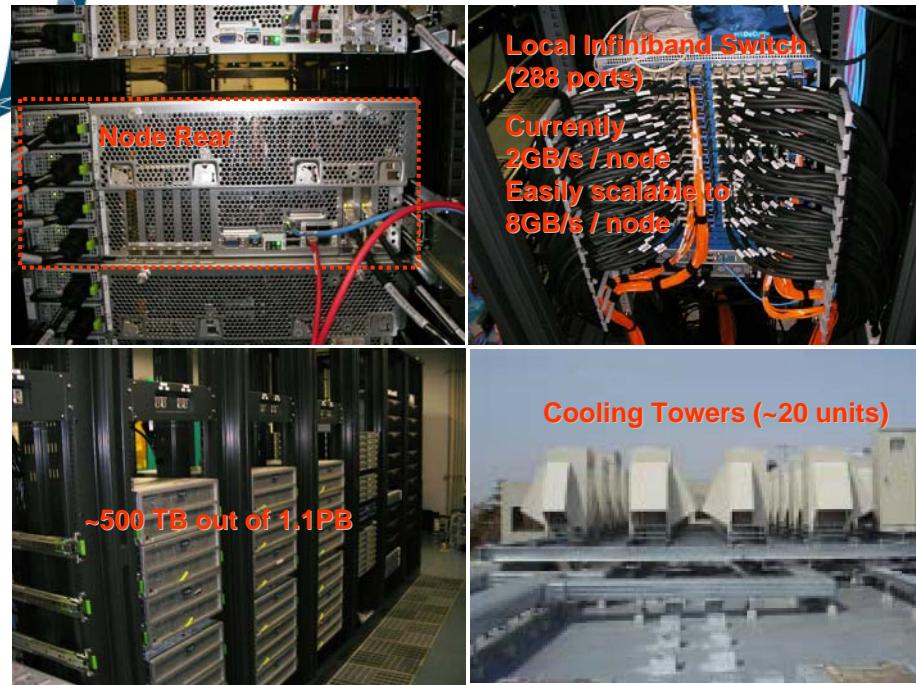
- Tokyo-tech
- Supercomputer and
- UBiquitously
- Accessible
- Mass-storage
- Environment



**TSUBAME** means swallow in Japanese,  
Tokyo-tech symbol is swallow.

### TSUBAME configuration details





TSUBAME is #7 Fastest in World

Linpack is used as a performance measure in ranking

		N	NB	P	Q	Time	Gflops
	WR10R2R4	1334160	240	36	144	41462.22	3.818e+04
Rank	Site	Computer	Processors	Year	R <sub>max</sub>	R <sub>peak</sub>	
1	DOE/NNSA/LNL United States	BlueGene/L - eServer Blue Gene Solution	131072	2005	280600	367000	<ul style="list-style-type: none"> <li>• N : 1334160</li> <li>• NB : 240</li> <li>• PMAP : Row-major process map</li> <li>• P : 36</li> <li>• Q : 144</li> <li>• RFACT : Right</li> <li>• NBMIN : 4</li> <li>• NDIV : 2</li> <li>• RFACT : Right</li> <li>• BCAST : 1ring</li> <li>• DEPTH : 1</li> <li>• SWAP : Mix (threshold = 240)</li> <li>• L1 : transposed form</li> <li>• U : transposed form</li> <li>• EQUIL : yes</li> <li>• ALIGN : 8 DP words</li> </ul>
2	IBM Thomas J. Watson Research Center United States	BGW - eServer Blue Gene Solution	40960	2005	91290	114688	
3	DOE/NNSA/LNL United States	ASC Purple - eServer pSeries p5 575 1.9 GHz	12208	2006	75760	92781	
4	NASA/Ames Research Center/NAS United States	Columbia - SGI Altix 1.5 GHz, Voltaire Infiniband	10160	2004	51870	60960	
5	Commissariat à l'Energie Atomique (CEA) France	Tera-10 - NovaScale 5160, Itanium2 1.6 GHz, Quadrics	8704	2006	42900	55705.6	
6	Sandia National Laboratories United States	Thunderbird - PowerEdge 1850, 3.6 GHz, Infiniband	9024	2006	38270	64972.8	
7	GSIC Center, Tokyo Institute of Technology Japan	TSUBAME Grid Cluster - Sun Fire X64 Cluster, Opteron 2.4/2.6 GHz, Infiniband	10368	2006	38180	49868.8	
8	Forschungszentrum Juelich (FZJ) Germany	JUBL - eServer Blue Gene Solution	16384	2006	37330	45875	
9	Sandia National Laboratories United States	Red Storm Cray XT3, 2.0 GHz	10880	2005	36190	43520	
10	The Earth Simulator Center Japan	Earth-Simulator	5120	2002	35860	40960	

38.18 TeraFlops

- Opteron Only, 648 nodes
- ~14 Terabytes memory
- 76.56% Efficiency

## High-resolution Typhoon Simulation

**CReSS: Cloud Resolving Storm Simulator**

Non-hydrostatic and compressible equation  
Terrain-following in three dimensional geometry

Prognostic variables:

- three-dimensional velocity components
- perturbation of pressure
- perturbation of potential temperature
- subgrid-scale turbulent kinetic energy, TKE
- mixing ratios for water vapor and several hydrometeors

## Cloud Physics Process

Bulk method of cold rain.

