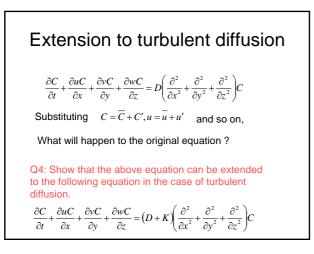
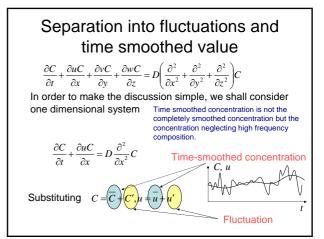
Urban Environmental Engineering 4

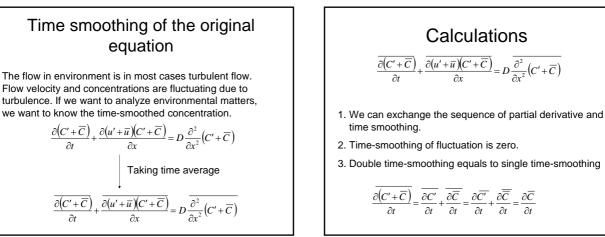
Taro Urase Tokyo Institute of Technology

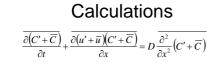
Lecture in the last time

- Diffusion
 - Molecular diffusion
 - Turbulent diffusion
 - Dispersion









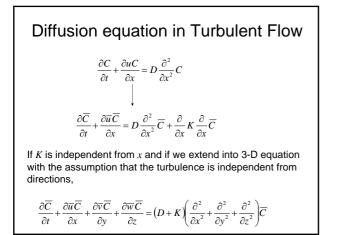
- 1. We can exchange the sequence of partial derivative and time smoothing.
- 2. Time-smoothing of fluctuation is zero.
- 3. Double time-smoothing equals to single time-smoothing

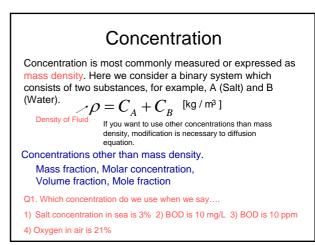
$$\frac{\overline{\partial (C' + \overline{C})}}{\partial t} = \frac{\overline{\partial C'}}{\partial t} + \frac{\overline{\partial \overline{C}}}{\partial t} = \frac{\partial \overline{C'}}{\partial t} + \frac{\partial \overline{\overline{C}}}{\partial \overline{t}} = \frac{\partial \overline{C}}{\partial t}$$

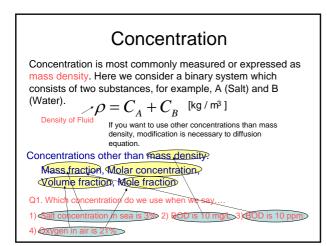
Calculations (cont.)

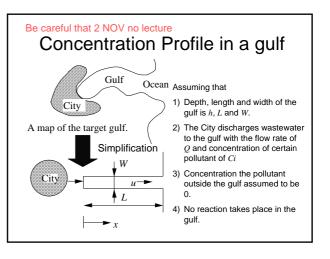
$$\frac{\overline{\partial(u'+\overline{u})}(C'+\overline{C})}{\partial x} = \frac{\overline{\partial u'C'}}{\partial x} + \frac{\overline{\partial u'\overline{C}}}{\partial x} + \frac{\overline{\partial \overline{u}C'}}{\partial x} + \frac{\overline{\partial \overline{u}\overline{C}}}{\partial x}$$

$$= \frac{\overline{\partial u'C'}}{\partial x} + \frac{\overline{\partial u'\overline{C}}}{\partial x} + \frac{\overline{\partial \overline{u}C'}}{\partial x} + \frac{\overline{\partial \overline{u}\overline{C}}}{\partial x} = \begin{bmatrix} \overline{\overline{\partial u'C'}} \\ \overline{\partial x} \\ \end{array} + \frac{\overline{\partial \overline{u}\overline{C}}}{\partial x}$$
In the case of Navier Stokes equation, we considered the correlation between u' and v' and we introduced a concept of Reynolds Stress. If no correlation is found between u' and C', the term u'C' will be zero. However, as we considered in the Reynolds stress, we introduce the following relationship as an analogy with Fick's law.
$$\overline{u'C'} = -K \frac{\overline{\partial \overline{C}}}{\partial x}$$









Be careful that 2 NOV no lecture Concentration Profile in a gulf (cont.)

Question

The mass flux in the gulf in steady state can be written as

$$J = uC(x) - D\frac{dC(x)}{dx}$$

The average velocity in the gulf is $u = \frac{Q}{Wh}$

1) Derive the equation $Q(C(x)-C_i) = hWD \frac{dC(x)}{dC(x)}$

- 2) Give the solution which satisfies at the mouth of the gulf to the ocean.
- 3) Draw a figure which shows concentration profile and give an explanation of the effect of *Q/hWD* on the profile.

