

Department of Mechanical and Control Engineering

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Analysis of a damped one degreeof-freedom vibration system (1)

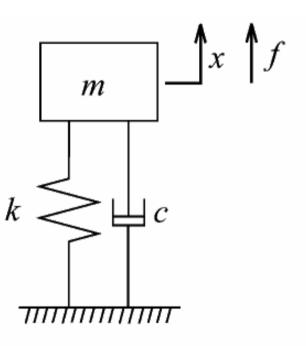


Fig.3 Damped one-degree-of-freedom vibration system

$$m\ddot{x} + c\dot{x} + kx = f$$

Analysis of a damped one degreeof-freedom vibration system (2)

Free Vibration

$$m\ddot{x} + c\dot{x} + kx = 0$$

Free Vibration Response

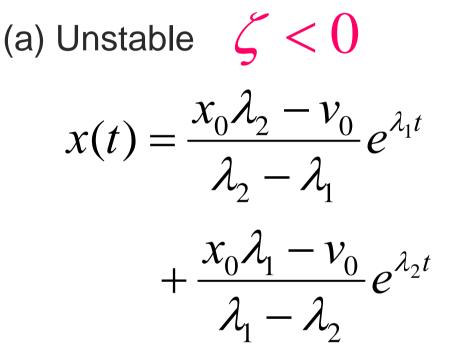
$$x(t) = C_1 e^{\lambda_1 t} + C_2 e^{\lambda_2 t}$$

where

$$\lambda_{1,2} = -\zeta \omega_n \pm \omega_n \sqrt{\zeta^2 - 1}$$

$$\zeta = \frac{c}{2\sqrt{mk}} \quad \text{Damping Ratio}$$

Damping ratio and initial value response (1)



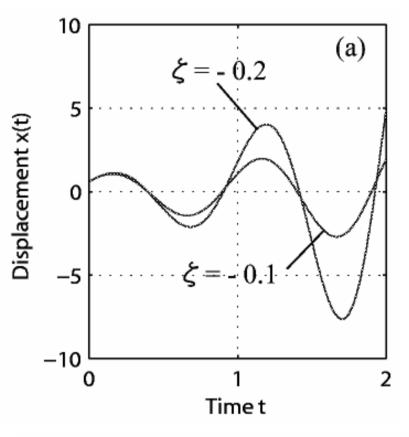
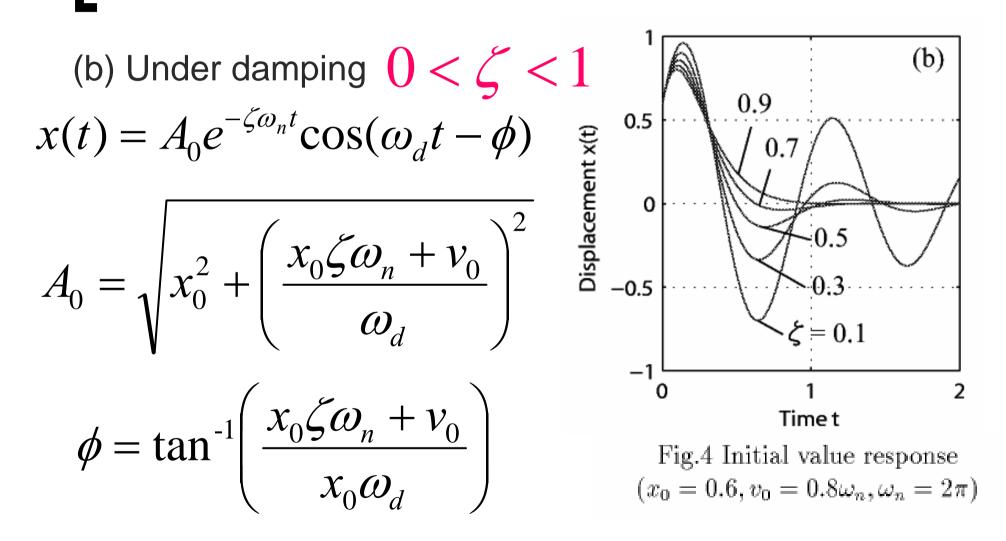


Fig.4 Initial value response $(x_0 = 0.6, v_0 = 0.8\omega_n, \omega_n = 2\pi)$

Damping ratio and initial value response (2)



Damping ratio and initial value response (3)

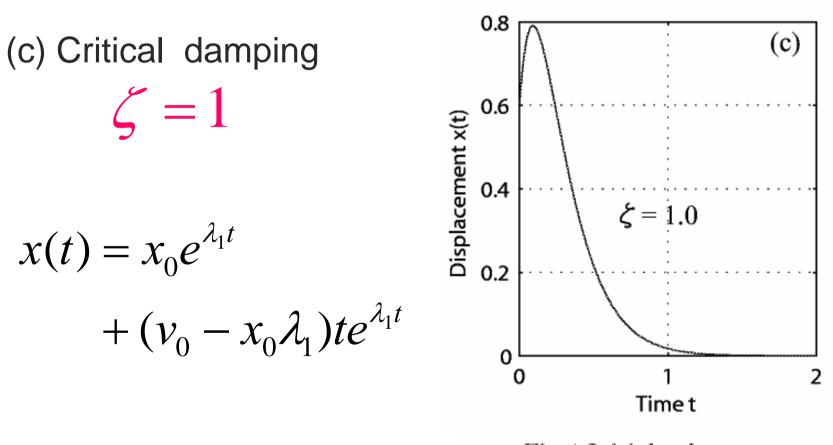
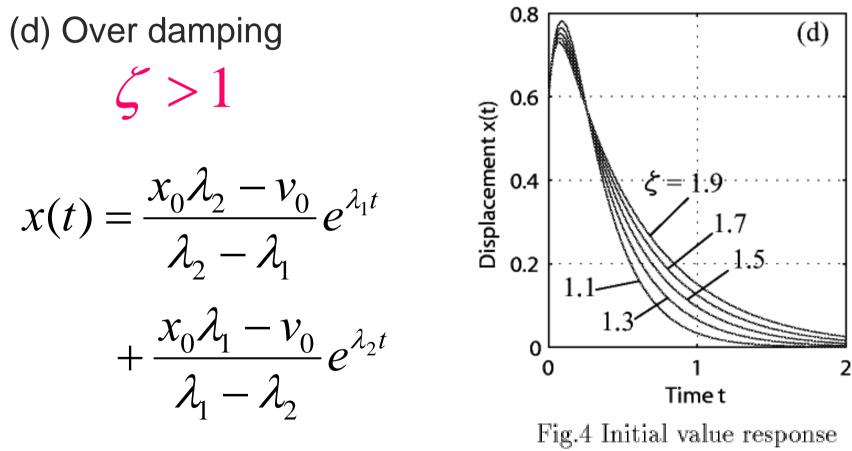


Fig.4 Initial value response $(x_0 = 0.6, v_0 = 0.8\omega_n, \omega_n = 2\pi)$

Damping ratio and initial value response (4)



 $(x_0 = 0.6, v_0 = 0.8\omega_n, \omega_n = 2\pi)$

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