Prognostic variables for mixing ratios :

- water vapor
- cloud water
- rain water
- cloud ice
- snow
- graupel



# Improved Dynamic Process



$$\frac{\partial \bar{\rho} u}{\partial t} + \bar{\rho} \left( u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} \right) = - \frac{\partial p'}{\partial x} + \bar{\rho} (f_s v - f_c w) + Turbu$$

4thFDM+Leap-flog method  
(with Asselin filter)

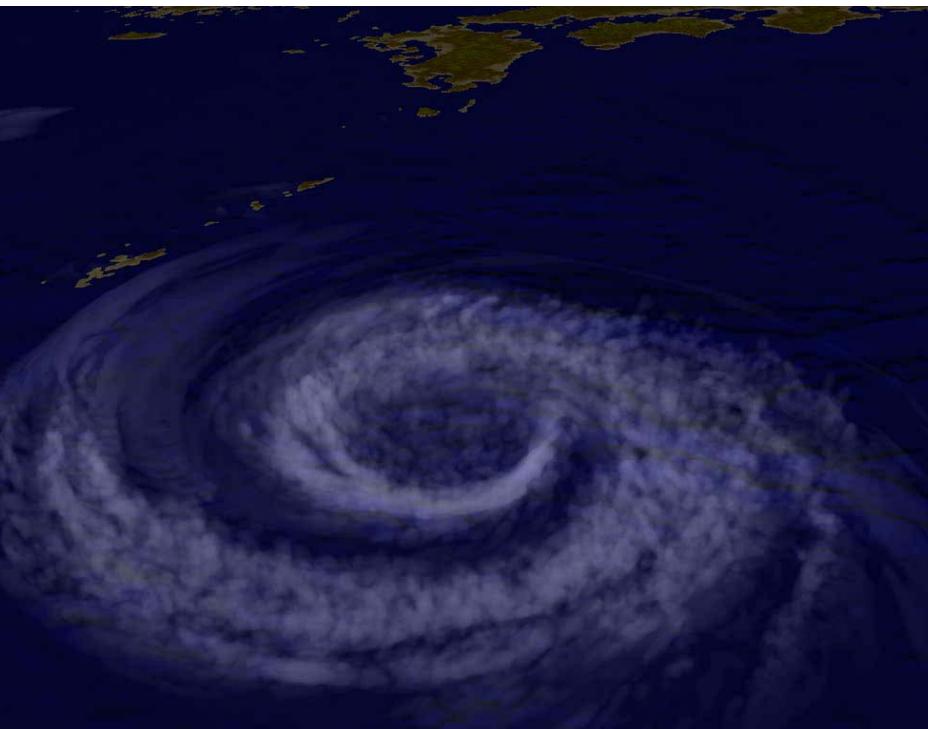
Semi-Lagrangian Scheme  
Cubic-Lagrange, CIP Method



CFL = 0.15

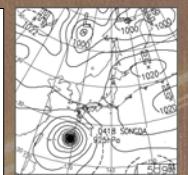
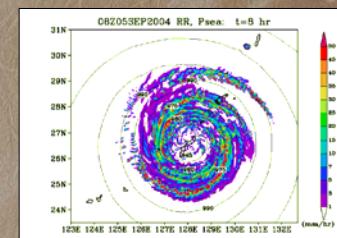
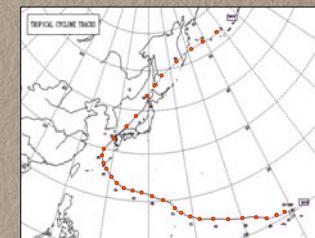


CFL = 0.6



# Typhoon Simulation

#18-typhoon Sep 2004, Sever Damage in Kyushu

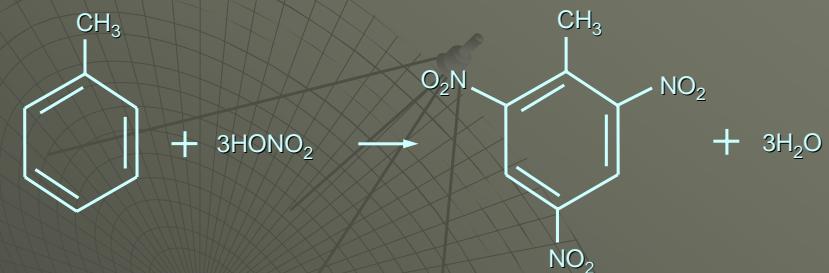


Calculation  
Conditions:

Domain  
H-grid size  
V-grid size  
Grid numbers  
Integration time  
Micro-physics  
Initial condition  
Boundary  
Surface  
Earth Simulator

H: 1000 km × 1000 km × V: 18 km  
1000 m  
200 ~ 300 m (stretched)  
H: 1003 × 1003 × V: 63  
48 hours  
the bulk cold rain type  
JMA Regional Spectral model output  
JMA Regional Spectral model output  
real topography and observed SST  
100 nodes (800 CPU)

# Explosion Simulation

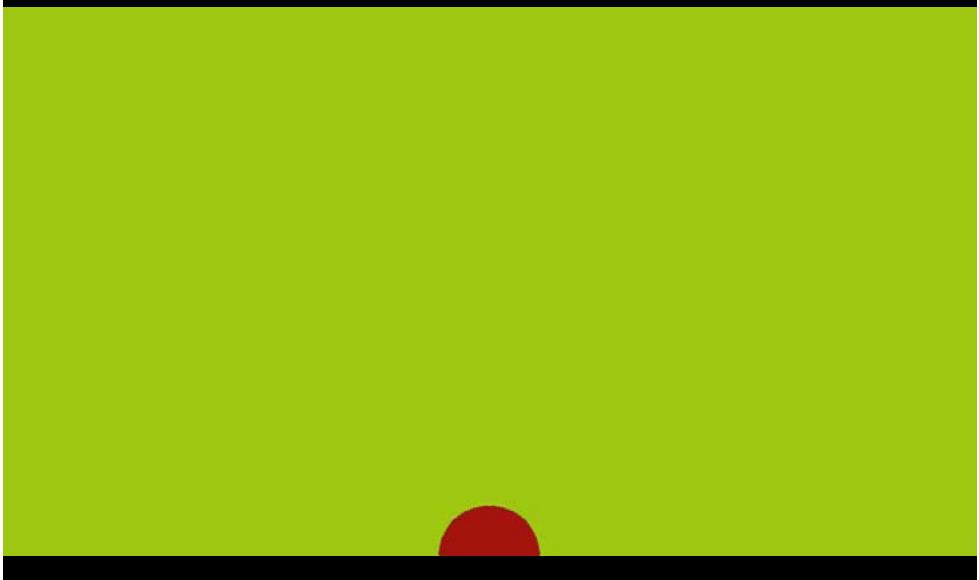


1kg-TNT explosion : 3.22 MJ  
30kg-TNT explosion : 100 MJ

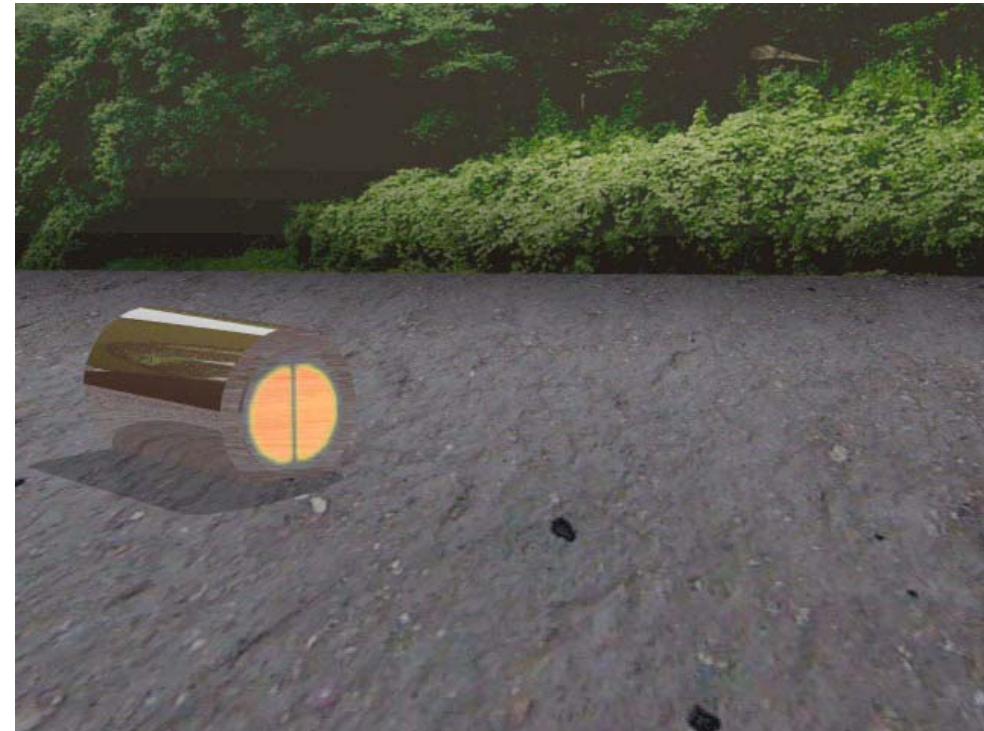
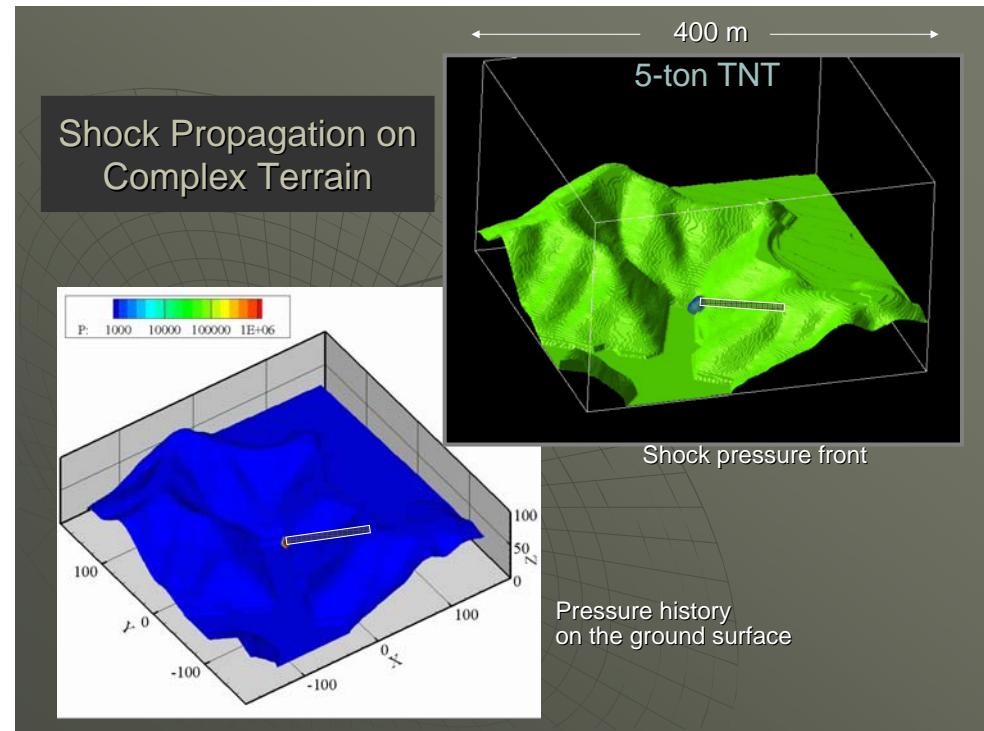
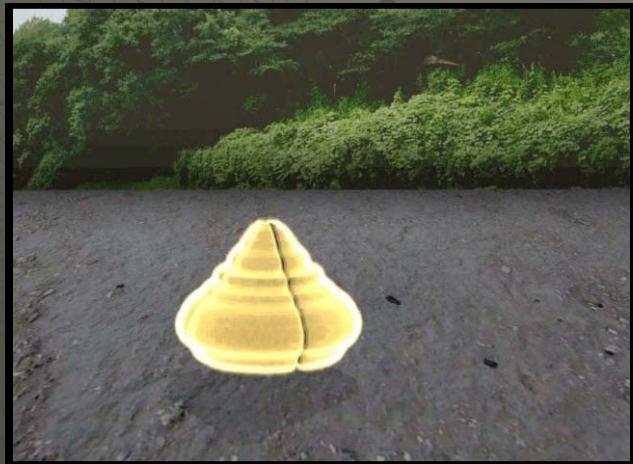
Dangerous and difficult  
experiment

→ Numerical Simulation

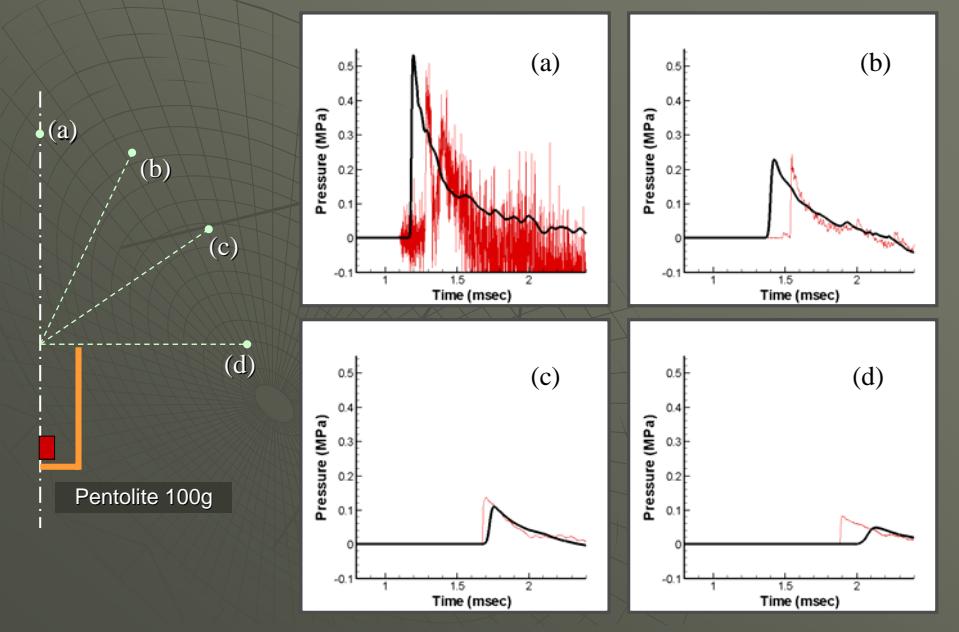
## Blast wave just after explosion in Cylindrical 2-D geometry



## 32kg-TNT EXPLOSION ON THE GROUND



## Comparison with Experiment



## 32kg-TNT Explosion Experiment

Safety test for 32kg-TNT Explosion on the ground.

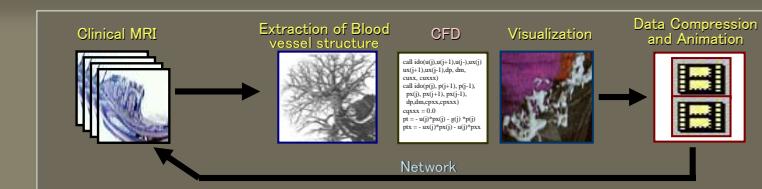
In 2002, December 3,  
In Oita Pref., Hijuu-dai, at Japan  
Ground Self-Defense Force,

The experiment was done by the  
Research Center for Explosion  
and Safety, National Institute of  
Advanced Industrial Science and  
Technology.

Recorded by High Speed Camera.



## Blood Flow Simulation System

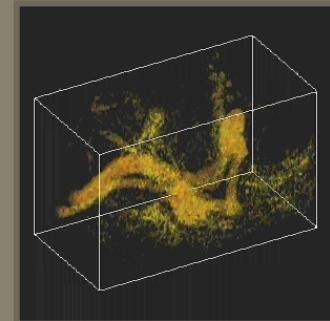
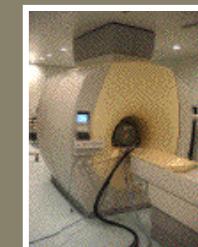


## MRI Facility

### Collaboration :

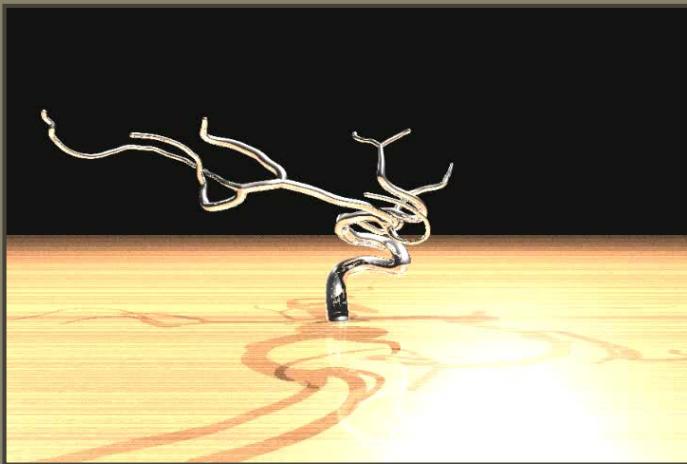
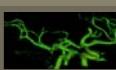
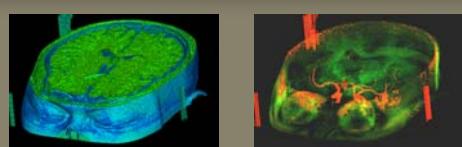
Division of Medical Imaging,  
National Institute of Radiological Sciences,  
Ikehira Lab.

Gyroscan Intera  
1.5T Philips

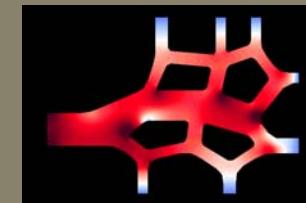


4-D MRI processing synchronizing  
electrocardiograph

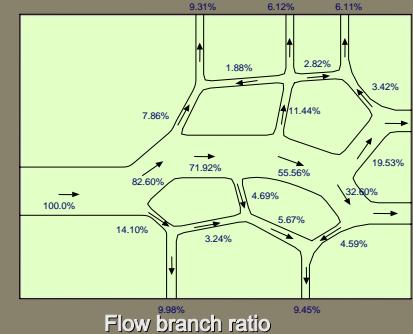
## Extraction of Blood Vessel Structure from Voxel data



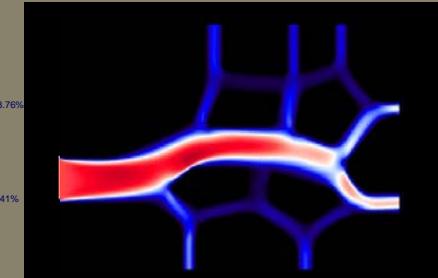
## Blood Flow With Complex Branches



Pressure Profile

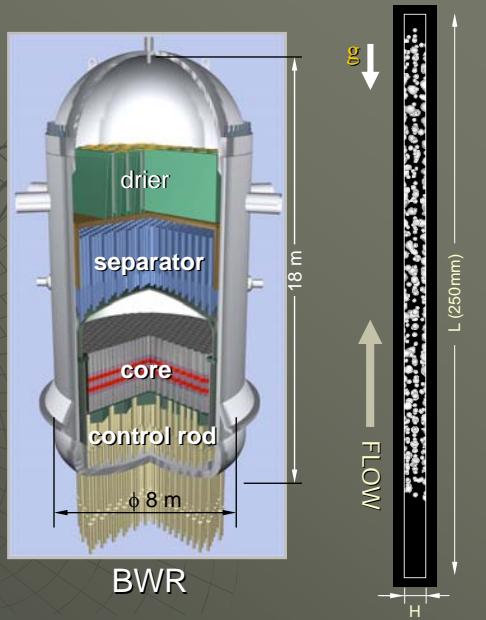


Flow Velocities



## Bubbly Flow Simulation

- Channel Width (H) 10 mm
- Channel Length (L) 250 mm
- Mesh Size : 0.25 mm
- Mesh Number :  $40 \times 40 \times 1000$
- Equal grid spacing
- Incoming Flow Velocity : 0.5 m/sec
- Wall Boundary condition: non-slip
- Periodic in the gravity direction
- Room Temperature
- No thermal process
- Initial Condition
  - Average Void Ratio : 0.1
  - Diameter of bubble : 2 mm
  - Number of bubbles : 594  
(=66 stages X 9)



## Computational Methods

- Gas – Liquid Unified Solver : CIP (CCUP) method
- 3-dimentional Compressible / Incompressible fluid
- Surface Tension : CFS model
- Contact angle between wall and bubbles
- Surface tracking method : improved VOF method

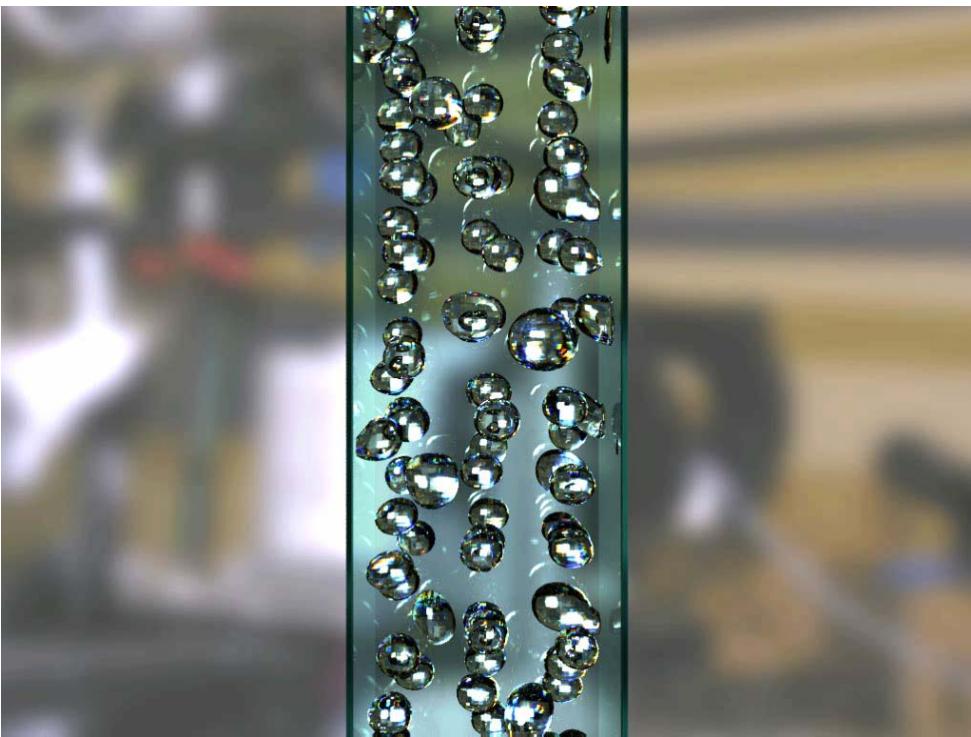
$$\frac{\partial \rho_l \phi_l}{\partial t} + \nabla \cdot (\rho_l \phi_l \mathbf{u}) = 0$$

$$\frac{Du_i}{Dt} = -\frac{1}{\rho} \frac{\partial p}{\partial x_i} + \frac{1}{\rho} \frac{\partial \tau_{ij}}{\partial x_j} + g_i + \sigma_i$$

$$\frac{\partial \rho_g \phi_g}{\partial t} + \nabla \cdot (\rho_g \phi_g \mathbf{u}) = 0$$

$$\frac{De}{Dt} = -\frac{p}{\rho} \frac{\partial u_i}{\partial x_i} + \frac{1}{\rho} \frac{\partial}{\partial x_i} \left( \lambda \frac{\partial T}{\partial x_i} \right) + q$$

$$\rho = \rho_l \phi_l + \rho_g \phi_g \quad \phi_l + \phi_g = 1$$



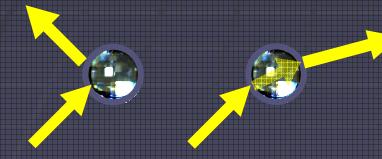
## Ray Tracing Visualization

Free Software

**POV-Ray 3.6**



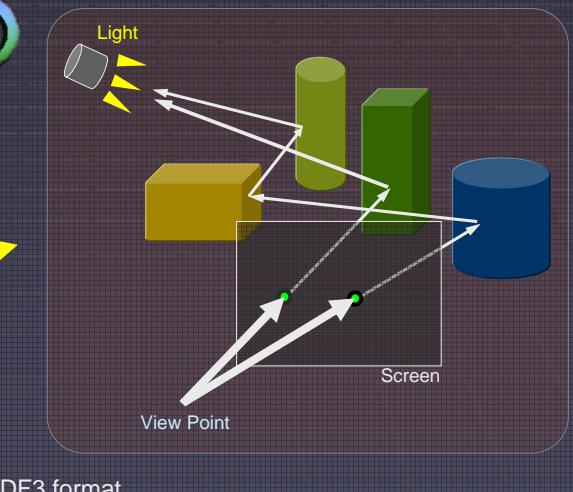
Tracing light ray correctly  
and reproducing optics.



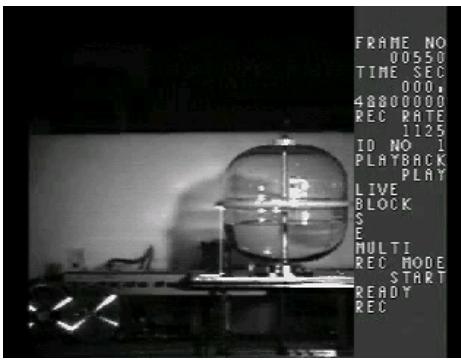
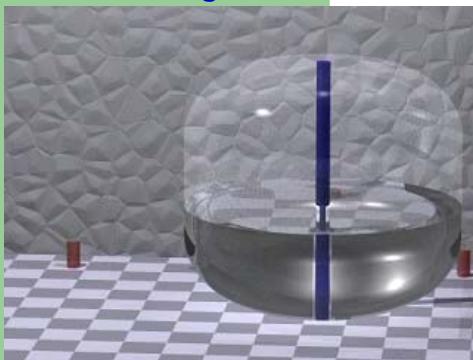
Reflection

Refraction

Void Ratio data → Voxel DF3 format

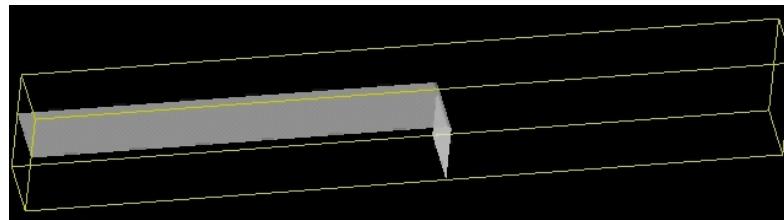


### Sloshing



Prof. Takehiro Himeno (Univ. of Tokyo)

### Non-linear wave



Prof. F. Xiao  
(Tokyo Tech)

## Navigating Ship Simulation

Computational Ship Hydrodynamics  
Moving Body interacting ocean flow, free surface



NMRI Japan  
Dr. Takizawa

# Simulation for Falling Leaves

## Major difficulties:

- Fluid-structure interaction
- Complex shape of leaves
- Very thin structure

Shape of the leaf :  
modeled by  
Geometry data

200 polygons  
DXF or STL CAD format

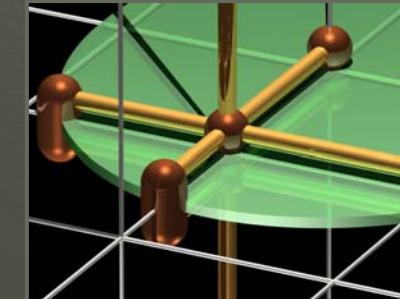
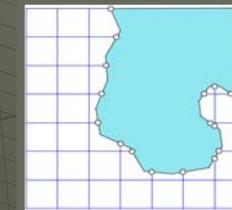
Computational Mother Domain: 50x50x80  
Computational Sub-Domain: 40x40x30



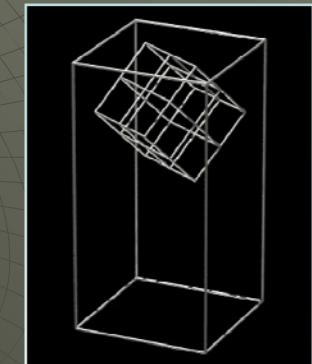
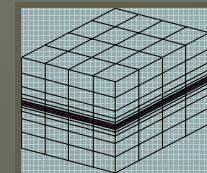
## Some techniques

### InterGrid (Cut Cell)

Two values at the same position,  
representing the  
front and the rear  
surface pressure.



### Overset grid



## DO Experiment

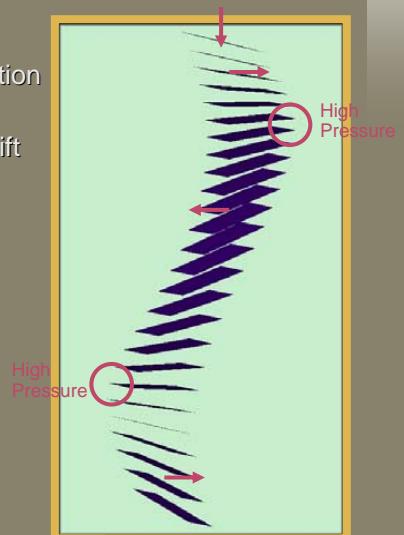
### A Preliminary Simulation:

A Falling Piece of Paper  
for example, a Name Card

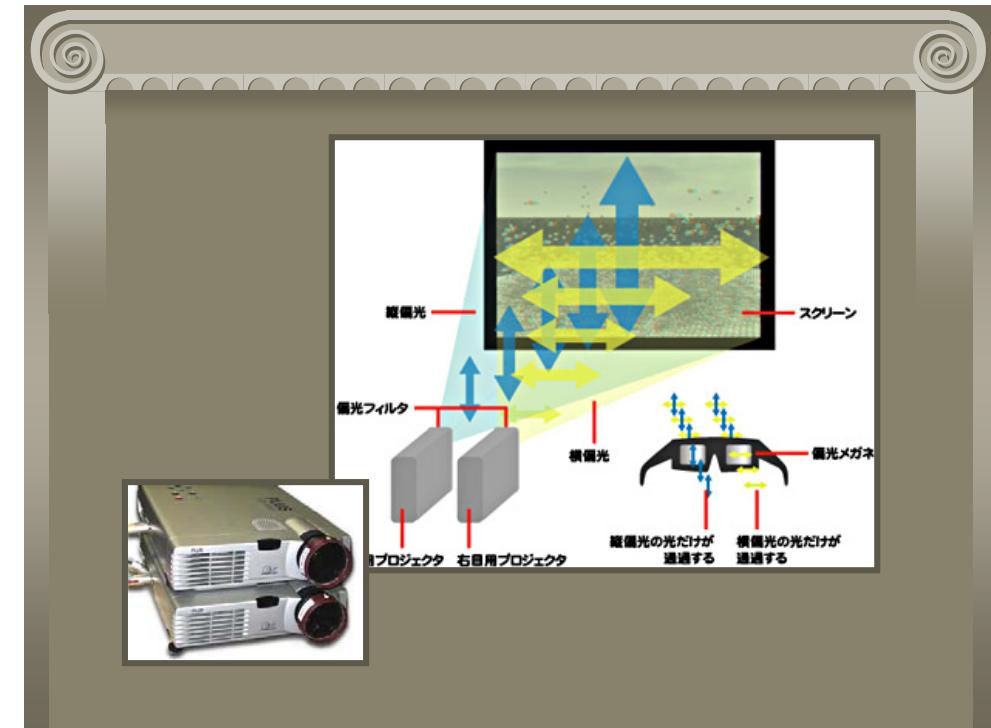


## Mechanism of Flattering

- Start to fall with gravity acceleration
- Transverse acceleration by the lift force due to an attack angle
- Deceleration by the drag due to pressure and friction
- Torque Generation
- Inverse attack angle
- Transverse acceleration in the inverse direction



## 3D Visualization



## Anaglyph # 2



## Particle Simulation for Disasters

Structure destruction by Landslide, Boulder flow,  
Crater formation by a meteorite impact

- ◆ Fluid like behavior of Granular

- ◆ Structure Destruction

(Continuous model is not applicable)

- Crack growth
- Amputation
- Shear
- Smashing

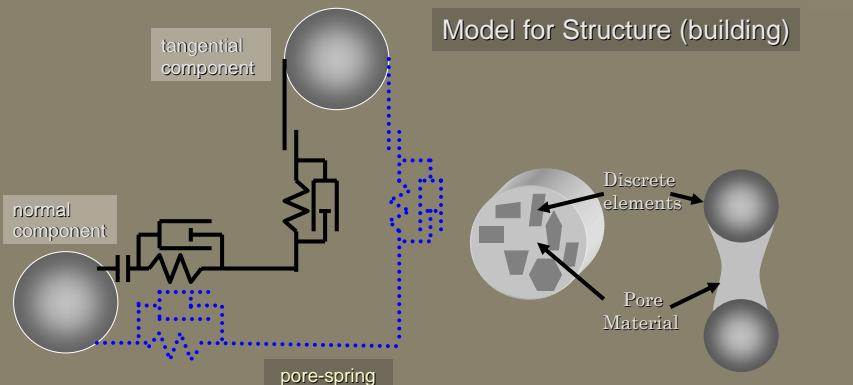


## eDEM

(Extended Discrete Element Method)

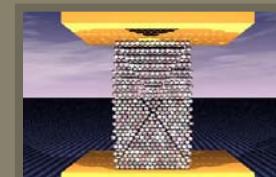
Model for Granular (Sand, etc)

Model for Structure (building)

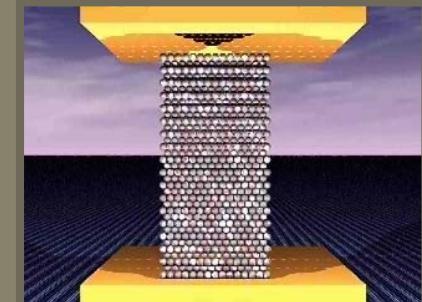


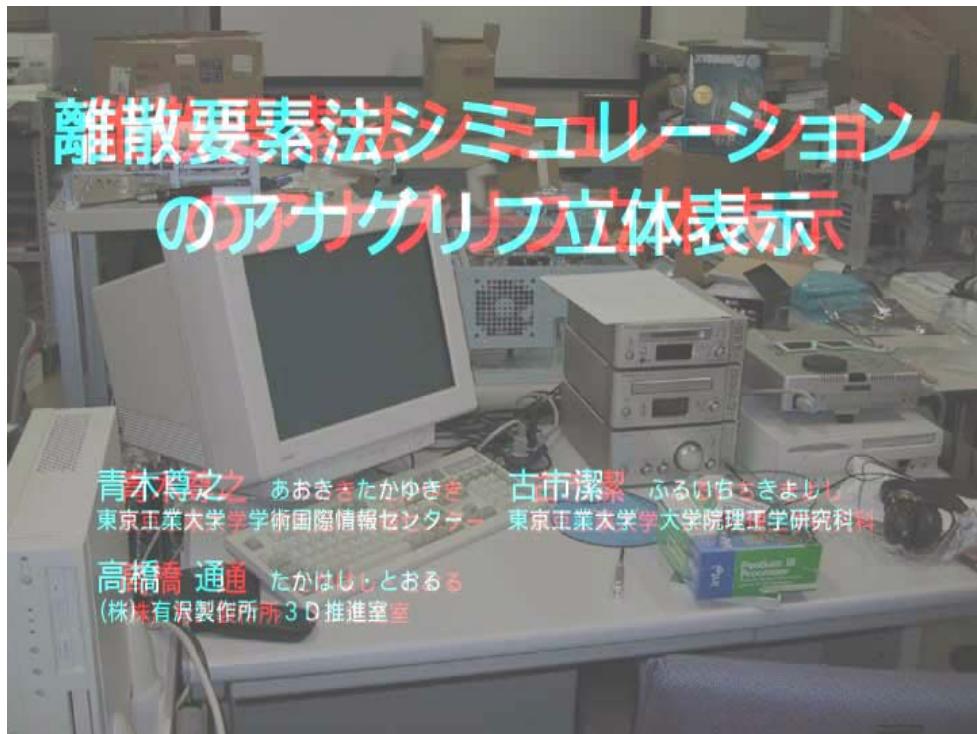
## Compression Test of Concrete Structure

Check for Destruction model



Shear Band (Dilatancy)





## Rock Fall Simulation

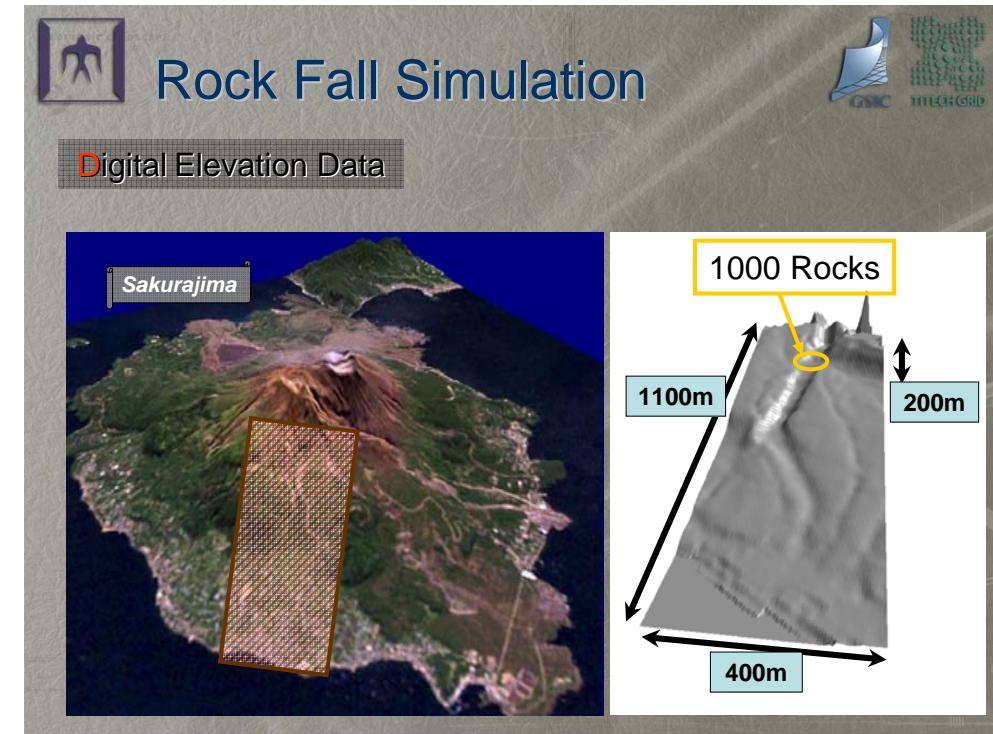
**Rock Fall : One of slope disasters**

**Prevention**

- ▶ Control of Sediments  
exp : fence, wall, net
- ▶ Improvement of Hazard Map

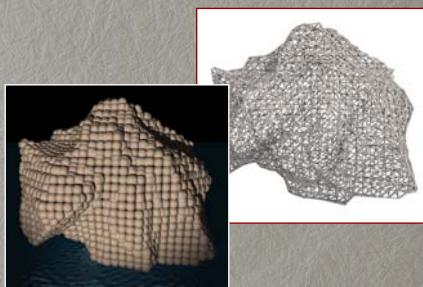
**Numerical Simulation : effective tool**

Aug 25, 1997

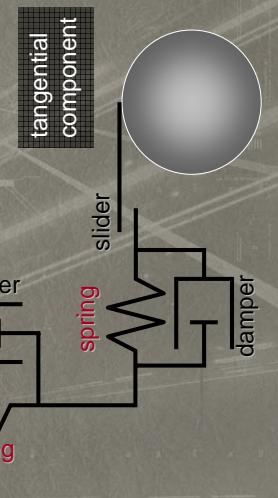




## Non-Spherical Rock Model



DEM Discrete Element Method



Summation for all the particles

Translational and  
Rotational motion of rocks

Quaternion

$$\tilde{Q} = Q_x + Q_t \mathbf{i} + Q_u \mathbf{j} + Q_v \mathbf{k}$$

normal  
component

damper

spring

slider

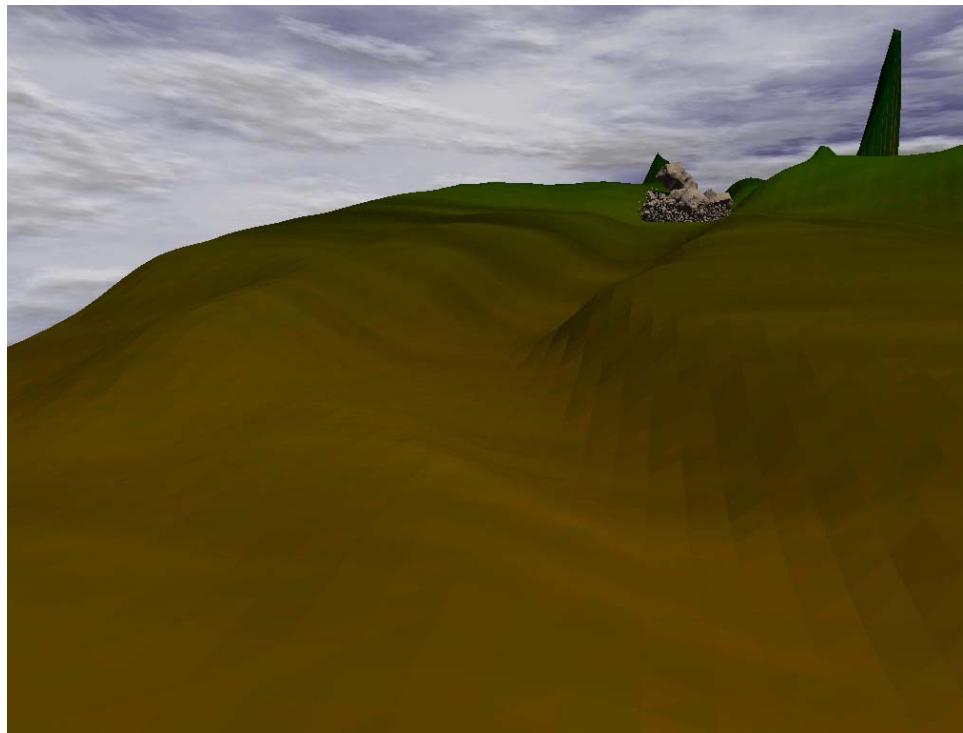
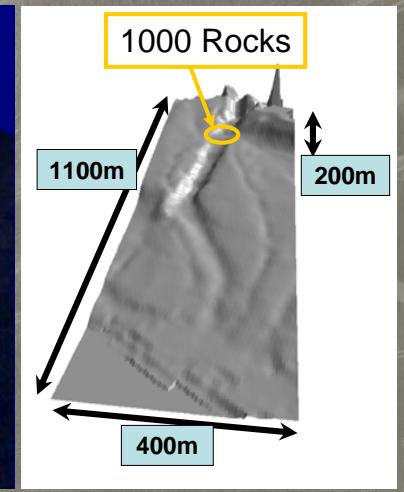
damper



## Rock Fall Simulation



Digital Elevation Data



## Guard Fence for Rock Fall



Digital Elevation Data

